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Systematic sensitivity analysis of the full economic impacts of sea level rise

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Abstract: The potential impacts of Sea Level Rise (SLR) due to climate change have been widely studied in the literature. However, the uncertainty and robustness of these estimates has seldom been explored. Here we assess the model input uncertainty regarding the wide effects of SLR on marine navigation from a global economic perspective. We systematically assess the robustness of Computable

General Equilibrium (CGE) estimates to model's inputs uncertainty. Monte Carlo (MC) and Gaussian Quadrature (GQ) methods are used for conducting a Systematic Sensitivity Analysis (SSA). This design allows to both explore the sensitivity of the CGE model and to compare the MC and GQ methods. Results show that, regardless whether triangular or piecewise linear Probability distributions are used, the welfare losses are higher in the MC SSA than in the original deterministic simulation. This indicates that the CGE economic literature has potentially underestimated the total economic effects of SLR, thus stressing the necessity of SSA when simulating the general equilibrium effects of SLR. The uncertainty decomposition shows that land losses have a smaller effect compared to capital and seaport productivity losses. Capital losses seem to affect the developed regions GDP more than the productivity losses do. Moreover, we show the uncertainty decomposition of the MC results and discuss the convergence of the MC results for a decomposed version of the CGE model. This paper aims to provide standardised guidelines for stochastic simulation in the context of CGE modelling that could be useful for researchers in similar settings.

JEL classification: C68, Q54

Key words: CGE, Sea Level Rise, Systematic Sensitivity Analysis, Monte Carlo, GTAP

1 Introduction

Sea-level rise (SLR) is one of the most studied impacts of climate change within the environmental economics literature. Researchers have used, among other methods, Computable General Equilibrium (CGE) models to assess the wider economic implications of SLR for a number of different climate change scenarios [Bosello et al. (2012a), Bosello et al. (2012b), Bosello et al. (2007), Darwin and Tol (2001), Deke et al. (2001)]. An extension to the aforementioned models includes the assessment of the broader economic impacts of SLR-induced coastal land and capital losses and their effect on sea transportation networks [Chatzivasileiadis et al. (2016)].

Climate change-induced transportation disruptions, through productivity losses in sea transport, can have a substantial effect on the global economy. Productivity losses affect the transportation costs which in turn may increase the market prices of transport-intensive products. Based on the IPCC RCP8.5 scenario, Chatzivasileiadis et al. (2016) show that climate change-induced transportation disruptions including coastal land and capital losses, could causes global welfare losses of circa USD 61 billion in 2050.

Most of the preceding studies have used CGE models to look at the economic implications of SLR using input data from a variety of sources to estimate the exogenous shock to the economy caused by SLR. Land loss is the most used link between SLR and changes in economic activity. In models such as the Dynamic Interactive Vulnerability Assessment (DIVA) model [Hinkel (2005), Hinkel et al. (2013), Hinkel et al. (2014), Vafeidis et al. (2008)], land loss is estimated as a function of SLR. Based on the IPCC RCP8.5 scenario, the expected mean SLR in cm by the year 2100 is 74 cm with a range of [52, 98] relative to the mean over 1986-2005 (IPCC, 2013). This range of almost half a meter reflects the level of uncertainty regarding the estimates of SLR. Consequently, land loss estimates and economic assessments connected to those SLR values will suffer from a much higher level of uncertainty that gets compounded in the different modelling stages.

A well-documented approach to address input uncertainty within a CGE model consists in performing a Systematic Sensitivity Analysis (SSA). In order to perform a SSA we make a set of explicit assumptions on the probability distribution of the exogenous inputs for which uncertainty is high [Arndt (1996), Arndt and Pearson (1996), DeVuyst and Preckel (1997), Horridge et al. (2011)]. The end goal of this process is to estimate the statistical moments of the model outputs that are driven by the underlying uncertainties of the exogenous model inputs, such as stochastic shocks or parameters [Villoria and Preckel (2017)].

This paper is the first to address the model input uncertainty regarding the wide effects of SLR on marine navigation from a global economic perspective. The analysis is based on a model that assesses the macroeconomic implications, both direct and indirect (general equilibrium), of climate change induced transportation disruptions by taking into account the direct loss of land and capital [Chatzivasileiadis et al. (2016)]. Our goal is to systematically assess the robustness of the CGE model results under the existing uncertainty of the model's inputs by means of a Monte Carlo (MC) and a Gaussian Quadrature (GQ) SSA design. We look at the differences in results produced by distinct choices of probabilistic distributions for the MC analysis and we also include an uncertainty decomposition of the results.

Section 2 reviews the literature on CGE assessments of the SLR wide economic impacts, and the different methods of SSA applied within CGE context. Section 3 discusses the methods and data we used for our assessment. Section 4 presents the results of the SSA and Section 5 concludes.

2 Literature review

2.1 Loss of productive resources

The literature simulating the effects of SLR on the economy using a GCE model is rather limited. Starting from Darwin and Tol (2001), SLR is linked to the economy-wide effects through a decrease in the endowment of land and capital in the economy. Based on the FUND model the authors estimate the exogenous shocks for land and capital based on the Global Vulnerability Assessment by Hoozemans et al. (1993) and other sources. The authors conclude that the uncertainty surrounding land and capital endowments threatened by sea level rise is substantial. Bosello et al. (2007) estimate the costs of 0.25 meters of global SLR based on a CGE model where SLR is also modelled as a reduction of the endowment land available. Their data sources are the same as in Darwin and Tol (2001) but the analysis is based on the GTAP model. Similarly, Bosello et al. (2012a) based on input

data from the DIVA model estimate the wide-economic effects of SLR focusing on land losses for Europe only using the same link between SLR and economy-wide effects as all the articles above. The aforementioned literature has focused on the full economic effects of SLR through land loss and coastal protection, ignoring changes to the transportation sector.

Chatzivasileiadis et al. (2016) look at the impact of SLR on transport infrastructure based on the GTAP model using the DIVA output as input. SLR is linked to economy-wide effects as a reduction of the available regional endowments of land and capital. SLR is then linked to regional productivity changes in the water transport sector based on the amount of land lost and on the flood costs each region will face in 2050.

To our knowledge, none of the existing papers has extended the analysis of the full economic effects of SLR to reflect the combined effects of input uncertainty in a systematic way. The novelty of this paper is that it addresses the model input uncertainty through a systematic sensitivity analysis in the link between SLR and economy wide effects by extending the analysis of Chatzivasileiadis et al. (2016).

2.2 Applications of SSA in the CGE literature

The results of CGE models depend heavily on the calibration of the model and the exogenous shocks applied to the system. Harrison and nod (1992) stress the need for SSA that can capture, to some extent, the uncertainties surrounding CGE models. Different methods of stochastic modelling have been explored to address the underlining uncertainties of CGE models, namely the GQ approach and MC methods. Both methodologies have addressed the sensitivity of CGE models with respect to parameters (endogenous variables) and model inputs (exogenous shocks).

Stochastic modelling is computationally intensive, thus the literature has focused mostly on the GQ approach for SSA which requires only a few data points to approximate the central moments of stochastic variables. Practical examples of this method can be found in Arndt (1996), Arndt and Pearson (1996), Preckel et al. (2011), Artavia et al. (2015).

In general, the literature has mostly avoided the use of MC methods for sensitivity analysis in CGE models. Looking back, we can find Harrison and nod (1992) that focus on two elasticities for 15,000 separate solutions to derive the central moments of the results. The same methodology was applied by Harrison et al. (1997) based on 1,000 realisations of the model elasticities in order to obtain the central moments of the outputs. Much later, Villoria and Preckel (2017) directly compare the GQ approach to MC for systematic sensitivity analysis within a CGE model. The authors conclude that the use of MC methods for implementing stochastic simulations has some advantages over GQ due to the advances in software and hardware available and the flexibility of the MC methods.

We contribute to the existing literature by applying a Monet Carlo SSA on a pre-existing static CGE model [Chatzivasileiadis et al. (2016)], where the input uncertainty regarding the SLR, as derived from the DIVA model, is substantial. Our purpose is threefold: to explore the sensitivity of the CGE model; to compare the MC and the GQ SSA methods; and more importantly, to set foundations for more standardised analysis for the future research by discussing the appropriate distributions that could be used in similar settings. We additionally discuss, for the first time, the uncertainty decomposition of the MC results and discuss the effects of decomposing the MC analysis into parts based on the shocks used in the CGE model. Last but not least, we developed a Stata program code that can be used to conduct the analysis discussed below using the DIVA dataset as input.

3 Methods and data

3.1 The base CGE model

Following Chatzivasileiadis et al. (2016), we explore the input sensitivity of the latest version of the GTAP multi-sector / multi-country model that assesses the impact of sea level rise on transport infrastructure. The authors link SLR to economy-wide effects through a reduction of the available land and capital endowments, using the benchmark equilibrium dataset of GTAP 8. The effect of SLR on water transportation infrastructure is modelled as a reduction of the sea-port productivity relative to land and capital loss in two separate scenarios named DIVA_L and DIVA_C. Both scenarios include a combination of the same exogenous shocks for land and capital losses and their differentiation is in

the source of the productivity shocks. In DIVA_L productivity reduction is dependent on land losses and in DIVA_C on sea-flood damage costs.

Data on the input variables described above are derived from the Dynamic Interactive Vulnerability Assessment model (DIVA). The DIVA model is an integrated impact-adaptation model of coastal systems that analyses the biophysical and socio-economic effects of SLR and socio-economic development on a regional and global scale. The DIVA model incorporates coastal erosion, coastal flooding, wetland changes and salinity intrusion. Additionally, adaptation to SLR is taken into account in terms of raising dikes and nourishing shores and beaches [Hinkel (2005), Hinkel et al. (2013), Hinkel et al. (2014), Vafeidis et al. (2008)].

The outputs of DIVA for the year 2050 used in this study were constructed using the RCP 8.5 (J14) radiative forcing and the SSP2 socio-economic scenarios. For the analyses below, we use the two outputs of the DIVA model described above: land losses due to submergence and, expected sea-flood damage costs due to SLR. The projected global mean SLR for 2050 and the uncertainty distribution (5th, 17th, 50th, 83rd, 95th and 99th percentiles) are derived from Jevrejeva et al. (2014). Those values are then used in the DIVA model to estimate the land losses due to submergence and expected sea-flood damage costs due to SLR for each percentile separately (e.g Spencer et al. (2016)).

3.2 Systematic Sensitivity analysis design

Similar to Arndt (1996), we define the general form of a computable general equilibrium model as:

$$G(x,\beta) = 0 \tag{1}$$

where x represents a vector of results or endogenous variables (such as prices, welfare etc.) and β a vector of exogenous variables. The solutions of the system of Equation 1 can be defined as $x^*(\beta)$. Then, given the non-zero probability density function (pdf) p over a multiple dimension domain Ω for the exogenous random variables part of β we can define $x^*(\beta) \equiv K(\beta)$ as a vector of results for each given parameter β . The calculation of the mean in the univariate case takes the form of:

$$\bar{x} = E[K(\beta)] = \int_{a}^{b} K(\beta) p(\beta) d\beta$$
(2)

and the calculation of the variance can be done by:

$$Var(x) = E\left[\left(K(\beta) - \bar{x}\right)^2\right] = \int_a^b \left(K(\beta) - E[K(\beta)]\right)^2 p(\beta) d\beta$$
(3)

In order to evaluate equations 2 and 3, two distinct approaches have been used, methods based on quadrature formulas (i.e. GQ) and MC sampling. Each approach has its advantages and limitations¹. These methods are commonly used due to the difficulty or impossibility of analytically evaluating equations 2 and 3.

Going back to equation 2, based on a Riemann sum we can approximate the integrand by:

$$\int_{a}^{b} K(\beta) p(\beta) \mathrm{d}\beta \approx \sum_{n=1}^{N} w_{n} K(\beta_{n})$$
(4)

and in the multivariate version the central k^{th} moment is approximated up to order d by:

$$\int_{\Omega} \left[\prod_{j=1}^{J} K(\beta_j)^{r_j} \right] p(\beta) \mathrm{d}\beta \approx \sum_{n=1}^{N} w_n \prod_{j=1}^{J} K(\beta_j)^{r_j}$$
(5)

where $\sum_{j=1}^{J} r_j \leq d$ and N is the number or realizations and w_n is the weight associated with each realization.

Up to this point both SSA methods (GQ and MC) follow the same methodology. The differentiation comes in the number or realizations required and the way w_n is defined. In the MC sampling method, we generate N pseudo-random numbers based on the $p(\beta)$ distribution and evaluate equations (2) or (5), N times, where $w_n = (\frac{1}{N})$ for each realization n. If N is sufficiently large then \bar{x} as defined by equations 4 and 5 is an unbiased estimator of $K(\beta)$.

¹ For more information see Fishman (2013)

The idea behind the GQ is to keep the number of the integrand evaluations N small by choosing the most appropriate points within the interval [a,b] and associated weights w_n (see equation (5)). The choice of points and probabilities is done in such a way that the crude moments of the approximating distribution equal the moments of the true distribution from zero to some specified order [Villoria and Preckel (2017)]. Once points and probabilities have been chosen, the moments can be calculated through equations (4) and (5) as above.

The GEMPACK software [Harrison et al. (2014)] provides an easy implementation of SSA based on GQ. The SSA is constrained for up to degree 3 quadratures for *symmetric distributions*. The equally weighted points estimated by the GEMPACK software are between 2S and $4S^2$, based on the Struod and Liu quadrature respectively [Stroud (1960), Liu (1997)]. The build-in version of the SSA in the GEMPACK allows for use of the *Uniform* and *Triangular* distribution.

As mentioned in Section 2.2, the CGE literature has focused mostly on the GQ approach for SSA. An important issue with the GQ proposed by Struod and Liu is that they restrict the variation around the mean of each random variable to no more than $\sqrt{2\sigma}$ in Struod quadrature and σ in Liu quadrature. Villoria and Preckel (2017) mention on the matter that:

[...] by taking the GQ approach, considerable information has been lost regarding the shape of the distribution, its higher order moments, and its range. This may be especially important in instances where the shocks can be expected to have asymmetric impacts. These applications likely include **productivity shocks associated with climate change**[...]

Preckel et al. (2011) attempt to solve this issue by proposing a change in the sampling method of Struod and Liu by implementing a broader sample technique. Similarly, Artavia et al. (2015), propose the use of MC methods to tackle this problem of low accuracy where the shocks' distribution is constrained by the Struod and Liu requirements.

Given the aforementioned information, the advantages of the MC method for SSA for the model developed by Chatzivasileiadis et al. (2016) becomes clear. On the one hand, the biggest advantage of GQ which is its ability to economise the SSA to only a few model runs does not necessarily hold in practice. In our case, the required number of simulations is **4096**, based on the parameters used in the SSA within the GEMPACK software. On the other hand, the analysis of Chatzivasileiadis et al. (2016) is based on *sea-port productivity shocks associated with climate change* and thus the problem of asymmetric impacts within the GQ method, as described above, becomes prominent. Another advantage of the MC method lies on the estimation of the error. In the MC method, the error is estimated from the generated data, whereas in the QG more global measures of error estimation are required such as the Chebyshev's inequality for the confidence bounds. The Chebyshev's inequality, will produce confidence bounds that are extremely conservative compared to the Central Limit Theorem which provides narrower confidence intervals if the available number of data points is sufficiently large [Fishman (2013)].

3.3 Monte Carlo sampling method

Before performing SSA with the MC method, we need to select the input variables of interest and make assumptions about the distributions they follow.

In the original model of Chatzivasileiadis et al. (2016), the exogenous parameters that are shocked to simulate the impacts caused by SLR to the global economy and in particular to the water-transportation sector (see Sec. 3), are: 1. *Land loss due to submergence, 2. Sea-flood damage costs and 3. Sea-port productivity losses.* It is important to note that if data for a goodness of fit test is not available, the selection of a probability distribution is rather subjective and arbitrary. However, the selection ideally has to reflect our perception regarding the characteristics of the process we are trying to represent (and its uncertainty). One important point to take into account can be how fast the tail of the distribution that is proposed decreases (e.g., a uniform distribution may considerably overestimate the probability of very large land losses; a triangular distribution may still be over estimating the probability of large losses but less than the uniform; a normal distribution has faster decaying tails, but it would be inadequate because it is symmetric and it supports the interval $(-\infty, \infty)$). The selection of the distribution should also reflect that the values the process can take may be limited by some physical constraints. For example, a probability distribution for land loss may be limited beyond a certain value from which it is impossible to have larger losses (right tail truncation). For sea-flood damage

 $^{2\,}$ Where S is the number of individual shocks included in the simulation

costs, apart from the problem of how fast the tails should decrease, the selected distribution should reflect that this variable cannot take negative values (left tail truncation). In this case, the exponential or the Gamma distribution could be appropriate. For sea-port productivity losses a triangular distribution could be used, although a distribution with faster decaying tails could be more desirable, such as the Beta distribution.

Figure 1 presents for MC and GQ percentiles and maximum values of percentage changes in sea port productivity for the DIVA_C and DIVA_L scenarios. As indicated in Section 3, only the 5th, 17th, 50th, 83rd, 95th and 99th percentiles of the DIVA data are available. Given the limited information about the DIVA data distribution, a triangular distribution (td) was chosen to represent all parameters. This is a common choice to represent parameters and variables when little information about their distribution is available 3 . Above that, this selection was made to preserve comparability with the GQ method, as implemented in the GEMPACK software. Otherwise, the parameters used in the two methods would probably not have similar mean and variance. This is due to the fact that the Struod and Liu quadrature was developed for symmetric distributions, whereas asymmetries are present in our data (see Figure 1). An additional set of analyses is conducted using the piecewise linear probability distribution (lpd) [Kaczynski et al. (2012)]. The lpd is a non-parametric probability distribution created using a piecewise linear representation of the cumulative distribution function⁴. Based on the DIVA data we have six points of the cumulative density function (cdf), thus six different slopes are used to generate the lpd data. This method does not impose a distribution shape as the td does and follows the data more closely. An advantage of the lpd over the td is that it uses all available information provided by the DIVA data and not just three points.

For the triangular distribution we assume that the 50th percentile for each region is the most plausible value and we restrict the distribution to the interval [99th, 5th]. This ensures the values for capital to be positive. We then generate 10,000 realizations for each of the three variables of interest, for every region in the model. This process was repeated twice once for the DIVA_C and once for the DIVA_L scenario. For the pld, we generate 15,000 realizations for each of the three shocks of interest, for every region in the model as above. A higher number of realizations is used in the lpd to avoid convergence problems that could be created by this sampling method. Table 1 shows the first two moments of the 10,000 td and 15,000 lpd realizations for each of the three variables for every region in combination with Figure 1, 2 that shows the productivity shock distributions for every region\scenario.

Additional attention is required in the estimation of the sea-port productivity shocks for the minimum and the maximum of the triangular distribution. Following Chatzivasileiadis et al. (2016), we get the land and capital shocks separately from the data for the 5th and the 99th percentile from the DIVA model. Then we estimate the ratio between each limit⁵ and the 50th percentile. So, we generate the the minimum and the maximum for the sea-port productivity shocks by multiplying each ratio to the Chatzivasileiadis et al. (2016) sea-port productivity shocks⁶. In cases where the new productivity shocks for the 99th percentile are higher than 50% we cut the value to 50%⁷.

In the generation process of the pseudo-random realizations for both MC SSA we made a set of additional assumptions regarding the distribution of the input parameters. Taking a closer look at Figure 1, we see that there are differences between the GQ and the MC maximum values. For the DIVA_C the difference is only in North East Europe, whereas in the DIVA_L the differences are apparent in all regions. Africa is a special case in the DIVA_L scenario, for the upper limit used in the GQ, where the upper limit is negative. The assumption of Chatzivasileiadis et al. (2016) is that the productivity changes due to SLR are proportional to the land loss or the sea-flood costs each region faces by 2050. Based on the DIVA model, and considering the left tail of the distribution (5th percentile), North East Europe sees gains in land due to negative SLR. That would mean, according to Chatzivasileiadis et al. (2016), that the sea-port productivity would *increase* due to the lower water levels. Jonkeren et al. (2007) show that, for inland water transport, lower water levels increase the freight prices as a result of lower productivity. Moreover, looking at the *GQ upper limit* in Figure 1, for the DIVA_L model, we see that due to the fact that the Struod and Liu quadratures where developed for symmetrical distributions, given the distance between the 50th and the 99th percentile the maximum is consistently positive, thus assuming productivity *gains* from sea level changes. For those

³ Other examples in the literature indicating that the triangular distribution is appropriate in similar cases are: Hoffman and Hammonds (1994), Johnson (1997), Korteling et al. (2013), Caralis et al. (2014)

Based on the MathWorks Matlab 2016

⁵ The 5th and the 99th percentiles.

⁶ The Chatzivasileiadis et al. (2016) sea-port productivity shocks where calculated using the 50th percentile form the same dataset.

⁷ We assume that 50% of sea-port productivity losses is the maximum level of extreme losses ports can endure before urgent protection measures, in all regions, take place

reasons, we have decided to restrict the distribution in the MC SSA to zero on the one side. This way, we can include cases where no changes to sea-port productivity have occurred even though there are land and capital losses.

3.4 Supplementary code

This paper is coupled with a code for Stata that, based on the DIVA data for our 13 regions, recreates the analysis discussed above. Starting from the initial dataset (downloaded through the code automatically), the user can choose the type of SSA to be conducted. The idea is based on the fact that the GEMPACK software, usually used for simulations based on the GTAP model, does not have a built-in function for conducting MC SSA yet. Due to the nature of the data, to this point, the code allows for sampling based on the td and the pld. When the number of simulations (chosen by the user) is completed, the program collects the data (inputs and outputs) into a csv file that is then fed to Stata for further analysis. A first version of the code can be found on GitHub⁸.

4 Results

For simplicity, we focus on just two results of the CGE model, namely the Hicksian Equivalent Variation (HEV) and the percentage change of regional GDP (qGDP, see appendix A.1). The HEV can be thought of as the dollar amount that the consumer would be indifferent about accepting in lieu of the shock caused by, in our case SLR; it is negative if the consumer would be worse off after the shock due to SLR [Mas-Colell et al. (1995)]. The other variable discussed, qGDP is the percentage change of regional GDP between the two equilibria i.e pre and post SLR. Tables 2, 3 and 4, show the results for both the DIVA_C and DIVA_L scenarios using both MC and GQ SSA, respectively. The tables also include the first two central moments for HEV and qGDP. Additionally, the upper and lower 95% confidence interval for each region have been included⁹. In order to make the comparison easier we have calculated the ratio of the MC means to the GQ means for each region (Table 5). To better explain the differences between DIVA_C and DIVA_L produced by the MC and QG method we also present the histograms of productivity shocks by region in Figures 2 and 3.

We start the analysis of the results from the DIVA_C scenario where the inputs for all three SSA methods are the same (see Figure 1) with the exception for North-East Europe. Even though the three points of the cdf used in the sampling process of the shocks are the same for each region the distribution of shocks used by the MC-td and the QG SSA methods seem to be different (see Figure 3). As indicated by Villoria and Preckel (2017), a significant amount of information is ignored by the GQ method regarding the shape of the distribution, its higher order moments, and its range. This information is very important in our case given that we are interested in productivity shocks associated with SLR, which potentially can have asymmetric impacts. The ratio of the two means presented in Table 5 shows that the two methods produce different results for all regions, even though they have similar input. The ratio of the mean is higher than 1.0^{10} indicating that the MC-td gives consistently higher estimates for both HEV and qGDP. China is the exception, where HEV results are identical. This underestimation of the QG could be due to poorly chosen discrete shock values produced by Liu Quadrature for variables that the model results are sensitive to. In North-East Europe with just a slight difference in the upper bound of the input distribution (0% productivity reduction in MC compared to 2.49% increase in GQ), we see that the HEV and qGDP results of the MC-td method is 2.4 and 2.7 times higher respectively (in absolute terms) compared to the GQ estimates.

Tables 2, 3 and 4 show that the results of the MC-lpd are similar to the ones produced by the GQ method with the exception of the three European regions where the MC-lpd results are higher. Additionally, there seems to be a significant difference between the two MC methods. This result is not surprising since the distribution chosen in the sampling process affects the final results significantly as discussed above (see 3.3§2). The Box-Plot in Figure 4 can give a clearer representation of the output distributions for each region under both MC methods¹¹.

The SSA methods show that the DIVA_C results produced by Chatzivasileiadis et al. (2016) are robust to the variations of SLR. The SSA mean results are similar to the ones reported by Villoria and

 $^{^8}$ https://github.com/eco056/SLR-DIVA_MC/archive/master.zip

⁹ In the GQ method the 95% Chebyshev's bound has been calculated based on: $(mean - \sqrt{20} \cdot SD, mean + \sqrt{20} \cdot SD)$.

¹⁰ Ratios are rounded at one decimal point.

¹¹ The Box-Plot for for GQ was not produced since the method generates *approximations* of the mean and standard deviation from numerical integration, but not distributions.

Preckel (2017), but not identical (see columns SIM and Mean in Tables 2, 3 and 4), except North-East Europe. It seems that the asymmetric td used in MC method for North-East Europe generates significantly larger means for HEV and qGDP (in absolute terms) compared to the GQ method. The sign and magnitude of the effects are robust to the variations of SLR based on the 95% confidence intervals¹², indicating that there is *no evidence of input sensitivity* present. Taking a closer look at Tables 2 and 3, we see that the global HEV losses are consistently higher in all SSA methods indicating possibly that the existent SLR CGE literature has underestimated the effects SLR on the global economy.

4.1 Convergence speed and decomposition

Figures 5 and 6 show the convergence speed of the mean and confidence intervals as the number of simulations increases in the MC-td SSA for HEV and qGDP respectively. These plots illustrate the sample size required by the MC process based on the speed of convergence of the results. Even though there are regional differences, it seems that 4,000 simulations are sufficient for the mean and confidence intervals (CI) to settle down. The theoretical point of convergence as shown on the graphs as reference lines is based on the Raftery and Lewis' diagnostic¹³ for Markov Chain MC [Raftery and Lewis (1992)].

Knowing the point of convergence for each output we expand our analysis by decomposing the CGE simulation to its components i.e.; 1. Land loss due to submergence, 2. Sea-flood damage costs and 3. Sea-port productivity losses. This is possible because CGEs are locally linear, i.e., the effect of a joint shock is the sum of the effects of the single shocks. This implies that we can run three MCs, one foe each exogenous variable, with K runs rather than one MC with 10,000 runs. We have used K = 4000 based on the Raftery and Lewis' diagnostic. The purpose of this experiment is to identify potential differences between the total and the decomposed CGEs results within the MC SSA. As above, we sample values for each region/exogenous variable based on the triangular distribution using the same seed for each region in the sampling process as before. After all simulations for each component are done, the separate HEVs and qGDPs are summed to produce the total effect of the three exogenous variables. Since the GTAP model is not linear this type of decomposed CGE results. In the MC analysis though, this error is expected to be averaged out as the number of simulation increases.

Looking at figures 5 and 6 the results of the total and decomposed CGEs for the MC-td of the DIVA_C scenario are identical. Exception is JaKoSing¹⁴ where the decomposed CGE produces slightly higher results. Interestingly, the upper and lower bound in North West and South Europe for qGDP, only, seem to be wider in the decomposed CGEs. This shows that the interaction component of the CGE model actually has an effect. Additionally the lower bound of the Raftery and Lewis's diagnostic is slightly lower in decomposed CGE experiment. This difference though is not large enough to indicate that the decomposed MCs require a smaller number of runs in total (here 3 * K) than the initial MC.

4.2 Uncertainty decomposition

The limited up-to-date literature on MC SSA of CGE models does not pay attention to assessing the impact of parameter uncertainty on the uncertainty surrounding the MC CGE results. Following Anthoff and Tol (2013), we run a regression of the MC inputs on the CGE outputs and compute the standardized regression coefficients. The standardized regression coefficient shows how many standard deviations the dependent variable will change for a one standard deviation change of a given independent variable, cette paribus [Landis (2014)]. Essentially, the regression will indicate the impact of a model parameter on the results after removing the impact of all other parameters. We use this method to identify the relative importance of each exogenous variable by linearising the model in the regression and thus capturing local sensitivities only. For simplicity we present the results of the uncertainty decomposition for the DIVA_C MC-lpd HEV and qGDP results only.

Figure 7 shows the four regional parameters that have the largest effect (in absolute terms) on HEV and qGDP by region. Tables A.2 and A.3 in the appendix include all 39 coefficients of the

¹² or the Lower and Upper Chebyshev's bound for 2 SDs.

¹³ Based on the runmlwin and MLwiN programs for Stata [Leckie and Charlton, Rasbash et al. (2009)]

¹⁴ See regional aggregation in appendix Table A.1.

standardized regression for each region\parameter. As expected in most regions the regional productivity losses has the highest effect on HEV and qGDP. Additionally land seems to have little to no effect on the final results since the coefficients are not significant for most regions. Interestingly, the developed regions' qGDP is affected more by the capital changes rather than the productivity losses in comparison to HEV. Figure 7 also shows the way regions are connected. For example the HEV and qGDP in Africa are not only affected by capital and productivity losses in Africa, but also by changes in Central Asia and North West Europe. In order to understand these connections better we show the two heat-map tables¹⁵ (6 and 7). It is clear that the HEV is generally more affected by the productivity changes rather than the capital changes. JaKoSing and the three European regions, seem to have a negative response (on both HEV and qGDP) to seaport productivity changes from almost all other regions.

5 Discussion and Conclusion

We estimate the input sensitivity in the simulation of the economy wide effects of productivity losses in the marine transportation sector due to sea level rise using the GTAP CGE model with 13 regions. Based on Chatzivasileiadis et al. (2016), we analyse two different scenarios for productivity changes. By comparing the MC SSA with the Liu GQ it becomes clear that small differences in the parameters of even the same distribution (here td) can cause significant changes in the outputs of the SSA. We show that in the case of productivity changes due to SLR -where shocks have asymmetric impactsthe MC method is the best choice for conducting SSA due to the potential information loss in the shocks generated by the GQ method. Based on the results of this paper, there is no evidence of input sensitivity in the DIVA_C scenario. Comparing the welfare losses of the two scenarios between Chatzivasileiadis et al. (2016) and the SSA methods for the year 2050, we see that in the DIVA_C scenario the welfare losses are higher in both MC SSA's based on the triangular and piecewise linear probability distributions. This indicates that the CGE economic literature has potentially underestimated the total economic effects of SLR, thus stressing the necessity of SSA when simulating the general equilibrium effects of SLR.

We show that since CGEs are locally linear, a decomposition of the MC is possible based on the CGE parameters. Our results indicate that the decomposed MC converges approximately at the same speed as the total MC and the two methods produce identical results with the exception of the confidence bounds for qGDP in Europe. An important addition to the MC SSA of CGE literature is the uncertainty decomposition analysis. We show that land losses have a smaller effect compared to capital and seaport productivity losses. Additionally, capital losses seem to affect the developed regions GDP more than the seaport productivity losses.

There are issues that call for further research. First and foremost, both SSA methods the we applied assume that the shocks vary independently across regions and sectors. Based on the DIVA model, land loss due to submergence and sea-flood damage costs are a function of the level of SLR each region faces which indicates a certain level of correlation between them. Although, the assumption of independence can be sensible due to the fact that land loss due to submergence and sea-flood damage costs are also dependent on the level of protection to SLR each region has which we assumed to be uncorrelated among regions. Furthermore, we compare the MC SSA method with the relatively restrictive Liu QG of the GEMPACK software. Future analysis is needed on the use of broader sampling methods in the GQ as in Preckel et al. (2011) and the use of the MC filtering approach as in Mary et al. (2013).

6 Tables

7 Figures

¹⁵ See appendix Tables A.2 and A.3 for the significance levels

DIVA_C												
td Ipd												
	La	nd	Cap	ital	Produc	ctivity	La	nd	Cap	vital	Produc	tivity
Region	Mean	SD	Mean	SD	Mean	SD	Mean	SD	Mean	SD	Mean	SD
Africa	-0.002	0.001	-0.061	0.011	-12.019	2.280	-0.001	0.001	-0.055	0.013	-10.877	2.487
CAsia	-0.006	0.003	-0.072	0.017	-14.539	3.401	-0.004	0.003	-0.061	0.017	-12.412	3.514
China	0.000	0.000	-0.057	0.004	-11.161	0.771	0.000	0.000	-0.054	0.004	-10.648	0.744
EastAsia	-0.011	0.006	-0.128	0.028	-23.608	5.000	-0.007	0.007	-0.113	0.029	-20.903	5.387
EEFSU	-0.004	0.002	-0.036	0.010	-5.534	1.528	-0.003	0.001	-0.030	0.010	-4.629	1.581
JaKoSing	-0.018	0.012	-0.011	0.003	-2.027	0.476	-0.005	0.010	-0.009	0.003	-1.719	0.478
LatinAmerica	-0.001	0.001	-0.101	0.026	-21.091	5.578	-0.001	0.001	-0.085	0.027	-17.687	5.701
NAmerica	-0.003	0.001	-0.047	0.011	-7.972	1.878	-0.002	0.001	-0.040	0.011	-6.848	1.928
NEEurope	-0.002	0.001	-0.031	0.014	-4.843	2.248	-0.001	0.001	-0.018	0.012	-2.845	1.920
NWEurope	-0.002	0.001	-0.058	0.012	-10.586	2.210	-0.002	0.001	-0.049	0.011	-9.082	2.117
Oceania	-0.002	0.001	-0.097	0.022	-20.113	4.458	-0.001	0.001	-0.087	0.024	-17.971	4.956
SEurope	-0.008	0.004	-0.028	0.007	-4.233	1.127	-0.005	0.004	-0.023	0.008	-3.510	1.141
WAsia	0.000	0.000	-0.107	0.024	-21.353	4.767	0.000	0.000	-0.097	0.027	-19.288	5.399



				td			lpd						
	La	nd	Cap	ital	Produc	ctivity	La	nd	Cap	oital	Produ	ctivity	
Region	Mean	SD	Mean	SD	Mean	SD	Mean	SD	Mean	SD	Mean	SD	
Africa	-0.002	0.001	-0.061	0.011	-24.873	9.392	-0.001	0.001	-0.055	0.013	-21.481	12.055	
CAsia	-0.006	0.003	-0.072	0.017	-23.513	9.779	-0.004	0.003	-0.061	0.017	-20.805	11.626	
China	0.000	0.000	-0.057	0.004	-18.432	11.214	0.000	0.000	-0.054	0.004	-11.105	13.837	
EastAsia	-0.011	0.006	-0.128	0.028	-19.338	10.758	-0.007	0.007	-0.113	0.029	-13.144	12.376	
EEFSU	-0.004	0.002	-0.036	0.010	-18.845	6.612	-0.003	0.001	-0.030	0.010	-13.901	6.243	
JaKoSing	-0.018	0.012	-0.011	0.003	-17.965	11.304	-0.005	0.010	-0.009	0.003	-15.037	16.819	
LatinAmerica	-0.001	0.001	-0.101	0.026	-14.874	7.154	-0.001	0.001	-0.085	0.027	-9.234	6.625	
NAmerica	-0.003	0.001	-0.047	0.011	-14.571	5.479	-0.002	0.001	-0.040	0.011	-10.066	4.759	
NEEurope	-0.002	0.001	-0.031	0.014	-15.859	9.738	-0.001	0.001	-0.018	0.012	-6.932	8.016	
NWEurope	-0.002	0.001	-0.058	0.012	-9.908	3.757	-0.002	0.001	-0.049	0.011	-7.498	4.050	
Oceania	-0.002	0.001	-0.097	0.022	-25.968	8.580	-0.001	0.001	-0.087	0.024	-20.638	9.143	
SEurope	-0.008	0.004	-0.028	0.007	-26.213	8.744	-0.005	0.004	-0.023	0.008	-24.832	13.582	
WAsia	0.000	0.000	-0.107	0.024	-8.291	4.124	0.000	0.000	-0.097	0.027	-5.459	4.041	
		SD is t	he Standard De	eviation, td is	triangular distrib	oution and lpd is	pd is piecewise linear probability Distribution						



Fig. 1 Percentiles and MC\QG maximum in sea-port percentage productivity changes

Table 2	MC-td results and first two moments
Table 2	WiC-tu results and mist two moments

				DI	VA_C					
			Н	EV				qGDP		
Region	SIM	Mean	SD	LCI	UCI	SIM	Mean	SD	LCI	UCI
Africa	-3270	-3647	785	-3662	-3631	-0.070	-0.078	0.016	-0.078	-0.078
CAsia	-4107	-5065	1321	-5091	-5039	-0.094	-0.116	0.030	-0.117	-0.116
China	-7157	-7527	771	-7542	-7512	-0.072	-0.076	0.008	-0.077	-0.076
EastAsia	-4977	-6057	1617	-6089	-6025	-0.090	-0.110	0.026	-0.110	-0.109
EEFSU	-1280	-1614	412	-1622	-1606	-0.031	-0.039	0.010	-0.039	-0.039
JaKoSing	-565	-669	124	-672	-667	-0.005	-0.006	0.001	-0.006	-0.006
LatinAmerica	-6948	-8883	2627	-8934	-8831	-0.083	-0.107	0.030	-0.107	-0.106
NAmerica	-6924	-8444	2086	-8485	-8404	-0.015	-0.019	0.004	-0.019	-0.018
NEEurope	-147	-356	203	-360	-352	-0.004	-0.011	0.007	-0.011	-0.011
NWEurope	-1329	-2299	436	-2308	-2291	-0.010	-0.015	0.003	-0.015	-0.015
Oceania	-1699	-1995	492	-2005	-1985	-0.060	-0.070	0.016	-0.071	-0.070
SEurope	-416	-557	174	-561	-554	-0.003	-0.005	0.002	-0.005	-0.005
WAsia	-8003	-9187	2445	-9235	-9139	-0.096	-0.110	0.027	-0.111	-0.110
					X 74 X					
				DI	VA_L					
			Н	EV				qGDP		
Region	SIM	Mean	SD	LCI	UCI	SIM	Mean	SD	LCI	UCI
Africa	-5721	-8052	4030	-8131	-7973	-0.111	-0.148	0.067	-0.149	-0.147
CAsia	-3691	-8569	4489	-8657	-8481	-0.086	-0.180	0.088	-0.181	-0.178
China	-3800	-13711	9211	-13891	-13530	-0.049	-0.122	0.068	-0.123	-0.120
EastAsia	-2453	-6596	4198	-6678	-6513	-0.066	-0.113	0.049	-0.114	-0.112
EEFSU	-1892	-3871	1808	-3906	-3835	-0.044	-0.085	0.038	-0.086	-0.084
JaKoSing	-1855	-8830	6957	-8966	-8694	-0.007	-0.019	0.013	-0.020	-0.019
LatinAmerica	-4492	-9356	4931	-9452	-9259	-0.064	-0.111	0.049	-0.112	-0.110
NAmerica	-7825	-14715	6389	-14840	-14590	-0.015	-0.023	0.007	-0.023	-0.023
NEEurope	-363	-1342	958	-1361	-1323	-0.007	-0.022	0.014	-0.022	-0.022
NWEurope	-797	500	1481	471	529	-0.009	-0.006	0.005	-0.006	-0.006
Oceania	-1370	-3617	1974	-3655	-3578	-0.054	-0.106	0.049	-0.107	-0.105
SEurope	-3960	-4977	2039	-5017	-4937	-0.012	-0.010	0.001	-0.010	-0.010
WAsia	-3519	-6087	3045	-6147	-6028	-0.065	-0.084	0.026	-0.084	-0.083
SIM represents the	result of the in	itial model run, q	GDP is the pe	rcentage change	of GDP post simu	lation, LCI and	JCI are the Low	er and Upper 9	5% confidence i	nterval

DIVA_C												
HEV qGDP												
Region	SIM	Mean	SD	LCI	UCI	SIM	Mean	SD	LCI	UCI		
Africa	-3270	-3231	587	-3240	-3221	-0.070	-0.070	0.011	-0.070	-0.069		
CAsia	-4107	-4272	1086	-4290	-4255	-0.094	-0.098	0.021	-0.099	-0.098		
China	-7157	-7026	467	-7033	-7018	-0.072	-0.071	0.004	-0.072	-0.071		
EastAsia	-4977	-5212	1398	-5235	-5190	-0.090	-0.096	0.019	-0.096	-0.095		
EEFSU	-1280	-1365	176	-1368	-1362	-0.031	-0.033	0.006	-0.033	-0.033		
JaKoSing	-565	-586	230	-590	-583	-0.005	-0.005	0.001	-0.005	-0.005		
LatinAmerica	-6948	-7326	2068	-7359	-7293	-0.083	-0.089	0.020	-0.089	-0.088		
NAmerica	-6924	-7182	1598	-7208	-7156	-0.015	-0.016	0.004	-0.016	-0.016		
NEEurope	-147	-166	166	-169	-163	-0.004	-0.005	0.006	-0.005	-0.004		
NWEurope	-1329	-1897	848	-1910	-1883	-0.010	-0.013	0.005	-0.013	-0.013		
Oceania	-1699	-1736	331	-1741	-1731	-0.060	-0.062	0.011	-0.062	-0.062		
SEurope	-416	-445	225	-449	-442	-0.003	-0.004	0.004	-0.004	-0.004		
WAsia	-8003	-8165	2181	-8200	-8131	-0.096	-0.099	0.022	-0.100	-0.099		
				DIV	A_L							
			HEV					qGDP				
Region	SIM	Mean	SD	LCI	UCI	SIM	Mean	SD	LCI	UCI		
Africa	-5721	-6882	4143	-6948	-6816	-0.111	-0.129	0.069	-0.130	-0.128		
CAsia	-3691	-7398	4718	-7474	-7323	-0.086	-0.155	0.088	-0.156	-0.154		
China	-3800	-9205	11065	-9382	-9027	-0.049	-0.087	0.078	-0.089	-0.086		
EastAsia	-2453	-4890	3342	-4944	-4837	-0.066	-0.091	0.034	-0.092	-0.091		
EEFSU	-1892	-2997	948	-3012	-2982	-0.044	-0.067	0.020	-0.068	-0.067		
JaKoSing	-1855	-8280	11273	-8460	-8099	-0.007	-0.018	0.019	-0.018	-0.018		
LatinAmerica	-4492	-6412	2563	-6453	-6371	-0.064	-0.082	0.024	-0.082	-0.081		
NAmerica	-7825	-10058	4569	-10131	-9985	-0.015	-0.018	0.004	-0.018	-0.018		
NEEurope	-363	-447	942	-462	-432	-0.007	-0.007	0.014	-0.007	-0.006		
NWEurope	-797	434	2144	400	469	-0.009	-0.006	0.007	-0.006	-0.006		
Oceania	-1370	-2873	1215	-2892	-2853	-0.054	-0.087	0.028	-0.088	-0.087		
SEurope	-3960	-5166	4020	-5230	-5102	-0.012	-0.012	0.010	-0.012	-0.012		
WAsia SIM represents the	-3519 e result of the in	-4630 itial model run, q	1491 GDP is the perc	-4653 entage change of	-4606 GDP post simu	-0.065 lation, LCI and I	-0.071 JCI are the Low	0.018 er and Upper 9	-0.072 5% confidence i	-0.071 nterval		

Table 3 MC-lpd results and first two moments

БТУА

Table 4 GQ results and first two moments

DIVA_C

			HEV					qGDP		
Region	SIM	Mean	SD	LCB	UCB	SIM	Mean	SD	LCB	UCB
Africa	-3270	-3283	168	-4032	-2533	-0.070	-0.070	0.007	-0.102	-0.039
CAsia	-4107	-4141	348	-5697	-2586	-0.094	-0.094	0.014	-0.156	-0.032
China	-7157	-7183	486	-9356	-5010	-0.072	-0.072	0.005	-0.092	-0.052
EastAsia	-4977	-5044	398	-6822	-3266	-0.090	-0.090	0.019	-0.176	-0.005
EEFSU	-1280	-1283	146	-1937	-630	-0.031	-0.031	0.008	-0.065	0.003
JaKoSing	-565	-569	435	-2513	1375	-0.005	-0.005	0.002	-0.013	0.003
LatinAmerica	-6948	-7042	767	-10470	-3614	-0.083	-0.084	0.018	-0.164	-0.004
NAmerica	-6924	-6951	719	-10166	-3737	-0.015	-0.015	0.005	-0.037	0.007
NEEurope	-147	-149	113	-655	357	-0.004	-0.004	0.012	-0.056	0.047
NWEurope	-1329	-1328	583	-3934	1279	-0.010	-0.010	0.007	-0.040	0.020
Oceania	-1699	-1725	261	-2894	-556	-0.060	-0.061	0.012	-0.114	-0.007
SEurope	-416	-413	193	-1278	452	-0.003	-0.003	0.005	-0.027	0.021
WAsia	-8003	-8058	448	-10062	-6054	-0.096	-0.096	0.018	-0.177	-0.016
				DI	VA_L					
			HEV					qGDP		
Region	SIM	Mean	SD	LCB	UCB	SIM	Mean	SD	LCB	UCB
Africa	-5721	-6057	840	-9812	-2302	-0.111	-0.118	0.020	-0.205	-0.030
CAsia	-3691	-4322	1159	-9505	861	-0.086	-0.097	0.029	-0.225	0.031
China	-3800	-5521	3569	-21482	10439	-0.049	-0.061	0.034	-0.216	0.093
EastAsia	-2453	-3032	1267	-8699	2635	-0.066	-0.071	0.022	-0.168	0.027
EEFSU	-1892	-2029	608	-4747	690	-0.044	-0.047	0.019	-0.130	0.036
JaKoSing	-1855	-3060	2166	-12746	6626	-0.007	-0.009	0.005	-0.030	0.012
LatinAmerica	-4492	-4725	1149	-9863	414	-0.064	-0.065	0.020	-0.154	0.023
NAmerica	-7825	-8575	2859	-21359	4209	-0.015	-0.016	0.006	-0.041	0.009
NEEurope	-363	-609	444	-2593	1376	-0.007	-0.009	0.013	-0.067	0.048
NWEurope	-797	-851	1491	-7519	5817	-0.009	-0.008	0.007	-0.040	0.024
Oceania	-1370	-1592	752	-4954	1770	-0.054	-0.058	0.020	-0.150	0.034
SEurope	-3960	-4231	835	-7966	-495	-0.012	-0.012	0.006	-0.041	0.017
WAsia	-3519	-3831	998	-8292	630	-0.065	-0.066	0.019	-0.153	0.021
SIM represents the result	of the initial mo	odel run, qGDP	is the percenta	ige change of GD	P post simulation	on, LBC and UB	C are the Lower	and Upper 95%	Chebyshev's bo	ound based on:

 $(mean - \sqrt{20} \cdot SD, mean + \sqrt{20} \cdot SD)$

 Table 5
 Ratio between MC-td and the GQ central moments

		DIV	A_C		DIVA_L					
	М	ean	5	SD	М	ean	S	SD		
Region	HEV	qGDP	HEV	qGDP	HEV	qGDP	HEV	qGDP		
Africa	1.1	1.1	4.7	2.2	1.3	1.3	4.8	3.4		
CAsia	1.2	1.2	3.8	2.2	2.0	1.9	3.9	3.1		
China	1.0	1.1	1.6	1.7	2.5	2.0	2.6	2.0		
EastAsia	1.2	1.2	4.1	1.4	2.2	1.6	3.3	2.2		
EEFSU	1.3	1.3	2.8	1.3	1.9	1.8	3.0	2.1		
JaKoSing	1.2	1.3	0.3	0.7	2.9	2.2	3.2	2.7		
LatinAmerica	1.3	1.3	3.4	1.7	2.0	1.7	4.3	2.5		
NAmerica	1.2	1.2	2.9	0.9	1.7	1.4	2.2	1.3		
NEEurope	2.4	2.7	1.8	0.6	2.2	2.3	2.2	1.1		
NWEurope	1.7	1.6	0.7	0.4	-0.6	0.7	1.0	0.7		
Oceania	1.2	1.2	1.9	1.4	2.3	1.8	2.6	2.4		
SEurope	1.3	1.6	0.9	0.3	1.2	0.9	2.4	0.1		
WAsia	1.1	1.1	5.5	1.5	1.6	1.3	3.1	1.4		

	Africa	China	WAsia	CAsia	EastAsia	JaKoSing	LatinAmer	NAmerica	NEEurope	NWEurope	SEurope	Oceania	EEFSU
AfricaC	0.080	0.001	0.001	0.001	0.000	0.007	0.000	0.001	0.001	0.002	0.006	0.001	-0.006
ChinaC	0.001	0.100	0.000	0.000	0.001	0.004	-0.001	0.001	0.000	0.001	0.000	0.001	0.001
WAsiaC	-0.001	0.002	0.112	0.003	0.000	0.024	0.000	0.003	0.002	0.006	0.013	-0.001	-0.007
CAsiaC	0.001	0.001	0.002	0.094	0.002	0.002	0.000	0.001	0.000	0.002	0.001	0.001	0.002
EastAsiaC	0.000	0.008	0.000	0.001	0.089	0.020	0.000	0.003	0.001	0.003	0.004	0.001	-0.001
JaKoSingC	0.001	0.003	0.000	0.000	0.001	0.160	0.000	0.001	0.001	0.001	0.002	0.000	0.001
LatinAmerC	0.000	0.003	-0.001	0.001	-0.001	0.016	0.110	0.004	0.003	0.008	0.012	0.000	-0.002
NAmericaC	0.000	0.006	0.001	0.002	0.000	0.039	0.001	0.227	0.006	0.016	0.020	0.003	0.001
NEEuropeC	0.000	0.000	0.000	0.000	0.000	0.002	0.001	0.001	0.253	0.003	0.003	0.000	0.004
NWEuropeC	0.004	0.003	0.002	0.001	0.001	0.021	0.001	0.007	0.017	0.422	0.038	0.003	0.006
SEuropeC	0.001	0.001	0.000	0.000	-0.001	0.004	0.000	0.001	0.003	0.007	0.480	0.000	0.005
OceaniaC	0.000	0.002	0.000	0.001	0.001	0.010	0.000	0.001	0.001	0.002	0.002	0.168	-0.001
EEFSUC	0.000	0.000	0.000	0.000	0.000	0.001	0.000	0.001	0.002	0.001	0.002	0.000	0.397
AfricaW	0.985	0.003	0.010	0.010	0.002	-0.114	0.004	-0.001	-0.011	-0.028	0.052	-0.001	0.021
ChinaW	0.020	0.899	0.008	0.009	0.008	0.044	0.021	0.018	-0.017	-0.033	-0.040	0.042	0.054
WAsiaW	0.045	0.044	0.987	0.047	0.010	-0.080	0.011	-0.017	-0.027	-0.144	0.077	-0.019	0.220
CAsiaW	0.048	0.006	0.028	0.991	0.032	-0.192	0.028	0.006	-0.034	-0.100	-0.065	0.182	0.108
EastAsiaW	0.016	0.024	0.012	0.073	0.990	0.231	-0.002	-0.010	-0.059	-0.148	-0.159	0.083	0.027
JaKoSingW	0.001	0.000	0.003	0.000	0.009	0.857	0.012	0.002	-0.008	-0.023	-0.027	0.047	0.014
LatinAmerW	0.038	-0.001	0.003	-0.009	0.002	-0.291	0.986	0.143	-0.064	-0.184	-0.138	0.010	0.079
NAmericaW	0.065	0.423	0.021	0.003	0.022	-0.111	0.048	0.959	-0.013	-0.132	-0.092	0.034	0.195
NEEuropeW	0.003	0.010	0.002	0.001	0.002	-0.012	0.007	-0.003	0.961	-0.015	-0.012	0.010	-0.002
NWEuropeW	0.097	0.089	0.032	0.008	0.013	-0.125	0.032	-0.018	0.013	0.835	-0.184	0.054	0.392
SEuropeW	0.016	0.003	0.007	-0.001	0.004	-0.052	0.007	0.001	-0.014	-0.042	0.808	0.007	0.128
OceaniaW	0.001	0.010	0.002	0.004	0.011	0.077	-0.001	0.002	-0.010	-0.030	-0.025	0.956	-0.005
EEFSUW	0.000	-0.007	0.000	0.000	-0.001	0.001	0.001	0.001	0.000	0.001	0.016	-0.001	0.749
Standardized regression coefficients by region. C is the regional variable for Capital and W is the regional variable for productivity losses.													

Table 6 Uncertainty decomposition heat-map of HEV in MC-lpd for DIVA_C

 Table 7 Uncertainty decomposition heat-map of qGDP in MC-lpd for DIVA_C

	Africa	China	WAsia	CAsia	EastAsia	JaKoSing	LatinAmer	NAmerica	NEEurope	NWEurope	SEurope	Oceania	EEFSU
AfricaC	0.500	0.000	0.001	0.001	0.000	0.003	0.000	0.000	0.000	0.000	0.000	0.001	-0.006
ChinaC	0.001	0.433	0.000	0.000	0.001	0.002	0.000	0.000	0.000	0.000	0.000	0.001	0.001
WAsiaC	0.000	0.001	0.719	0.003	0.000	0.008	0.000	0.000	0.001	0.001	0.001	-0.001	-0.009
CAsiaC	0.000	-0.001	0.001	0.367	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.001
EastAsiaC	0.000	0.003	0.000	0.000	0.717	0.005	0.000	0.001	0.001	0.001	0.001	0.000	-0.001
JaKoSingC	0.001	0.003	0.000	0.000	0.001	0.948	0.001	0.001	0.001	0.000	0.001	0.001	0.001
LatinAmerC	0.002	0.002	0.000	0.001	-0.001	0.009	0.578	0.000	0.002	0.003	0.003	0.001	-0.001
NAmericaC	0.002	-0.001	0.001	0.001	0.000	0.026	0.002	0.964	0.003	0.004	0.002	0.002	-0.004
NEEuropeC	0.000	0.000	0.000	0.000	0.000	0.002	0.001	0.000	0.920	0.000	0.000	0.000	0.003
NWEuropeC	0.003	0.006	0.001	0.002	0.001	0.021	0.001	0.002	0.004	0.953	0.005	0.003	0.000
SEuropeC	0.001	0.001	0.000	0.000	0.000	0.003	0.000	0.000	0.001	0.001	0.961	0.000	0.003
OceaniaC	0.000	0.001	0.000	0.001	0.000	0.003	0.000	0.000	0.000	0.001	0.000	0.799	-0.001
EEFSUC	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.866
AfricaW	0.862	0.003	0.004	0.010	-0.001	-0.048	0.000	-0.004	-0.018	-0.032	-0.027	0.000	-0.001
ChinaW	0.017	0.733	0.004	0.008	0.005	0.031	0.019	0.012	-0.011	-0.021	-0.022	0.030	0.042
WAsiaW	0.006	0.061	0.681	0.047	0.006	-0.038	0.003	-0.009	-0.057	-0.129	-0.107	-0.018	-0.001
CAsiaW	0.033	-0.021	0.010	0.924	0.013	-0.050	0.022	0.007	-0.030	-0.057	-0.044	0.122	0.056
EastAsiaW	0.006	0.006	0.002	0.065	0.684	0.086	-0.006	-0.004	-0.051	-0.087	-0.098	0.053	0.027
JaKoSingW	-0.002	-0.002	0.001	-0.001	0.006	0.259	0.011	0.001	-0.007	-0.013	-0.014	0.034	0.013
LatinAmerW	0.015	0.040	-0.004	-0.002	0.001	-0.135	0.810	0.031	-0.056	-0.106	-0.106	0.011	0.032
NAmericaW	0.014	0.515	-0.007	-0.004	0.008	-0.033	0.033	0.251	-0.057	-0.120	-0.124	0.006	0.108
NEEuropeW	0.001	0.007	0.000	0.000	0.001	-0.007	0.006	-0.001	0.373	-0.013	-0.013	0.006	-0.010
NWEuropeW	0.056	0.106	0.008	0.003	0.006	-0.023	0.024	-0.002	-0.028	0.174	-0.075	0.032	0.196
SEuropeW	0.012	0.006	0.002	-0.001	0.002	-0.013	0.007	0.001	-0.011	-0.020	0.105	0.004	0.086
OceaniaW	-0.002	0.003	-0.001	0.004	0.006	0.025	-0.002	0.000	-0.012	-0.020	-0.022	0.576	-0.007
EEFSUW	0.001	0.000	0.000	0.000	-0.001	0.001	0.000	0.000	0.005	-0.005	-0.006	0.000	0.433
		Standardized	l regression	coefficients	by region. C i	s the regional v	ariable for Capi	tal and W is the	regional variabl	e for productivity	y losses.		



Fig. 2 Productivity Shocks Histogram based on the triangular distribution sampling



Fig. 3 Productivity Shocks, GQ Histogram\MC kernel density estimates in DIVA_C for the td and lpd sampling methods





Fig. 5 DIVA-C HEV mean convergence for the MC-td of the Total and the Split Simulations. Split simulations are indicated by the extension _S

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Fig. 6 DIVA-C qGDP mean convergence for the MC-td of the Total and the Split Simulations. Split simulations are indicated by the extension _S



Fig. 7 Uncertainty decomposition coefficients of HEV and qGDP in DIVA_C by region for the MC-lpd. The extension C to a regional variable stands for for Capital, L for Land losses and W for productivity losses. Results are multiplied by 100.

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A Appendix

A.1 qGDP

As in Chatzivasileiadis et al. (2016), approaching GDP from the expenditure side, GDP can be expressed by the following accounting identity:

$$GDP \equiv C + I + E - M \tag{6}$$

Where C denotes final consumption of goods and services, I is (gross) investment, E is exports of goods and services, and M is imports of goods and services. In GTAP, exports E is divided into exports of goods and services to all other countries (E) and exports of transportation services to the "global" transportation sector (T). The "global" transportation sector as designed in the GTAP model purchases transport services from all regions and in return it supplies transport services to every region. The accounting identity then becomes:

$$GDP \equiv C + I + E + T - M \tag{7}$$

Total differentiation of this identity shows how relative changes in GDP can be decomposed into relative changes in its factors, where percentage changes are denoted by q: "qGDP = (dGDP/GDP)*100" :

$$qGDP = \left(c * \frac{C}{GDP} + i * \frac{I}{GDP} + e * \frac{E}{GDP} + t * \frac{T}{GDP} - m * \frac{M}{GDP}\right) * 100$$
(8)

Table A.1 Regional and sector aggregation

	Regional A	Aggregation			Sectoral Aggregation
1	OCE	Australia, New Zealand	1	AGR	All Agriculture
2	EAS	East Asia	2	AIR	Air Transport
3	WAS	West Asia	3	ENY	Energy and energy production
4	NAM	North America	4	NTIND	Non Transportation Intensive industries
5	LAM	Latin America	5	SERV	Other Services
6	NEW	North West Europe	6	TIND	Transportation Intensive industries
7	NEE	North East Europe	7	OTR	Transport Not Elsewhere Classified
8	SEU	South Europe	8	SEA	Water Transport
9	CAS	Central Asia			
10	AFR	Africa			
11	EEF	Ex-Soviet countries			
12	JAK, JaKoSing	Japan, Korea, Singapore			
13	CHN	China, Hong Kong			

 Table A.2 Uncertainty decomposition of HEV in MC-lpd for DIVA_C

	Africa	China	WAsia	CAsia	EastAsia	JaKoSing	LatinAmer	NAmerica	NEEurope	NWEurope	SEurope	Oceania	EEFSU
AfricaC	0.080***	0.001***	0.001	0.001	0.000	0.007***	-0.000	0.001***	0.001***	0.002***	0.006***	0.001	-0.006***
ChinaC	0.001^{*}	0.100***	0.000	0.000	0.001	0.004***	-0.001	0.001*	-0.000	0.001*	0.000^{*}	0.001*	0.001***
WAsiaC	-0.001*	0.002***	0.112***	0.003***	0.000	0.024***	-0.000	0.003***	0.002***	0.006***	0.013***	-0.001	-0.007***
CAsiaC	0.001	0.001***	0.002^{*}	0.094***	0.002**	0.002***	-0.000	0.001*	0.000	0.002***	0.001***	0.001	0.002***
EastAsiaC	0.000	0.008^{***}	0.000	0.001	0.089***	0.020***	0.000	0.003***	0.001***	0.003***	0.004***	0.001	-0.001***
JaKoSingC	0.001**	0.003***	-0.000	0.000	0.001	0.160***	0.000	0.001***	0.001**	0.001**	0.002***	0.000	0.001***
LatinAmerC	0.000	0.003***	-0.001	0.001^{*}	-0.001	0.016***	0.110***	0.004***	0.003***	0.008***	0.012***	0.000	-0.002***
NAmericaC	0.000	0.006***	0.001	0.002***	0.000	0.039***	0.001	0.227***	0.006***	0.016***	0.020***	0.003***	0.001***
NEEuropeC	0.000	0.000^{*}	-0.000	0.000	-0.000	0.002***	0.001	0.001**	0.253***	0.003***	0.003***	0.000	0.004***
NWEuropeC	0.004***	0.003***	0.002**	0.001***	0.001	0.021***	0.001	0.007***	0.017***	0.422***	0.038***	0.003***	0.006***
SEuropeC	0.001***	0.001***	0.000	0.000	-0.001	0.004***	-0.000	0.001***	0.003***	0.007***	0.480***	0.000	0.005***
OceaniaC	-0.000	0.002***	-0.000	0.001**	0.001	0.010***	0.000	0.001**	0.001*	0.002***	0.002***	0.168***	-0.001***
EEFSUC	0.000	0.000**	-0.000	0.000	0.000	0.001	0.000	0.001*	0.002***	0.001***	0.002***	0.000	0.397***
AfricaL	-0.000	0.000	0.000	0.000	0.001	0.001	-0.001	-0.000	0.000	-0.000	0.000	-0.000	0.000
ChinaL	0.001*	0.000	0.000	0.000	-0.000	-0.000	0.000	-0.000	0.000	-0.000	0.000	-0.000	-0.000
WAsiaL	0.000	-0.000	-0.000	-0.001	-0.000	0.000	-0.001	-0.001*	0.000	0.000	0.000	0.000	-0.000
CAsiaL	0.000	0.000	-0.001	0.003***	-0.000	-0.000	0.001	0.000	-0.000	0.000	-0.000	-0.000	-0.000
EastAsiaL	-0.000	0.000**	-0.000	-0.000	0.002**	0.001*	-0.000	-0.000	0.000	-0.000	0.000	-0.000	0.000
JaKoSingL	0.000	-0.000	-0.000	0.000	-0.000	0.008***	0.000	-0.000	-0.000	0.000	-0.000	-0.000	0.000
LatinAmerL	-0.000	-0.000	0.000	-0.000	0.001	0.001*	-0.002*	-0.001*	-0.000	0.000	0.000	-0.000	-0.000
NAmericaL	0.000	-0.000	0.001	0.000	-0.001	-0.000	-0.000	0.000	-0.000	-0.000	0.000	-0.001	0.000
NEEuropeL	-0.000	-0.000	-0.000	-0.000	0.000	0.000	-0.000	0.000	0.000	-0.000	-0.000	-0.000	-0.000
NWEuropeL	-0.000	-0.000	-0.000	-0.000	-0.001	-0.000	0.000	-0.000	0.000	0.000	0.000	-0.001	-0.000
SEuropeL	0.000	-0.000	0.001	-0.000	-0.000	-0.000	0.000	-0.000	0.000	0.000	0.003***	-0.000	0.000
OceaniaL	0.000	-0.000	0.001	-0.001	-0.000	0.000	0.000	-0.000	0.000	-0.000	0.000	0.000	-0.000
EEFSUL	-0.000	0.000	-0.000	-0.000	0.001	0.001	-0.001	-0.000	0.000	-0.000	-0.000	-0.000	0.002***
AfricaW	0.985***	0.003***	0.010***	0.010***	0.002*	-0.114***	0.004***	-0.001***	-0.011***	-0.028***	0.052***	-0.001*	0.021***
ChinaW	0.020***	0.899***	0.008***	0.009***	0.008***	0.044***	0.021***	0.018***	-0.017***	-0.033***	-0.040***	0.042***	0.054***
WAsiaW	0.045***	0.044***	0.987***	0.047***	0.010***	-0.080***	0.011***	-0.017***	-0.027***	-0.144***	0.077***	-0.019***	0.220***
CAsiaW	0.048***	0.006***	0.028***	0.991***	0.032***	-0.192***	0.028***	0.006***	-0.034***	-0.100***	-0.065***	0.182***	0.108***
EastAsiaW	0.016***	0.024***	0.012***	0.073***	0.990***	0.231***	-0.002**	-0.010***	-0.059***	-0.148***	-0.159***	0.083***	0.027***
JaKoSingW	0.001**	0.000*	0.003***	0.000	0.009***	0.857***	0.012***	0.002***	-0.008***	-0.023***	-0.027***	0.047***	0.014***
LatinAmerW	0.038***	-0.001***	0.003***	-0.009***	0.002*	-0.291***	0.986***	0.143***	-0.064***	-0.184***	-0.138***	0.010***	0.079***
NAmericaW	0.065***	0.423***	0.021***	0.003***	0.022***	-0.111***	0.048***	0.959***	-0.013***	-0.132***	-0.092***	0.034***	0.195***
NEEuropeW	0.003***	0.010***	0.002*	0.001	0.002**	-0.012***	0.007***	-0.003***	0.961***	-0.015***	-0.012***	0.010***	-0.002***
NWEuropeW	0.097***	0.089***	0.032***	0.008***	0.013***	-0.125***	0.032***	-0.018***	0.013***	0.835***	-0.184***	0.054***	0.392***
SEuropeW	0.016***	0.003***	0.007***	-0.001	0.004***	-0.052***	0.007***	0.001*	-0.014***	-0.042***	0.808***	0.007***	0.128***
OceaniaW	0.001***	0.010***	0.002**	0.004***	0.011***	0.077***	-0.001	0.002***	-0.010***	-0.030***	-0.025***	0.956***	-0.005***
EEESUW	0.000	-0.007***	0.000	-0.000	-0.001	0.001***	0.001	0.001***	-0.000	0.001**	0.016***	-0.001	0 749***
$\frac{R^2}{R^2}$	0.999	1.000	0.994	0.998	0.991	0.999	0.990	0.999	0.999	0.998	0.999	0.994	0.999

Standardized beta coefficients, * p < 0.05, ** p < 0.01, *** p < 0.001

The extension C to a regional variable stands for for Capital, L for Land losses and W for productivity losses.

The extension C to a regional variable stands for for Capital, L for Land losses and W for productivity losses.

Standardized beta	coefficients, *	p < 0.05, *	* $p < 0.01$	$,^{***} p < 0.001$

$ \begin{array}{c} eq:approx_appro$		Africa	China	WAsia	CAsia	EastAsia	JaKoSing	LatinAmer	NAmerica	NEEurope	NWEurope	SEurope	Oceania	EEFSU
ChinaC 0.001 ⁺⁺ 0.433 ⁺⁺⁺ 0.000 0.000 ⁺⁺⁺ 0.000 ⁺⁺⁺ 0.001 ⁺⁺⁺⁺⁺ 0.001 ⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺⁺	AfricaC	0.500***	0.000*	0.001	0.001	0.000	0.003***	-0.000	-0.000***	0.000*	0.000**	-0.000*	0.001	-0.006***
WASAC 0.000 0.001 ⁺⁺⁺ 0.000 ⁺⁺⁺⁺ 0.000 ⁺⁺⁺⁺ 0.000 ⁺⁺⁺⁺ <td>ChinaC</td> <td>0.001**</td> <td>0.433***</td> <td>0.000</td> <td>0.000</td> <td>0.001</td> <td>0.002***</td> <td>-0.000</td> <td>0.000***</td> <td>0.000</td> <td>0.000</td> <td>0.000</td> <td>0.001*</td> <td>0.001***</td>	ChinaC	0.001**	0.433***	0.000	0.000	0.001	0.002***	-0.000	0.000***	0.000	0.000	0.000	0.001*	0.001***
CASAC 0.000 -0.001** 0.001 0.307*** 0.001** 0.000 0.000 0.000** 0.000 0.000*** 0.000 0.001*** 0.000**** 0.000**** 0.000**** 0.000****	WAsiaC	0.000	0.001***	0.719***	0.003***	0.000	0.008***	0.000	-0.000***	0.001***	0.001***	0.001***	-0.001*	-0.009***
	CAsiaC	0.000	-0.001***	0.001	0.367***	0.001*	0.000	-0.000	0.000***	0.000	0.000	0.000	0.000	0.001***
JakosingC 0.001*** 0.000 0.001 0.001*** <th0< td=""><td>EastAsiaC</td><td>0.000</td><td>0.003***</td><td>0.000</td><td>-0.000</td><td>0.717***</td><td>0.005***</td><td>0.000</td><td>0.001***</td><td>0.001***</td><td>0.001***</td><td>0.001***</td><td>-0.000</td><td>-0.001***</td></th0<>	EastAsiaC	0.000	0.003***	0.000	-0.000	0.717***	0.005***	0.000	0.001***	0.001***	0.001***	0.001***	-0.000	-0.001***
	JaKoSingC	0.001***	0.003***	0.000	0.000	0.001*	0.948***	0.001	0.001***	0.001***	0.000***	0.001***	0.001	0.001***
NAmericaC 0.002*** 0.001*** 0.000 0.002*** 0.002*** 0.002*** 0.002*** 0.002*** 0.002*** 0.002*** 0.002*** 0.002*** 0.002*** 0.002*** 0.002*** 0.002*** 0.002*** 0.001*** 0.000*** 0.000*** 0.001*** 0.001*** 0.001*** 0.001** 0.001*** 0.001*** 0.001*** 0.001*** 0.001*** 0.001*** 0.001*** 0.000 0.001*** 0.001*** 0.000 0.000*** 0.001*** 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000<	LatinAmerC	0.002***	0.002***	-0.000	0.001^{*}	-0.001	0.009***	0.578***	0.000**	0.002***	0.003***	0.003***	0.001^{*}	-0.001***
NEEuropeC 0.000 -0.000 0.002 ⁺⁺⁺ 0.000 ⁺⁺⁺⁺ 0.000 ⁺⁺⁺⁺ 0.000 ⁺⁺⁺⁺⁺ <td>NAmericaC</td> <td>0.002***</td> <td>-0.001***</td> <td>0.001</td> <td>0.001**</td> <td>0.000</td> <td>0.026***</td> <td>0.002**</td> <td>0.964***</td> <td>0.003***</td> <td>0.004***</td> <td>0.002***</td> <td>0.002***</td> <td>-0.004***</td>	NAmericaC	0.002***	-0.001***	0.001	0.001**	0.000	0.026***	0.002**	0.964***	0.003***	0.004***	0.002***	0.002***	-0.004***
NWEuropeC 0.003*** 0.001*** 0.001** 0.001*** 0.001*** 0.003*** 0.000*** 0.001*** 0.001*** 0.000*** 0.000*** 0.001*** 0.001*** 0.000*** 0.000*** 0.001*** 0.001*** 0.000*** 0.000*** 0.000*** 0.001*** 0.000 0.000*** 0.000 0.000*** 0.000 0.000*** 0.000 0.000*** 0.000 0.000 0.000 0.000*** 0.000 0.000*** 0.000 0.000*** 0.000 0.000**** 0.000 0.000**** 0.000 0.000*** 0.000 0.000**** 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0	NEEuropeC	0.000	0.000	-0.000	0.000	-0.000	0.002***	0.001	0.000**	0.920***	0.000**	0.000**	0.000	0.003***
$ \begin{array}{ccccc} Second Seco$	NWEuropeC	0.003***	0.006***	0.001**	0.002***	0.001*	0.021***	0.001*	0.002***	0.004***	0.953***	0.005***	0.003***	0.000***
$ \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} 0.000 & 0.001^{***} & -0.000 & 0.001^{***} & 0.000 & 0.000 & 0.000 & 0.000^{***} & 0.001^{****} & -0.001^{****} & -0.001^{****} & -0.001^{****} & -0.001^{****} & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.0$	SEuropeC	0.001**	0.001***	0.000	0.000	-0.000	0.003***	-0.000	0.000***	0.001***	0.001***	0.961***	0.000	0.003***
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	OceaniaC	-0.000	0.001***	-0.000	0.001**	0.000	0.003***	0.000	0.000	0.000**	0.001***	0.000^{*}	0.799***	-0.001***
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	EEFSUC	0.000	0.000**	-0.000	0.000	0.000	0.000^{*}	0.000	0.000	0.000^{*}	0.000	0.000	-0.000	0.866***
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	AfricaL	0.001*	0.000	0.000	0.000	0.001	0.000	-0.001	-0.000	0.000	-0.000	0.000	-0.000	0.000
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	ChinaL	0.001*	0.001***	0.000	0.000	-0.000	-0.000	0.000	-0.000	0.000	-0.000	0.000	-0.000	-0.000
$ \begin{array}{ccccc} CAsiaL & 0.000 & 0.000^* & -0.001 & 0.007^{***} & -0.000 & 0.000^* & 0.000 & 0.000 & 0.000 & 0.000 & 0.000 & 0.000 & 0.000 \\ EastAsiaL & 0.000 & 0.001^{***} & -0.000 & 0.000 & 0.011^{***} & 0.000 & 0.000 & 0.000 & 0.000 & 0.000 & 0.000 & 0.000 \\ JatoSingL & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & 0.000 & 0.000 & -0.000 \\ LatinAmerL & 0.000 & -0.000 & 0.000 & -0.000 & 0.000^* & -0.001 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 \\ NAmericaL & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & -0.000 \\ NEEuropeL & -0.000 & -0.000 & -0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 \\ NWEuropeL & -0.000 & -0.000 & -0.000 & -0.000 & -0.000 & 0.000 & -0.000 & 0.000^* & 0.000 & -0.000 & -0.000 \\ SuropeL & 0.000 & -0.000 & -0.000 & -0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 \\ CccaniaL & 0.000 & -0.000 & -0.000 & -0.000 & -0.000 & -0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.000 & -0.000 & 0.$	WAsiaL	0.000	-0.000	-0.000	-0.001	-0.000	0.000	-0.000	-0.000*	0.000	0.000	0.000	0.000	-0.000
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	CAsiaL	0.000	0.000^{*}	-0.001	0.007***	-0.000	0.000**	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	EastAsiaL	0.000	0.001***	-0.000	0.000	0.011***	0.000***	-0.000	0.000	0.000	0.000	0.000	0.000	0.000
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	JaKoSingL	0.000	0.000^{*}	-0.000	0.000	-0.000	0.021***	0.000	0.000	-0.000	0.000	0.000	0.000	0.000
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	LatinAmerL	0.000	-0.000	0.000	-0.000	0.000	0.000^{*}	-0.001	-0.000	0.000	0.000	0.000	-0.000	-0.000
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	NAmericaL	0.000	0.000	0.001	0.000	-0.000	0.000	-0.000	0.001***	-0.000	-0.000	0.000	-0.000	-0.000
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	NEEuropeL	-0.000	-0.000	-0.000	-0.000	0.000	0.000	-0.000	0.000	0.001***	-0.000	0.000	-0.000	-0.000
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	NWEuropeL	-0.000	-0.000	-0.000	-0.000	-0.001	-0.000	0.000	-0.000	0.000	0.000**	0.000	-0.001	-0.000
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	SEuropeL	0.000	0.000	0.000	-0.000	-0.000	-0.000	0.000	-0.000	0.000	0.000	0.003***	-0.000	0.000
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	OceaniaL	0.000	-0.000	0.000	-0.001	-0.000	0.000	0.000	-0.000	0.000	-0.000	0.000	0.000	-0.000
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	EEFSUL	-0.000	0.000	-0.000	-0.000	0.001	0.000	-0.000	0.000	0.000	0.000	0.000	-0.000	0.003***
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	AfricaW	0.862***	0.003***	0.004***	0.010***	-0.001	-0.048***	0.000	-0.004***	-0.018***	-0.032***	-0.027***	-0.000	-0.001***
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	ChinaW	0.017***	0.733***	0.004***	0.008***	0.005***	0.031***	0.019***	0.012***	-0.011***	-0.021***	-0.022***	0.030***	0.042***
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	WAsiaW	0.006***	0.061***	0.681***	0.047***	0.006***	-0.038***	0.003***	-0.009***	-0.057***	-0.129***	-0.107***	-0.018***	-0.001***
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	CAsiaW	0.033***	-0.021***	0.010***	0.924***	0.013***	-0.050***	0.022***	0.007***	-0.030***	-0.057***	-0.044***	0.122***	0.056***
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	EastAsiaW	0.006***	0.006***	0.002***	0.065***	0.684***	0.086***	-0.006***	-0.004***	-0.051***	-0.087***	-0.098***	0.053***	0.027***
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	JaKoSingW	-0.002***	-0.002***	0.001^{*}	-0.001	0.006***	0.259***	0.011***	0.001***	-0.007***	-0.013***	-0.014***	0.034***	0.013***
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	LatinAmerW	0.015***	0.040***	-0.004***	-0.002***	0.001**	-0.135***	0.810***	0.031***	-0.056***	-0.106***	-0.106***	0.011***	0.032***
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	NAmericaW	0.014***	0.515***	-0.007***	-0.004***	0.008***	-0.033***	0.033***	0.251***	-0.057***	-0.120***	-0.124***	0.006***	0.108***
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	NEEuropeW	0.001*	0.007***	0.000	-0.000	0.001^{*}	-0.007***	0.006***	-0.001***	0.373***	-0.013***	-0.013***	0.006***	-0.010***
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	NWEuropeW	0.056***	0.106***	0.008***	0.003***	0.006***	-0.023***	0.024***	-0.002***	-0.028***	0.174***	-0.075***	0.032***	0.196***
	SEuropeW	0.012***	0.006***	0.002***	-0.001	0.002***	-0.013***	0.007***	0.001***	-0.011***	-0.020***	0.105***	0.004***	0.086***
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	OceaniaW	-0.002***	0.003***	-0.001	0.004***	0.006***	0.025***	-0.002*	-0.000	-0.012***	-0.020***	-0.022***	0.576***	-0.007***
R^2 0.999 1.000 0.997 0.998 0.996 1.000 0.993 1.000 1.000 1.000 1.000 0.998 1.000	EEFSUW	0.001***	0.000	0.000	0.000	-0.001	0.001***	0.000	0.000***	0.005***	-0.005***	-0.006***	-0.000	0.433***
	R^2	0.999	1.000	0.997	0.998	0.996	1.000	0.993	1.000	1.000	1.000	1.000	0.998	1.000

 Table A.3 Uncertainty decomposition of qGDP in MC-lpd for DIVA_C