Abstract
Changes in conscious level have been associated with changes in dynamical integration and segregation among distributed brain regions. Recent theoretical developments emphasize changes in directed functional (i.e., causal) connectivity as reflected in quantities such as ‘integrated information’ and ‘causal density’. Here we develop and illustrate a rigorous methodology for assessing causal connectivity from electroencephalographic (EEG) signals using Granger causality (GC). Our method addresses the challenges of non-stationarity and bias by dividing data into short segments and applying permutation analysis. We apply the method to EEG data obtained from subjects undergoing propofol-induced anaesthesia, with signals source-localized to the anterior and posterior cingulate cortices. We found significant increases in bidirectional GC in most subjects during loss-of-consciousness, especially in the beta and gamma frequency ranges. Corroborating a previous analysis we also found increases in synchrony in these ranges; importantly, the Granger causality analysis showed higher inter-subject consistency than the synchrony analysis. Finally, we validate our method using simulated data generated from a model for which GC values can be analytically derived. In summary, our findings advance the methodology of Granger causality analysis of EEG data and carry implications for integrated information and causal density theories of consciousness.
which takes into account potential non-stationarity by applying GC to short data segments that are approximately stationary, and allowing GC to vary across segments. This approach enables us to move beyond the detection of significant causal connections between time series, allowing analysis of the distribution of GC values across segments, and, moreover, inference on differences in distributions of GC values between different steady states. Our method also incorporates a permutation analysis to eliminate statistical bias. We further distinguish our approach by validation against a simulation model for which GC values can be analytically derived.

We illustrate our method by application to high-density, steady-state, source-localized EEG data acquired from subjects during wakeful resting (WR) and when undergoing propofol-induced general anaesthesia (loss-of-consciousness, LOC). Extending a previous analysis, we focused on time series localized to the anterior and posterior cingulate cortices (ACC and PCC respectively), see Figure 1; (ACC coverage extends to the mesiobfrontal cortex and PCC to the precuneus). These areas form part of an anatomically-defined ‘mesial highway’ implicated in slow-wave propagation during both anaesthesia and sleep [10,11]. In the previous analysis, both ACC and PCC showed large increases in gamma (25–40 Hz) power during LOC [11]. Significantly, functional connectivity in the gamma range between these regions also increased during LOC, as measured by phase synchrony. Here, we extend this analysis by examining changes in power and phase synchrony across multiple frequency bands (delta 0.5–4 Hz, theta 4–8 Hz, alpha 8–12 Hz, beta 12–25 Hz, and gamma 25–40 Hz) on a subject-by-subject basis. Our main extension remains however to examine bidirectional GC changes for each subject using a rigorous and well-validated analysis pipeline.

**Methods**

**Ethics statement**

The data analysed in this study were obtained from a previous study [11] with procedures approved by the Ethics Committee of the Faculty of Medicine of the University of Liège.

**EEG data acquisition and preprocessing**

We re-analyzed a subset of the data comprising 5 min of spontaneous high-density EEG recordings sampled at 1000 Hz from each of 7 subjects during both WR and LOC, with LOC defined as clinical unconsciousness (no response to command, Ramsay scale score 5) [12]. LOC was induced via administration of propofol, an intravenous anaesthetic that is widely used in surgical settings which reversibly induces a state of diminished responsiveness behaviourally similar to non-rapid eye movement sleep [13]. Average arterial blood concentrations of propofol were 3.87±1.39 mcg/ml for LOC [11]. Sensor-space EEG data were source modelled using GeoSource (see [11]) and time-courses corresponding to the ACC and PCC regions were extracted. Each region furnished 9 time series, which we averaged to obtain a single time series pair for each subject, in each of the WR and LOC states. From each pair we selected 1–3 non-overlapping artifact-free epochs of variable length. For ease of analysis, for a given subject, the total length of data analyzed in each condition was the same. Across different subjects, the data retained ranged between 140 sec and 200 sec. We paid particular attention to preprocessing steps given the sensitivity of GC to standard manipulations [8,7]. For the GC analysis we applied the following additional preprocessing steps. Following [9], for each epoch we applied two-way least-squares finite impulse response (FIR) notch filters (49–51 Hz and 99–101 Hz) to remove the 50 Hz mains-electricity line-noise as well as its harmonic at 100 Hz (if left in, these artifacts lead to nonstationarity). Then we downsampled the data to 250 Hz in order to ensure a reasonable model order for autoregressive modelling (see the section ‘Granger causality’ and [14,8]). Note that higher harmonics of the line noise were rendered higher than the Nyquist frequency following downsampling. No other filtering was carried out; other artifacts were dealt with by choosing artifact-free epochs by inspection.

**Granger causality**

In this section we rehearse the formalism of Granger causality in the time and frequency domains. Given two wide-sense stationary time series \(X\) and \(Y\) (i.e., time series whose observations have constant means and variances), GC, \(F_{Y \rightarrow X}\), is a measure of the extent to which the past of \(Y\) assists in predicting the future of \(X\) over and above the extent to which the past of \(X\) already predicts the future of \(X\) [5]. Standardly, the measure is implemented in terms of linear regressions. Specifically we compare the (unrestricted, Eq. (1), and restricted, Eq. (2)) models

\[
\begin{align*}
X(t) &= \sum_{k=1}^{p} A_k X(t-k) + E(t) \\
Y(t) &= \sum_{k=1}^{p} B_k X(t-k) + E(t) \tag{1}
\end{align*}
\]

\[
X(t) = \sum_{k=1}^{p} B_k X(t-k) + E(t), \tag{2}
\]

where \(A_k\) and \(B_k\) are respectively \(2 \times 2\) and \(1 \times 1\) matrices of model coefficients, \(p\) is the model order, \(E_x, E_y\) and \(\bar{E}\) are the residuals, \(t_0\) denotes the time between successive observations, and we have assumed for simplicity that \(X\) and \(Y\) are both zero mean. In practice, \(A_x, B_x, A_y, B_y, E_x, E_y\) and \(\bar{E}\) can be derived by standard linear autoregression methods, including ordinary least squares and multivariate Yule-Walker equations [13]. GC is then given by the log-ratio of the variance of the residual in the restricted regression to that in the unrestricted regression:
\[ F_{Y \rightarrow X} = \ln \left( \frac{\text{var}(E_Y)}{\text{var}(E_X)} \right) \].

(3)

Importantly, GC has a spectral decomposition that can be used to restrict inferences about causal influence to particular frequency bands [16,17,6]. Spectral GC can be thought of as measuring the proportion of power of \( X \) at the given frequency that derives from its interaction with \( Y \). Spectral GC is written in terms of the inverse \( H \) of the transfer matrix \( A \), which is defined via the frequency domain representation for the unrestricted regression:

\[
A(\omega) \begin{bmatrix} \tilde{X}(\omega) \\ \tilde{Y}(\omega) \end{bmatrix} = \begin{bmatrix} \tilde{E}_x(\omega) \\ \tilde{E}_y(\omega) \end{bmatrix},
\]

(4)

where we use tildes to denote Fourier transform. Explicitly in terms of unrestricted regression coefficients we have

\[
A(\omega) = I - \sum_{k=1}^{p} z^{-k} A_k,
\]

(5)

where \( z = e^{-i\tau} = e^{-i2\pi \alpha} \), and \( \tau = 2\pi \) is the circle constant [18]; (see http://tauday.com for several reasons why we adopt \( \tau \) rather than \( \pi \) as the circle constant). Let us also introduce the covariance matrix of residuals of the unrestricted regression (1) as

\[
\Sigma \equiv \begin{pmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{yx} & \sigma_{yy} \end{pmatrix} = \text{COV} \left[ \begin{bmatrix} E_x(t) \\ E_y(t) \end{bmatrix} \right].
\]

(6)

Then the spectral GC at a given frequency \( \omega \) is given by

\[
F_{Y \rightarrow X}(\omega) = \ln \left( \frac{S_{xx}(\omega)}{S_{xx}(\omega) - H_{xx}(\omega)\sigma_{xx}^{-1}H_{xx}^*(\omega)} \right),
\]

(7)

where \( * \) denotes complex conjugation. The transformation \( Y \rightarrow Y - (\sigma_{yx}/\sigma_{xx})X \) leaves GC invariant, but diagonalizes the covariance matrix \( \Sigma \) of residuals and simplifies the expression for spectral GC to

\[
F_{Y \rightarrow X}(\omega) = \ln \left( \frac{S_{xx}(\omega)}{H_{xx}(\omega)\sigma_{xx}H_{xx}^*(\omega)} \right),
\]

(8)

where now we have from Eq. (4) and \( S_{xx} = |\tilde{X}|^2 \) that

\[
S_{xx}(\omega) = H_{xx}(\omega)\sigma_{xx}^{-1}H_{xx}^*(\omega) + H_{yy}(\omega)\sigma_{yy}^{-1}H_{yy}^*(\omega).
\]

(9)

Written this way, we see explicitly how spectral GC is measuring the contribution of causal power relative to intrinsic power.

To obtain the ‘band-limited’ GC for a frequency band defined by the range \([\omega_1,\omega_2]\), which we denote as \( F_{Y \rightarrow X}(\omega_1,\omega_2) \), we compute the mean spectral GC across the range, thus

\[
F_{Y \rightarrow X}(\omega_1,\omega_2) = \frac{1}{\omega_2 - \omega_1} \int_{\omega_1}^{\omega_2} F_{Y \rightarrow X}(\omega)d\omega.
\]

(10)

It is noteworthy that the total time-domain GC is given by the mean spectral GC over all frequencies up to the Nyquist frequency \( \omega_N = \frac{\tau}{2} \).

\[
F_{Y \rightarrow X} = \frac{1}{\omega_N} \int_{0}^{\omega_N} F_{Y \rightarrow X}(\omega)d\omega.
\]

(11)

Simulation model

To validate our GC methodology, we simulated data from a multivariate autoregressive model with white noise error terms, a model for which we were able to derive true GC values analytically. The general such system is specified by:

\[
\begin{bmatrix} X(t) \\ Y(t) \end{bmatrix} = \sum_{k=1}^{p} A_k \begin{bmatrix} X(t-k_0) \\ Y(t-k_0) \end{bmatrix} + \begin{bmatrix} E_x(t) \\ E_y(t) \end{bmatrix},
\]

(12)

where \( t_0 \) is the time between observations and each \( E_x(t) \) and \( E_y(t) \) are independent Gaussian random variables of mean 0 and variance 1. True spectral GC values are obtained as follows. Since the residuals are uncorrelated in this model, spectral GC is given by Eq. (6). The transfer matrix is given by Eq. (5), and its inverse \( H \) by

\[
H(\omega) = \frac{1}{\text{det}(A(\omega))} \left( \frac{1 - \sum_{k=1}^{p} a_{k,yy}z^{-k}}{1 - \sum_{k=1}^{p} a_{k,yy}z^{-k}} \right),
\]

(13)

where \( z = e^{-i\tau} = e^{-i2\pi \alpha} \). From this, and Eq. (9), and using that the covariance matrix of residuals is the identity, we have

\[
S_{xx} = \frac{1}{|\text{det}(A(\omega))|^2} \left( 1 - \sum_{k=1}^{p} a_{k,yy}z^{-k} \right) + \left( \sum_{k=1}^{p} a_{k,yy}z^{-k} \right)^2.
\]

(14)

Putting these together into Eq. (6) yields

\[
F_{Y \rightarrow X}(\omega) = \ln \left( 1 + \frac{\sum_{k=1}^{p} a_{k,yy}z^{-k}}{1 - \sum_{k=1}^{p} a_{k,yy}z^{-k}} \right).
\]

(15)

For \( F_{X \rightarrow Y}(\omega) \), simply swap \( X \) and \( Y \) in Eq. (15).

Results

Granger causality analysis of EEG data

GC analysis was conducted on artifact-free epoched time series, following notch filtering and downsampling, reflecting mean EEG activity within two source-localized brain areas, the ACC and the PCC, recorded from subjects during normal wakeful resting (WR) and under propofol sedation (LOC). Figure 2 shows 40 sec representative samples of data from each area during both LOC and WR. These samples exhibit non-stationary features such as local linear trends at time scales of approximately 1 sec, which would confound GC analysis. To avoid confounds due to nonstationarity we divided the data into approximately stationary non-overlapping short segments from each of which we removed the mean and applied a linear detrend [19,20]. We chose segment lengths of 2 sec (i.e., 500 time points) in order to strike a balance between stationarity (shorter time series are more likely to be stationary) and model fit (longer time series support better parameter estimation for locally valid linear autoregressive...
models). For our data, shorter segments (1 sec) led to poor model fitting for many segments, while longer segments (4 sec) were frequently nonstationary; a 2 sec segment length is also in line with previous investigations of stationarity of EEG obtained from sleeping human subjects [21,22]. Dividing each epoch into non-overlapping 2 sec segments furnished at least 70 segments per condition per subject. Figure 3 illustrates representative segments (with additional normalization of standard deviation for clarity of illustration).

We next computed, for each segment, the recommended model order \( p \) as given by the Akaike information criterion (AIC) [23]. (We also computed the Bayesian information criterion [24]; however this criterion often failed to reach a minimum.) The 95th percentile of the values obtained was 20 (corresponding to 80 ms). We used this as our model order throughout the GC analysis.

We next carried out the following GC analysis method for each subject, condition (WR or LOC), direction, and frequency band (delta, theta, alpha, beta, gamma). First, for each 2 sec segment we calculated numerical estimates of GC using Eqs. (1), (2), (8) and (10), using the model order \( p = 20 \), and denoted these by \( \mathcal{F}_i(0) \) where \( i = 1, \ldots, n_s \), and \( n_s \) is the number of segments per condition for the given subject. These computations were performed using the Granger Causal Connectivity Analysis toolbox implemented in MATLAB (Natick, MA) [8].

Numerical GC values obtained directly from finite data yield biased estimates of the true GC of the underlying process. In our next step we estimated and removed the bias by applying the following permutation procedure. For each subject, condition, direction and frequency band, we selected 1000 random pairs of 2 sec segments from the ACC with (non-corresponding) 2 sec segments from the PCC. We then computed the numerical GC for each pair, \( \mathcal{F}_i(0) \), where \( x = 1, \ldots, 1000 \). Since each pair has a true GC of zero by definition, the distribution of observed GC values across all pairs approximates the null distribution for zero GC in processes that closely match the analyzed processes. From the empirical null distribution we extracted the mean \( \mu(\mathcal{F}(0)) \) and the standard error \( \sigma(\mathcal{F}(0)) \), i.e. standard deviation divided by \( \sqrt{1000} \). Approximately unbiased GC values were then obtained by subtracting the mean of the null distribution from the biased estimates: \( \hat{G}_i = \mathcal{F}_i(0) - \mu(\mathcal{F}(0)) \). It is worth noting that, for time-domain GC, and a true linear autoregressive process, this debiasing procedure is asymptotically exact. This follows because estimates of time-domain GC for such processes asymptotically follow a non-central chi-squared distribution with the true GC value given by the non-centrality parameter [16]. Therefore, the above procedure will furnish exactly unbiased GC values if any factors distorting the distribution away from a chi-square distribution affect the null and non-zero true GC distributions in the same way. These factors may include (i) aspects of the data that are not exactly linear autoregressive, (ii) analysis of short segments which challenge accurate model fitting, (iii) analysis in the frequency domain rather than the time-domain (exact distributions are not known for the frequency domain). In practice, even if these factors apply non-uniformly to null and non-null distributions, our debiasing procedure nonetheless provides improved empirical estimates of the true (unbiased) GC values. We further validate our methods by application to a simulation model (see Section ‘Simulation model’).

Finally, for each subject, condition, direction and frequency band, we obtained an estimate of the mean GC, \( \mu(\hat{G}) \) by taking the mean of the approximately unbiased estimates across segments,

\[
\mu(\hat{G}) = \frac{1}{n_s} \sum_{i=1}^{n_s} \hat{G}_i. \tag{16}
\]

An estimate of the standard error \( s(\hat{G}) \) of this estimate is then given by

\[
s(\hat{G}) = \frac{1}{\sqrt{n_s}} \sigma(\hat{G}) + \sigma(\mathcal{F}(0)), \tag{17}
\]

where \( \sigma \) denotes the standard deviation of the \( \hat{G}_i \).

We repeated the above procedure for the time-domain, with time-domain GC values computed in approximation by taking the mean over frequencies from 0.5–40 Hz (Eq. (10)). We avoided the explicit time-domain GC (3) because that was found to sometimes contain residual spurious contributions from the line noise at
50 Hz [9]; (we took 40 Hz as a safe frequency cut-off for avoiding this, and there was negligible power above 50 Hz in all data). We also repeated the procedure to compute GC values at all integer frequencies from 1 Hz to 40 Hz.

To confirm validity of application of linear regression models of order \( p = 20 \) to each of the data segments, following [8] we performed both the Durbin-Watson test for whiteness of residuals [25] and the consistency test of Ding et al [26]. Residuals were reliably white across all segments for all subjects (mean \( P > 0.66 \)), indicating that the linear regression models adequately accounted for the variance in the data. The mean consistency value across segments was \( > 80\% \) for all subjects and \( > 60\% \) for all subjects, verifying that the models are capable of regenerating the observed data with high accuracy. Together, these results validate the suitability of GC analysis for the data.

Figures 4 and 5 show band-limited and time domain GC for the directions (PCC→ACC) and (ACC→PCC) respectively. Figure 6 shows mean GC and phase synchrony, see below) at all integer frequencies for each condition and each subject. To assess significance of differences in GC between WR and LOC, for each subject, condition, direction and frequency, we performed a Wilcoxon rank sum test to compare the distributions of \( \hat{G}_{W}^{i} \) and \( \hat{G}_{L}^{i} \), i.e., the distributions across segments of approximately unbiased GC estimates for WR and LOC respectively. (Note that we are interested in whether GC values differ between conditions, not in whether any particular GC value is statistically significant.) The results of these tests are given in Table 1 (PCC→ACC) and Table 2 (ACC→PCC), at various significance levels. Verifying the consistency of these results, in all cases in which a significant difference was found at a false discovery rate of either \( < 0.01 \) or \( < 0.05 \), there was no overlap in the corresponding error bars in the corresponding graph (see Figs. 4 and 5). The overall outcome of this analysis is that changes in mean GC from WR to LOC show high inter-subject consistency, with most subjects exhibiting a bidirectional increase in GC between the ACC and the PCC during LOC, particularly in the beta and gamma bands.

Granger causality of simulated data

To validate the GC analysis of the EEG data, we applied the same procedure to the simulation model described in the section ‘Simulation model’, for which analytical GC values could be computed. The model we simulated had the following non-zero regression matrices

\[
A_{1} = \begin{pmatrix}
0.3 & 0 \\
0 & 0.2
\end{pmatrix}, \quad A_{10} = \begin{pmatrix}
0 & 0.25 \\
0.2 & 0
\end{pmatrix}.
\]

chosen so that there is frequency-dependent bidirectional causality between \( X \) and \( Y \). We assumed a sampling rate of 250 Hz, so that \( t_{0} = 4 \) ms. Using this model, we computed bidirectional spectral GC analytically using Eq. (15), and compared results with those obtained from simulated data consisting of 100 segments of length 2 sec each. For comparison with the GC analysis of the EEG data, we used a model order of \( p = 20 \). Figure 7 (a) shows the analytical GC and the numerically computed (‘sample’) GC both before and after application of the debiasing method described in the section ‘Granger causality analysis of EEG data’. It is clear that raw sample GC values have a substantial positive bias, which is significantly reduced uniformly across frequencies by the debiasing method. Figure 7 (b) shows the results of repeating this procedure over 100 different instantiations of the model, confirming the effectiveness of the debiasing method. We note that there is some remaining oscillation of the debiased value around the analytic value, but that this oscillation is small. Finally, we performed Wilcoxon tests on numerical GC estimates across 100 segments (of a single instantiation of the model) to look for significant differences in GC in the two directions. We tested for differences in band-limited GC in the frequency bands 1–25 Hz, 26–50 Hz, 51–75 Hz, 75–100 Hz and 100–125 Hz. Consistent with the analytical profile of the spectral GC measure, we found no significant difference in the 1–25 Hz band, \( P < 0.05 \) in the 26–50 Hz band, and \( P < 0.01 \) in all the other bands. These observations further attest the consistency of our method.

Figure 4. Mean band-limited GC computed using (16) in the direction PCC→ACC, in WR (light) and LOC (dark). Each panel shows a different frequency band; the bottom-right panel shows the time-domain. Error bars show standard error (17).

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We next compared the results of our GC analysis of the EEG data with a phase synchrony analysis of the same data. Unlike GC, phase synchrony provides an undirected measure of functional connectivity. Synchrony measures have also been widely applied in studies of both conscious content and conscious level (see [27] for a review). The present analysis extends the previous analysis [11], which found that on average, across all subjects, phase synchrony increased during LOC in the theta, alpha and gamma frequency bands. Here, augmenting this group level analysis, we investigate changes in synchrony for each subject individually.

As described in the Methods section, in contrast to the GC analysis, for the synchrony analysis we did not notch-filter or downsample the data during preprocessing. (We did repeat the synchrony analysis with downsampling to 250 Hz; the only effect of this was loss of significance for a few cases, due to the throwing away of data. Notch filtering would be redundant because bandpass filters are applied as part of the synchrony computation.) For each data point we computed the instantaneous synchrony between the ACC and PCC in each of the five frequency bands (delta, theta, alpha, beta, gamma) following the spatial analytic phase difference (SAPD) method of [28], which was also the method used in [11].

For each subject and condition we divided the synchrony data into 10 sec non-overlapping windows. For each window we calculated the proportion of time-points with above-threshold (i.e., 0.2 radian) SAPD phase synchrony within each frequency band. Figure 8 shows the mean of this proportion across all 10 sec windows, in each frequency band, for each subject individually. As for GC, we also computed synchrony at all integer frequencies from 1 Hz to 40 Hz (using pass bands of $f - 0.5$ Hz to $f + 0.5$ Hz for each frequency $f$). Figure 6 shows synchrony at all frequencies for each condition and subject, furnishing a direct comparison with the GC analysis. Together, Figures 8 and 6 indicate that phase synchrony generally increases during LOC though with less consistency across subjects than as compared to the GC analysis. Supporting this interpretation, Table 3 shows the outcome of significance tests on the difference in phase synchrony between WR and LOC, calculated using the Wilcoxon rank sum test. In contrast to the GC analysis, the results of this analysis show substantial variability between subjects, particularly in the beta and gamma bands, for which two subjects showed a highly significant decrease in synchrony during LOC while the majority of subjects showed a highly significant increase. Nonetheless, the grand average across all subjects showed an increase during LOC in the theta, alpha, beta and gamma bands and a decrease in the delta band (significance not tested for here), reconfirming the group-average analysis in [11].

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Power spectral density analysis of EEG data

To examine changes in spectral power on a subject-by-subject basis, we applied a fast Fourier transform to each of the 10 sec windows identified in the previous synchrony analysis. For each subject and frequency band we computed the mean power spectral density (PSD) across all windows, in both the ACC (Figure 9) and the PCC. Table 4 shows the outcome of Wilcoxon rank sum significance tests on the difference in PSD between LOC and WR for each subject and frequency band. The majority of entries in
this table show a significant increase in PSD during LOC, in line with the group-average results described by [11]. Corroborating these findings, Figure 10 shows the full PSD spectra in WR and LOC for the ACC region in each subject, averaged over all the windows.

Discussion

We have presented a method for applying GC analysis to steady state EEG data, that (i) accommodates non-stationarity by dividing the data into short approximately-stationary segments, and (ii) systematically removes bias by permutation analysis. Our method is generally applicable in neuroimaging contexts that generate continuous time series data at sampling rates reflecting neural interactions (magneto/electroencephalographic signals, intracranial recordings, electrocorticographic signals, other local-field-potential signals). We demonstrated the efficacy of our method via a rigorous set of simulations for which GC could be solved analytically. We illustrated its value by application to source-localized steady-state high-density EEG data obtained from healthy human subjects undergoing propofol-induced anaesthesia, examining changes in bidirectional GC between the ACC and
A rigorous methodology for GC analysis

The increasing focus on functional brain networks underlying cognition [29] requires well validated methods for extracting functional connectivity from time series data obtained via neuroimaging. While robust methods exist for identification of undirected functional connectivity (e.g., synchrony, correlation), methods for extracting directed functional (i.e., causal) connectivity are less well established. Among these methods, GC is especially promising because of its simple conceptual and statistical foundations (relative predictive ability and autoregressive modeling, respectively, see [7]), and because it does not require strong priors on the underlying connectivity patterns. GC can be contrasted with ‘dynamic causal modelling’ [30], which aims at assessing effective connectivity rather than (directed) functional connectivity. Functional connectivity describes directed or undirected network dynamics which need not univocally map onto underlying structural connectivity, whereas effective connectivity aims to infer the underlying physical generative processes [7,31]. GC also admits a useful interpretation in terms of information transfer because, for Gaussian variables, it is equivalent to transfer entropy [32]. Importantly, changes in GC are not confounded by changes in spectral power: changes in power simply rescale entropy [32]. Importantly, changes in GC are not confounded by these advantages, application of GC to empirical data requires

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<th>Subject</th>
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+1 indicates an increase during LOC, -1 indicates a decrease, and ‘n/s’ indicates no significant change. Absence of brackets indicates significance at a false discovery rate of <0.01, round brackets indicate significance at a false discovery rate of <0.05, and square brackets indicate significance at the P<0.05 level.

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Table 1. Significant changes in GC from WR to LOC, in the direction PCC→ACC, in each frequency band, and also in the time domain.

Table 2. Significant changes in GC from WR to LOC, in the direction ACC→PCC, in each frequency band, and also in the time domain.

Elements of the above method have been proposed previously. Analysis of short time-windows was advocated by Hesse et al [20]; however their emphasis was on extracting time-varying GC over short time-scales and not on accurate estimation of GC for steady-state data. To our knowledge, the issue of bias has not been
examined until now, possibly because most previous studies have been concerned with inference on the statistical significance of individual GC values and not on comparing distributions of GC values across conditions, as we do here. Importantly, we have been able to demonstrate the efficacy of our method with respect to debiasing via our novel analytically solvable model of spectral bidirectional GC.

The context of spectral bidirectional GC between two variables is deliberately simple. The method is however readily extensible to more complicated situations including conditional GC (in which the GC between each pair is conditioned on the common causal influence of other variables, see [6,9]) and ‘multivariate’ or ‘block’ GC in which causality is assessed between two (or more) multivariate variables (i.e., variables consisting of >1 time series) [33]. With respect to preprocessing we have emphasized the need to avoid bandpass filtering. While GC is theoretically invariant to very general filtering, in practice GC estimates are often confounded by increases in empirical model order entailed by the application of a filter [9]. Hence we recommend that filtering be used only where absolutely necessary to ensure stationarity (e.g., application of a notch filter to remove line noise); bandpass filtering should not be applied as a panacea for artifact removal; furthermore, bandpass filtering is entirely inappropriate for estimation of GC within specific frequency ranges. In the latter case, the correct approach is to compute spectral GC at all frequencies and then integrate over the desired range (‘band-limited’ GC, see [9]).

Dynamical neural correlates of propofol anaesthesia

The neurophysiological changes accompanying propofol-induced LOC have been extensively studied. Alkire and colleagues found using positron emission tomography a reduction in global
brain metabolism of about 50% [34]; however global brain metabolism is not a reliable predictor of conscious level, as demonstrated by patients who recover from a vegetative state while still exhibiting dramatically reduced brain metabolism [35]. While a large number of subsequent studies have focused on region-specific neural activity changes during anaesthesia, only recently have researchers studied changes in connectivity. Connectivity studies of propofol-induced LOC have now leveraged multimodal neuroimaging methods including functional magnetic resonance imaging [36,37,38,39], EEG [11,40,41], and electrocorticography [42]. Other important studies assessed connectivity changes using different anaesthetic agents including isoflurane and halothane [43] and midazolam [44], the latter in combination with transcranial magnetic stimulation (TMS). A complex picture is emerging from these studies, indicating that anaesthetic LOC is associated with modulated operation of discrete networks rather than global or regional suppression or enhancement of neural activity [45]. However, the diversity of methodologies, potential anaesthetic pathways, and neuroimaging results, together indicate a need for overarching theories specifying unifying dynamical mechanisms.

Addressing this need, a variety of theoretical interpretations have been offered to account for the sedative effects of anaesthetics, including impaired thalamocortical connectivity [43], “cognitive unbinding” of low-level sensory and high-level executive cortical regions [46,47], reduced information integration [45,2,48], and diminished causal density among participating brain regions [49,3]. The latter two notions specifically involve causal interactions and so are particularly relevant to the present approach. Integrated information uses information theory to capture the extent to which a system considered as a whole generates more information than when considered as a set of independent parts [2,50,48]. Causal density uses GC to measure the overall level of causal interactivity sustained by a system [49,3]. Both measures are motivated by the observation that conscious experiences seem, at the level of phenomenology, to be simultaneously highly differentiated (each experience is different from every other experience) and highly integrated (every experience appears as a unified whole). Both measures also account for experimental observations that consciousness seems to be lost in situations in which the underlying neural dynamics are disintegrated [44,51] or pathologically integrated, as in generalized epilepsy [52].

The ability to detect directed functional brain networks during anaesthetic LOC is therefore key to refining, as well as differentiating between, the above theories. To our knowledge, only one previous neuroimaging study has attempted this. Lee and colleagues [41] used a method based on asymmetry of modulations of scalp EEG signals, finding diminished feedback connectivity during LOC. However, their method is not widely used as compared to GC and its properties are less well understood. In a related study, Ferrarelli et al examined effective connectivity during anaesthesia by perturbing the brain using TMS and observing cortical response patterns [44]. However, this perturbational method does not characterize directed functional networks per se. In this context, the method we have described opens the way to

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**Table 3.** Significant changes in mean phase synchrony from WR to LOC in each frequency band.

<table>
<thead>
<tr>
<th>Subject</th>
<th>1</th>
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<tbody>
<tr>
<td>δ</td>
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<td>n/s</td>
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<td>n/s</td>
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<tr>
<td>γ</td>
<td>(–)</td>
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<tr>
<td>α</td>
<td>n/s</td>
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<td>+</td>
<td>+</td>
<td>+</td>
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</tbody>
</table>

‘+’ indicates an increase during LOC, ‘–’ indicates a decrease, and ‘n/s’ indicates no significant change. Absence of brackets indicates significance at a false discovery rate of <0.01, round brackets indicate significance at a false discovery rate of <0.05, and square brackets indicate significance at the P<0.05 level.

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**Figure 9.** Mean power spectral density in the ACC in WR (light) and LOC (dark). Each panel shows a different frequency band. Error bars show standard error. Mean and standard error computed across 10 sec windows of data, see main text.

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Conclusions

We have described a methodological pipeline for GC analysis of steady-state EEG signals, accommodating nonstationarity, eliminating bias, and validated against an analytically solvable model. This pipeline represents a contribution towards the general problem of identifying directed functional connectivity in brain networks [29], with specific relevance to the problem of measuring conscious level [35,3]. The bidirectional increases in GC that we observed between the ACC and PCC appear to challenge current theories of consciousness based on integrated information and causal density. However, these theories are based on network-theoretic descriptions of causal connectivity which are not well represented by considering only two regions. Further studies incorporating additional regions are therefore required to shed new light on the network-level dynamical changes underlying anaesthetic LOC. Such studies may, as a result, furnish novel theoretically-motivated procedures for assessing intraoperative anaesthetic depth [45] and for assaying residual consciousness in traumatically brain-injured patients [56]. The increased between-subject consistency we observed for GC, as compared to phase synchrony, further supports its potential use as a biomarker for consciousness.

The present GC analysis could build on the theory of neuronal global workspace [13,1]. This theory posits that consciousness is supported by the increased between-subject consistency we observed for GC, as compared to phase synchrony, further supports its potential use as a biomarker for consciousness.

<table>
<thead>
<tr>
<th>Table 4. Significant changes in mean power from WR to LOC in each frequency band and for both the ACC and the PCC.</th>
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</thead>
<tbody>
<tr>
<td>Subject</td>
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‘+’ indicates an increase during LOC, ‘−’ indicates a decrease, and ‘n/s’ indicates no significant change. Absence of brackets indicates significance at a false discovery rate of <0.05, and square brackets indicate significance at the P < 0.05 level.
doi:10.1371/journal.pone.0029072.t004

Figure 10. Mean (log) power spectral density in the ACC during WR (blue) and LOC (red) for each subject. Logarithms are to base 10.
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explicitly linking theoretically-motivated measures of conscious level with experimentally available data. Our method is also supported by the increased between-subject consistency we observed in modulations of GC, as compared to modulations of phase synchrony, suggesting that GC analysis may offer increased robustness as well as sensitivity to directed interactions.

Stepping back, most theoretical views share the notion that anaesthetic LOC is associated with decreased functional (or effective) connectivity, whether directed or undirected. On the face of it, these views contrast with our results which showed increased GC and phase synchrony during LOC, as well as increased power. However, increased functional connectivity could be consistent with overall reduction of causal density and/or information integration under at least two scenarios. First, high values of some measures (synchrony, bivariate GC) could reflect pathologically increased integration at the expense of differentiation. This view aligns with the increased cortical-subcortical synchrony observed during LOC associated with generalized epilepsy [32]; these authors argue that enhanced synchrony ‘blocks access’ to a neuronal global workspace. Second, in any GC analysis, common unmeasured sources can influence results [33,59]. In this context, it is important to recognize that the present results are based on analyzing connectivity between only two areas, the ACC and the PCC, which form part of a distinctive anatomical cortical backbone (the ‘mesial highway’) [34]. Thus it is plausible that increased functional connectivity between the ACC and the PCC may reflect a wider disruption or disintegration of functional connectivity, once other regions are taken into account. Adequate tests of theories based on functional disintegration therefore require extending the present analysis to incorporate a broader range of cortical (and possibly subcortical) sources, together with fully multivariate measures of causal connectivity.

Conclusions

G-Causality in EEG during Propofol Anaesthesia

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