

# Magnetic moment $(g - 2)_\mu$ and new physics

Dominik Stöckinger, TU Dresden



Sussex, November 2011

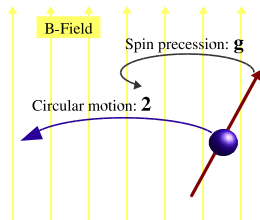
# Outline

- 1 Introduction
  - Motivation and Prehistory
  - Legacy of Brookhaven measurement:  $3\sigma$  deviation
- 2 New  $g - 2$  experiments at Fermilab and JParc
- 3 Impact on New Physics in general
- 4 SUSY could explain the deviation
  - General behaviour
  - Two-loop contributions
  - $a_\mu$ , parameter measurements and model discrimination
- 5 Alternatives to SUSY
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# Muon magnetic moment



$$H_{\text{magnetic}} = -2(1 + a_{\mu}) \frac{e}{2m_{\mu}} \vec{B} \cdot \vec{S}$$

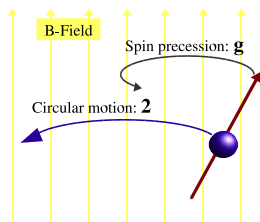
Measurement:

circular motion:  $\omega_c = -\frac{e}{m_{\mu}} B$

spin precession:  $\omega_s = -\frac{2(1+a_{\mu})e}{2m_{\mu}} B$

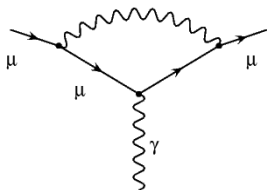
$\rightarrow$  measure  $\omega_a = \omega_s - \omega_c = -a_{\mu} \frac{e}{m_{\mu}} B$

# Muon magnetic moment



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Quantum field theory:

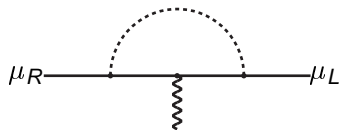


$$\approx \bar{u}(p') \left[ \gamma_{\mu} F_1 + \frac{i}{2m_{\mu}} \sigma_{\mu\nu} q^{\nu} a_{\mu} \right] u(p)$$

$$\rightarrow \text{Operator: } \frac{a_{\mu}}{m_{\mu}} \bar{\mu}_L \sigma_{\mu\nu} q^{\nu} \mu_R$$

# Why is $a_\mu$ special?

$$\frac{a_\mu}{m_\mu} \bar{\mu}_L \sigma_{\mu\nu} \mu_R F^{\mu\nu}$$

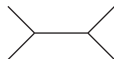


Beautifully simple “textbook” quantity, very precise

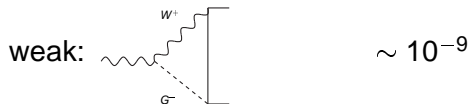
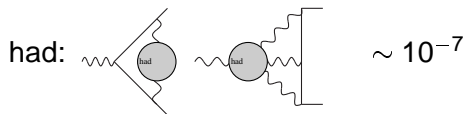
**CP- and Flavour-conserving, chirality-flipping, loop-induced**

compare: EDMs,  $b \rightarrow s\gamma$   
 $B \rightarrow \tau\nu$   
 $\mu \rightarrow e\gamma$

EWPO



# Classification of SM contributions



# (Pre)history

'49 Schwinger: QED 1L:

$$\frac{\alpha}{2\pi}$$

'57 Garwin et al:

$g_{\mu} \approx 2 \Rightarrow$  Muon=Dirac particle!



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hadronic cont. needed, confirmed!

'80-'11 Theory developments:

QED, hadronic,

weak cont. [Czarnecki, Krause, Marciano '95]  
[Heinemeyer, DS, Weiglein '04]

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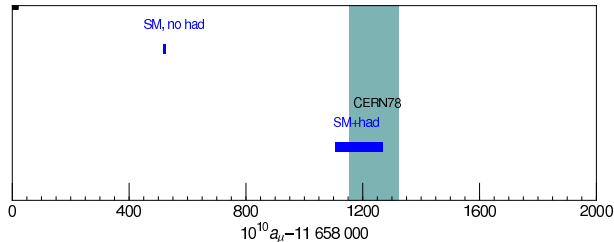
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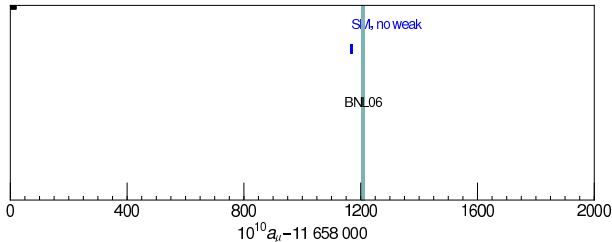
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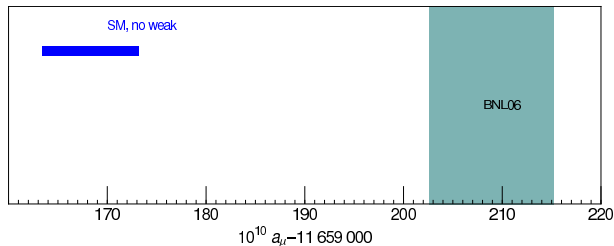
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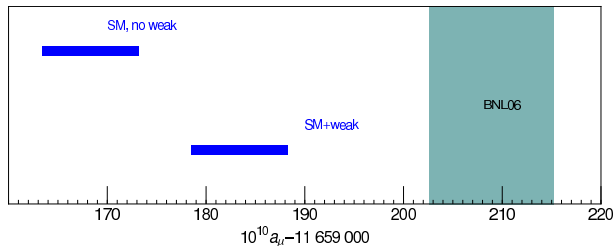
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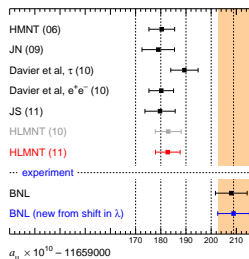
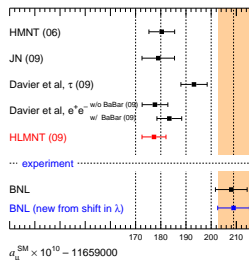


# Era of the muon $g - 2$ experiment at Brookhaven



$$a_{\mu}^{\text{exp}} = (11\,659\,208.9 \pm 6.3) \times 10^{-10}$$

# Current status: SM prediction



Full SM:  $a_\mu \times 10^{10} - 11659000$

|          |                |                 |
|----------|----------------|-----------------|
| dR08:    | ... 178.5(5.1) | (3.6 $\sigma$ ) |
| JN09:    | ... 179.0(6.5) | (3.2 $\sigma$ ) |
| HLMNT09: | ... 177.3(4.8) | (4.0 $\sigma$ ) |
| Detal09: | ... 183.4(4.9) | (3.2 $\sigma$ ) |
| JS11:    | ... 179.7(6.0) | (3.3 $\sigma$ ) |
| HLMNT11: | ... 182.8(4.9) | (3.3 $\sigma$ ) |
| BDDJ11:  | ... 175.4(5.3) | (4.1 $\sigma$ ) |

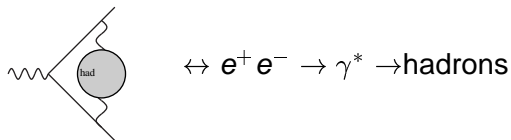
Exp:

BNL06: ... 208.9(6.3)

3 $\sigma$  deviation established

# Current status: SM prediction

Hadronic vacuum polarization contributions:



Recent progress:

- new exp data (CMD2, SND, KLOE, B-factories)  
⇒ significantly more precise!
- possible explanations of  $\tau$ -based results  
→ confirmation of  $e^+ e^-$ -based evaluations

[Benayoun et al '07][Jegerlehner, Szafron '11]

- assume  $e^+ e^-$  data different  
⇒ contradiction to Higgs mass bounds!

[Marciano, Passera, Sirlin '08]

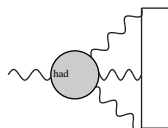




# Current status: SM prediction

## Hadronic light-by-light contributions

new estimates with correct sign,  
using different approximations



|                                     |                |
|-------------------------------------|----------------|
| [Bijnens, Prades '07]               | $10.0 \pm 4.0$ |
| [Melnikov, Vainshtein '03]          | $13.6 \pm 2.5$ |
| [Jegerlehner '08]                   | $11.4 \pm 3.8$ |
| [Jegerlehner, Nyffeler '09]         | $11.6 \pm 4.0$ |
| [Prades, Vainshtein, de Rafael '08] | $10.5 \pm 2.6$ |

Cannot be computed from first principles — Error difficult to assess!

Promising new approaches: lattice, Dyson-Schwinger, perturbative

# Discrepancy

SM prediction too low by  $\approx (25 \pm 8) \times 10^{-10}$

Why?

Confirmation needed!

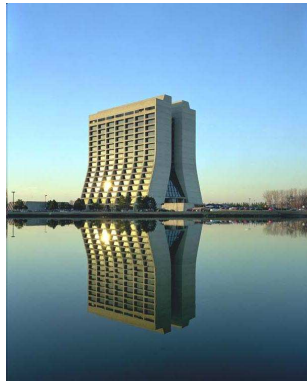
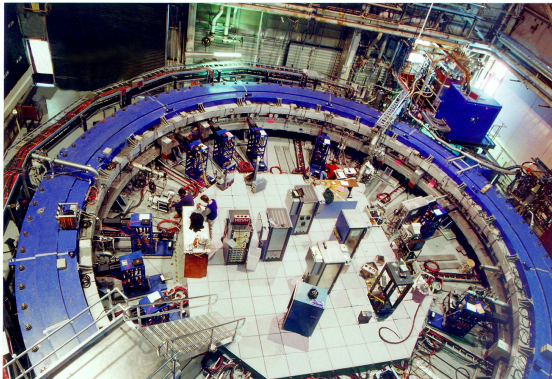
Note: discrepancy **twice as large as**  $a_{\mu}^{\text{SM,weak}}$

but we expect:  $a_{\mu}^{\text{NP}} \sim a_{\mu}^{\text{SM,weak}} \times \left(\frac{M_W}{M_{\text{NP}}}\right)^2 \times \text{couplings}$

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# The Opportunity

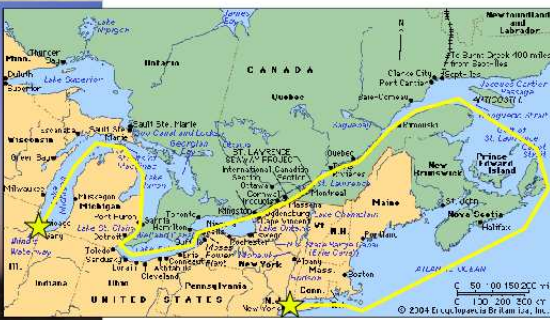


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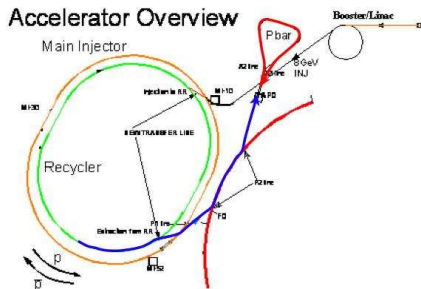


## Barge around St. Lawrence

- Airlift coils to barge off Long Island
- Estimated barge cost \$1M to transport yoke steel and coils
- Ship through St Lawrence -> Great Lakes -> Calumet SAG
- Airlift from somewhere around Romeoville, IL to Fermilab



# Advantages of Fermilab



$\pi$  decay length 900m vs 88m

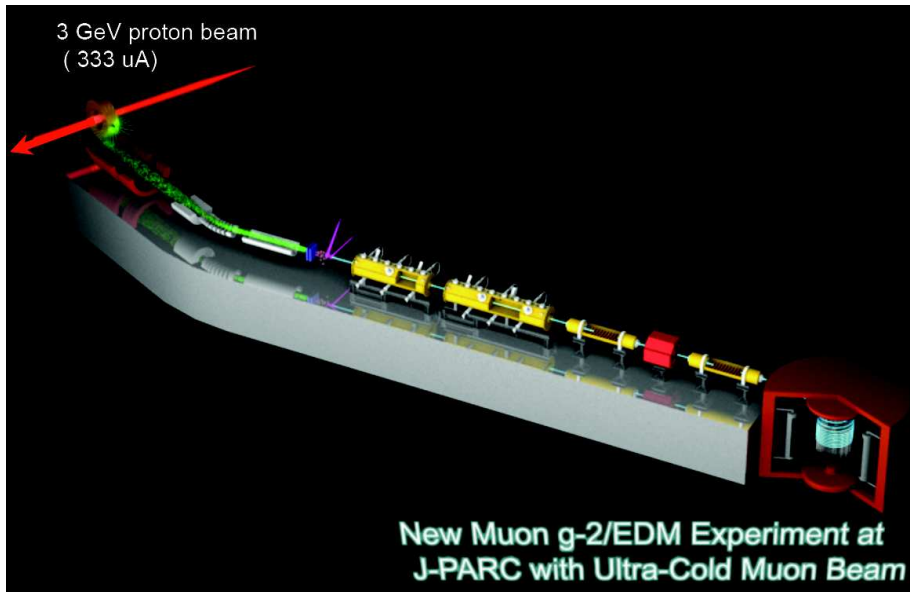
- 6–12 times more stored muons per initial proton
- 4 times fill frequency
- 20 times reduced hadronic-induced background at injection

# The Collaboration



First collaboration meeting after approval in March

# Complementary experiment at JParc (N. Saito)





## Complementary experiment at JParc (N. Saito)

|                              | BNL-E821      | Fermilab | J-PARC    |
|------------------------------|---------------|----------|-----------|
| Muon momentum                | 3.09 GeV/c    |          | 0.3 GeV/c |
| gamma                        | 29.3          |          | 3         |
| Storage field                | B=1.45 T      |          | 3.0 T     |
| Focusing field               | Electric quad |          | None      |
| # of detected $\mu^+$ decays | 5.0E9         | 1.8E11   | 1.5E12    |
| # of detected $\mu^-$ decays | 3.6E9         | -        | -         |
| Precision (stat)             | 0.46 ppm      | 0.1 ppm  | 0.1 ppm   |

## Goal of both new $(g - 2)$ experiments

$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = (255?? \pm 16^{\text{Exp}} \pm 34^{\text{Th??}}) \times 10^{-11}$$

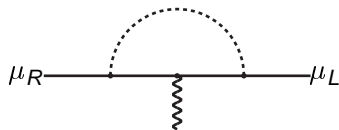
Data in  $\sim 4$ – $5$  years

- Tremendously useful complement of LHC (and flavour physics experiments), independent of final value [Hertzog, Miller, de Rafael, Roberts, DS '07]
- Benchmark for any new physics scenario
- Timely, complementary constraints
- This will be demonstrated in the following

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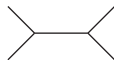
# Why is $a_\mu$ special?



## CP- and Flavour-conserving, chirality-flipping, loop-induced

compare: EDMs,  $B \rightarrow \tau \nu$   
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EWPO

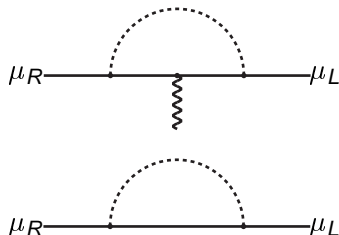


# New physics contributions to $a_\mu$

$g - 2 =$  chirality-flipping interaction

$m_\mu =$  chirality-flipping interaction as well

are the two related?



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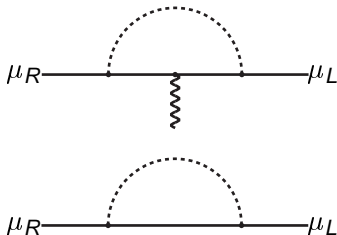
$m_\mu =$  chirality-flipping interaction as well

are the two related?

New physics loop contributions to  $a_\mu$ ,  $m_\mu$  related by chiral symmetry

[Czarnecki, Marciano '01]

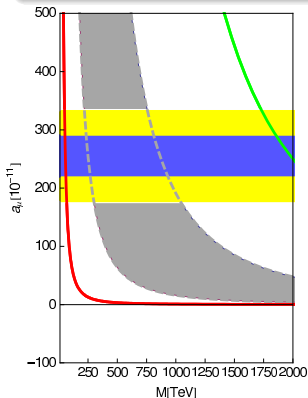
generally: 
$$\delta a_\mu(\text{N.P.}) = \mathcal{O}(\mathbf{C}) \left( \frac{m_\mu}{M} \right)^2, \quad \mathbf{C} = \frac{\delta m_\mu(\text{N.P.})}{m_\mu}$$



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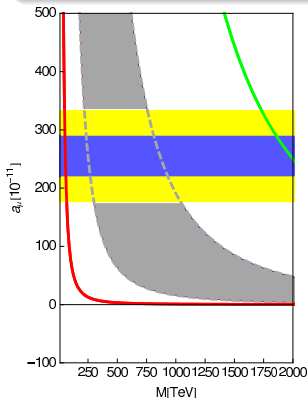
classify new physics:  $C$  **very** model-dependent



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$\mathcal{O}(1)$

$\mathcal{O}\left(\frac{\alpha}{4\pi} \dots\right)$

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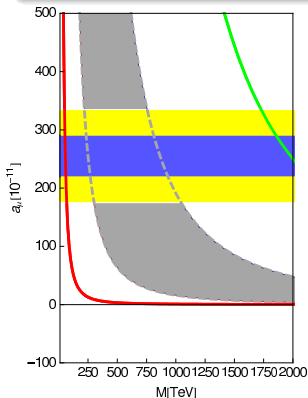
$Z', W', \text{UED, Littlest Higgs (LHT)} \dots$



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supersymmetry ( $\tan \beta$ ), unparticles

[Cheung, Keung, Yuan '07]

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extra dim. (ADD/RS) ( $n_C$ )...

[Davioudasl, Hewett, Rizzo '00]

[Graesser,'00][Park et al '01][Kim et al '01]

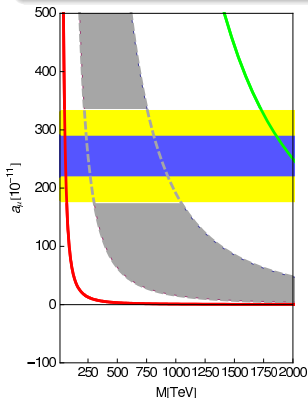
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$\mathcal{O}(1)$

radiative muon mass generation ...

[Czarnecki, Marciano '01]

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# $a_\mu$ and new physics

Different types of new physics lead to very different  $\delta a_\mu$  (N.P.)

- SUSY, RS, ADD, . . . : strong parameter constraints
- $Z'$ , UED, LHT, . . . : ruled out if deviation confirmed

If new physics found at LHC:

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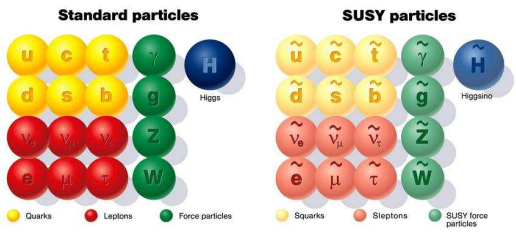
Now illustrate general points with examples

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# SUSY and the MSSM

- MSSM:



- free parameters:  $\tilde{m}$  masses and mixings,  $\mu$  and  $\tan \beta$

## $g - 2$ in the MSSM: chirality flips, $\lambda_\mu$ , and $H_2$

$$\tan \beta = \frac{\langle H_2 \rangle}{\langle H_1 \rangle}, \quad \mu = H_2 - H_1 \text{ transition}$$

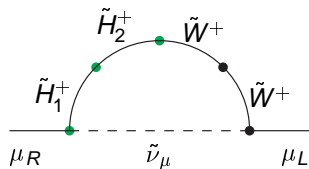
some terms

$$\propto \lambda_\mu \langle H_1 \rangle = m_\mu \quad \rightarrow \quad a_\mu^{\text{SUSY}} \propto \frac{m_\mu^2}{M_{\text{SUSY}}^2}$$

some terms

$$\propto \lambda_\mu \mu \langle H_2 \rangle = m_\mu \mu \tan \beta \quad \rightarrow \quad a_\mu^{\text{SUSY}} \propto \tan \beta \text{sign}(\mu) \frac{m_\mu^2}{M_{\text{SUSY}}^2}$$

**potential enhancement**  $\propto \tan \beta = 1 \dots 50$  (and  $\propto \text{sign}(\mu)$ )



# $g - 2$ in the MSSM

numerically

$$a_{\mu}^{\text{SUSY}} \approx 12 \times 10^{-10} \tan \beta \text{ sign}(\mu) \left( \frac{100 \text{ GeV}}{M_{\text{SUSY}}} \right)^2$$

SUSY could be the origin of the observed  $(25 \pm 8) \times 10^{-10}$  deviation!

$a_{\mu}$  significantly restricts the SUSY parameters

→ generically, positive  $\mu$ , large  $\tan \beta$ /small  $M_{\text{SUSY}}$  preferred

Precise analysis justified!



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- 1-loop and most 2-loop contributions known
- remaining theory uncertainty of SUSY prediction: [DS '06]

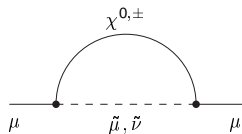
$$\delta a_{\mu}^{\text{SUSY}} \approx 3 \times 10^{-10}$$

Aim in Dresden: reduce error to  $1 \times 10^{-10} \Rightarrow$  full computation!

# Status of SUSY prediction

1-Loop

$$\propto \tan \beta$$



[Fayet '80],...

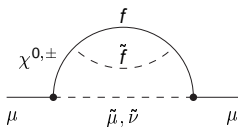
[Kosower et al '83],[Yuan et al '84],...

[Lopez et al '94],[Moroi '96]

complete

2-Loop (SUSY 1L)

$$\text{e.g. } \propto \log \frac{M_{\text{SUSY}}}{m_\mu}$$



[Degrassi, Giudice '98]

[Marchetti, Mertens, Nierste, DS '08]

[Schäfer, Stöckinger-Kim,

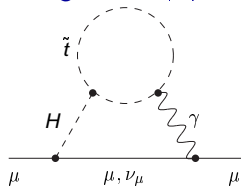
v. Weitzershausen, DS '10]

photonic  
 $(\tan \beta)^2$

rest under investigation

2-Loop (SM 1L)

$$\text{e.g. } \propto \tan \beta \mu m_t$$



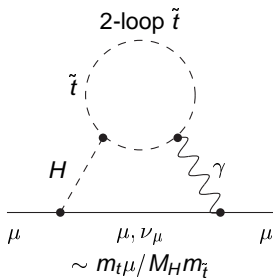
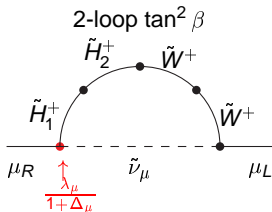
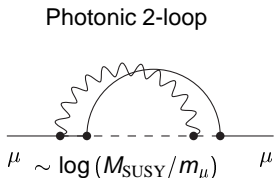
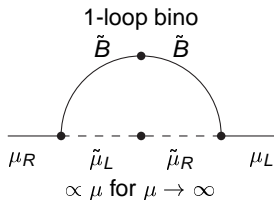
[Chen, Geng'01][Arhib, Baek '02]

[Heinemeyer, DS, Weiglein '03]

[Heinemeyer, DS, Weiglein '04]

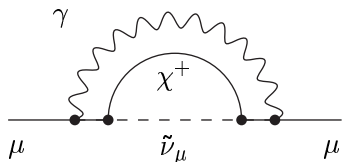
complete

# Physics of subleading contributions (examples)



Important for drawing precise conclusions from confronting  
 SUSY-prediction with  $a_\mu^{\text{Exp-SM}}$

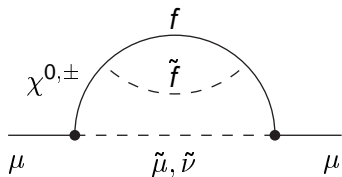
# Technical details: Photon loops



## All SUSY 1-loop diagrams with additional photon loop

- leading log:  $-7 \dots -9\%$  [Degrassi, Giudice '98]
- full result: subleading logs,  $\log(m_\chi/m_{\tilde{\nu}_\mu})$ , non-log terms
- additional terms  $\mathcal{O}(1\%)$
- full result more precise [v. Weitershausen, Schäfer, Stöckinger-Kim, DS '09]
- technically difficult but useful: contains all infrared divergences

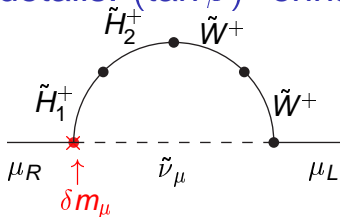
## Technical details: $f/\tilde{f}$ -loops



### All SUSY 1-loop diagrams with additional $f/\tilde{f}$ -loop (3rd generation)

- finite, gauge invariant class of contributions
- enhanced by top/bottom Yukawa coupling
- partial results [Drechsel, Gneidiger, Passehr, Schäfer, Stöckinger-Kim, DS] [Fagnoli, Stöckinger-Kim]
- typically  $\mathcal{O}(1\%)$

## Technical details: $(\tan \beta)^2$ enhanced corrections



$$a_\mu^{\text{SUSY}} \propto \text{chirality flip} \propto \lambda_\mu$$

However, one-loop coupling to “wrong” Higgs doublet induces shift

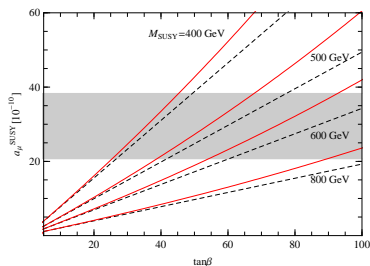
$$\lambda_\mu \rightarrow \frac{\lambda_\mu}{1 + \Delta_\mu} \quad \text{or} \quad \delta m_\mu^{\text{OS}} = \frac{m_\mu}{1 + \Delta_\mu} + \dots$$

Corresponding 2-loop shift in  $a_\mu^{\text{SUSY}}$

[Marchetti, Mertens, Nierste, DS '08]

$$a_\mu^{\text{SUSY}} \rightarrow \frac{a_\mu^{\text{SUSY}}}{1 + \Delta_\mu}$$

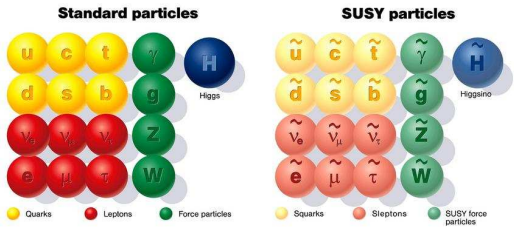
# Technical details: leading two-loop corrections



$$a_{\mu}^{\text{SUSY}} = a_{\mu}^{\text{SUSY,1L}} \left( 1 - \frac{4\alpha}{\pi} \log \frac{M_{\text{SUSY}}}{m_{\mu}} \right) \left( \frac{1}{1 + \Delta_{\mu}} \right)$$

- QED-logs:  $-7 \dots -9\%$
- $(\tan \beta)^2$ :  $+1 \dots +15\%$ ,  $\Delta_{\mu}(M_{\text{SUSY}}) \approx -0.0018 \tan \beta \text{ sign}(\mu)$

# SUSY and $a_\mu$



$$a_\mu^{\text{SUSY}} \approx 12 \times 10^{-10} \tan \beta \text{sign}(\mu) \left( \frac{100 \text{GeV}}{M_{\text{SUSY}}} \right)^2$$

$\tan \beta = \frac{v_2}{v_1}$ ,  $\mu = H_1 - H_2$  transition — central for EWSB

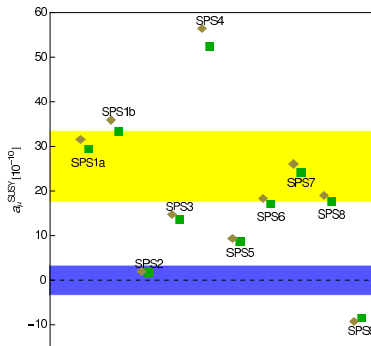
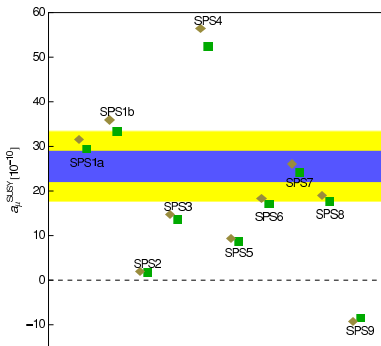
If SUSY signals at LHC:

$a_\mu$  complementary for: model selection, parameter measurements

→ understand EWSB, link to GUT scale ...

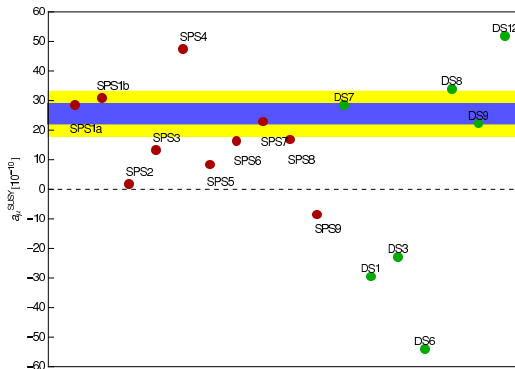


# $a_\mu$ central complement for SUSY parameter analyses



- $a_\mu$  sharply distinguishes SUSY models
- breaks LHC degeneracies

# $a_\mu$ central complement for SUSY parameter analyses

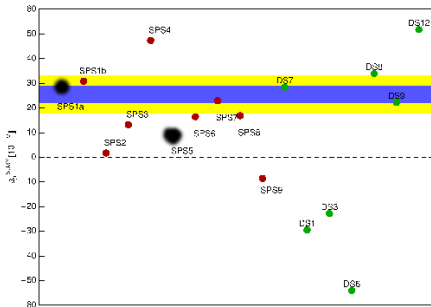


SPS benchmark points

LHC Inverse Problem ( $300\text{fb}^{-1}$ )  
can't be distinguished at LHC

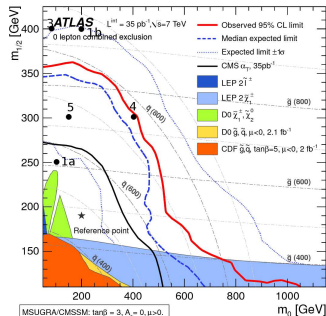
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# $a_\mu$ central complement for SUSY parameter analyses



SPS benchmark points

LHC Inverse Problem ( $300\text{fb}^{-1}$ )  
 can't be distinguished at LHC  
 [Sfitter: Adam, Kneur, Lafaye,  
 Plehn, Rauch, Zerwas '10]



[ATLAS jets+0lepton 02/11]

- LHC already rules out small masses in CMSSM
- $\Rightarrow$  large  $\tan \beta$  (SPS1b,4)? Non-CMSSM (heavier squarks)?
- $a_\mu^{\text{SUSY}}$  smaller?

# Ways to reconcile the LHC bounds with $a_\mu$

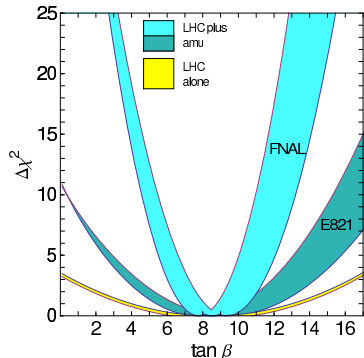
LHC mainly constrains squarks/gluinos

- Even within the CMSSM: heavy masses + large  $\tan \beta$
- Beyond the CMSSM: sleptons lighter than squarks

Don't worry, SUSY still viable — but the LHC— $b$ -decays— $a_\mu$  tensions start preferring some parameter regions

- If SUSY exists,  $a_\mu$  will be even important to measure parameters

# $a_\mu$ central complement for SUSY parameter analyses



[Hertzog, Miller, de Rafael, Roberts, DS '07]

$\tan \beta = \frac{v_2}{v_1}$   
central for understanding EWSB

LHC:  $(\tan \beta)^{\text{LHC, masses}} = 10 \pm 4.5$  bad  
[Sfitter: Lafaye, Plehn, Rauch, Zerwas '08, assume SPS1a]

$a_\mu$  improves  $\tan \beta$  considerably

vision: test universality of  $\tan \beta$ , like for  $\cos \theta_W = \frac{M_W}{M_Z}$  in the SM:

$$(\tan \beta)^{a_\mu} = (\tan \beta)^{\text{LHC, masses}} = (\tan \beta)^H = (\tan \beta)^{b?}$$

# Outline

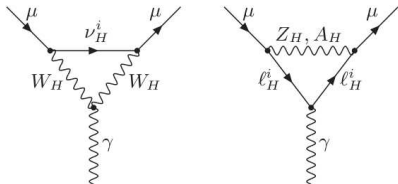
- 1 Introduction
  - Motivation and Prehistory
  - Legacy of Brookhaven measurement:  $3\sigma$  deviation
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# Littlest Higgs (with T-parity)

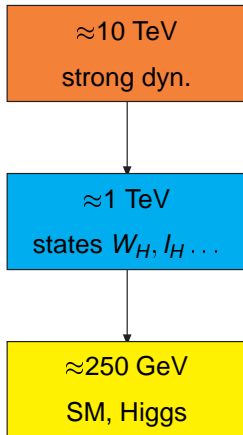
[Georgi; Arkani-Hamed, Cohen, Georgi]  
 Concrete LHT model: [Cheng, Low '03]  
 [Hubisz, Meade, Noble, Perelstein '06]

## Bosonic SUSY

- partner states, same spin
- cancel quadratic div.s
- T-parity  $\Rightarrow$  lightest partner stable



no enhancement of  $\frac{\alpha}{4\pi} \left(\frac{m_\mu}{M}\right)^2$



$$a_\mu^{\text{LHT}} < 1.2 \times 10^{-10}$$

[Blanke, Buras, et al '07]

Clear-cut prediction, sharp distinction from SUSY possible

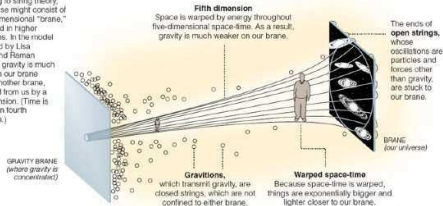
# Randall-Sundrum models

**Big question:** Where does the hierarchy  $M_{\text{Pl}} : M_W \sim 10^{17}$  come from?

**Answer:** beautifully explained by warp factor  $e^{-kL}$

## Island Universes in Warped Space-Time

According to string theory, our universe might consist of a three-dimensional "brane," embedded in higher dimensions. In the model developed by Lisa Randall and Raman Sundrum, gravity is much weaker on our brane than on another brane, separated from us by a fifth dimension. (Time is the unseen fourth dimension.)



Gravity propagates in extra dimension  
each KK-Graviton contributes equally,  
weakly, **no decoupling!**

TeV-scale determined by:

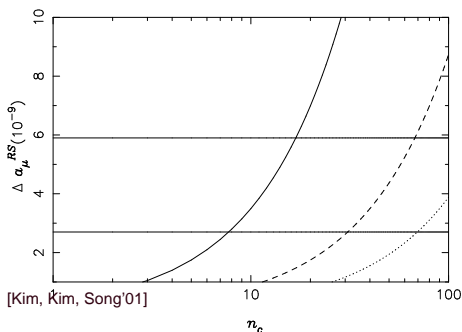
- coupling  $k/M_{\text{Pl}}$
- scale  $\Lambda_\pi = e^{-kL} M_{\text{Pl}}$

theory breaks down at scale  
 $\sim \Lambda_\pi$ ,  $n_c$  KK-gravitons up to  
that scale

$$\rightarrow a_\mu^{\text{RS}} \sim \frac{5n_c}{16\pi^2} \frac{m_\mu^2}{\Lambda_\pi^2}$$



# $g - 2$ and Randall-Sundrum models



## Complementarity: LHC

- lowest KK-modes
- masses

## $a_\mu$ from KK-loops

- feels all KK-modes
- e.g.  $C_{\text{Grav}} \propto M^2$ ,  $C_H \sim 1$
- guides model building of full theory

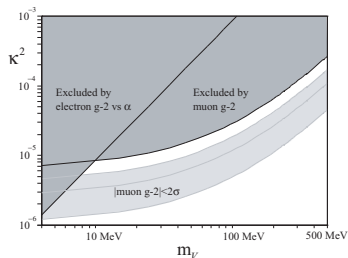
# Other types of new physics

What if the LHC does not find new physics — “Dark force”? [Pospelov, Ritz...]

- very light new vector boson
- very weak coupling
- motivated e.g. by dark matter, not by EWSB

$$C \propto 10^{-8}, M < 1\text{GeV}$$

- $a_\mu$  can be large
- could be “seen” by  $a_\mu$ -exp.



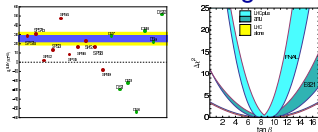
[Pospelov 08]

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# Conclusions

- Currently  $a_{\mu}^{\text{Exp}} - a_{\mu}^{\text{SM}} \approx (25 \pm 8) \times 10^{-10}$  — tantalizing
- New Fermilab measurement will start soon — very promising!
- $a_{\mu}^{\text{N.P.}}$  very model-dependent, typically  $\mathcal{O}(\pm 1 \dots 50) \times 10^{-10}$ 
  - ▶ Benchmark, model discriminator
  - ▶ unique properties
- New measurement of  $a_{\mu}$  will
  - ▶ sharply distinguish models, even with similar LHC signatures
  - ▶ break degeneracies
  - ▶ measure central parameters



$a_{\mu}$  will provide essential complementary input in the quest to understand TeV-scale physics — no matter what the result  
**BSM physics can look forward to the new  $a_{\mu}$  measurement!!**