

# Heavy quark pair physics with LHCb

Rhorry Gauld

Particle Theory Seminar  
University of Sussex - 23/03/15



**Science & Technology**  
Facilities Council

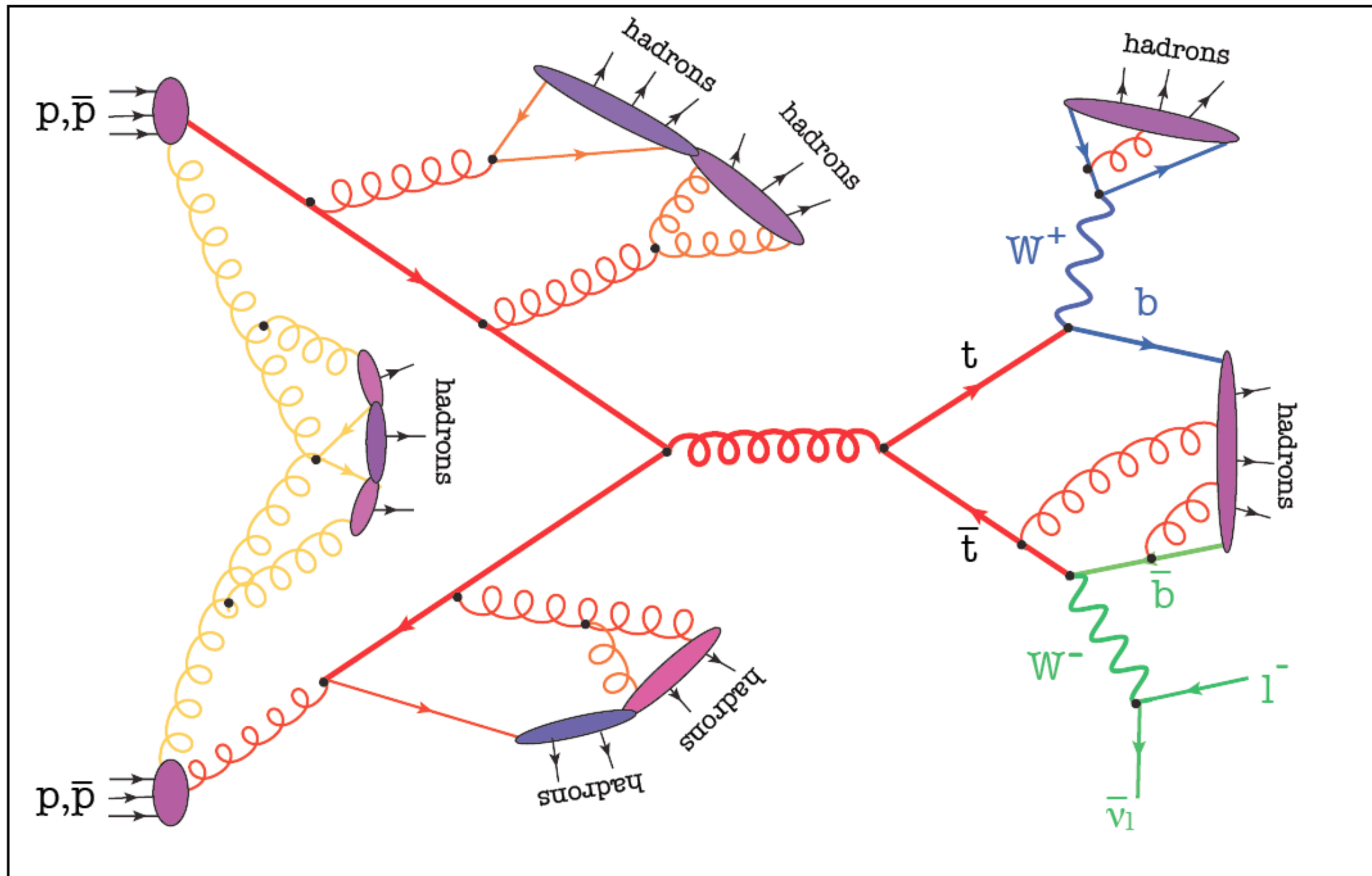


**Durham**  
University

# Overview

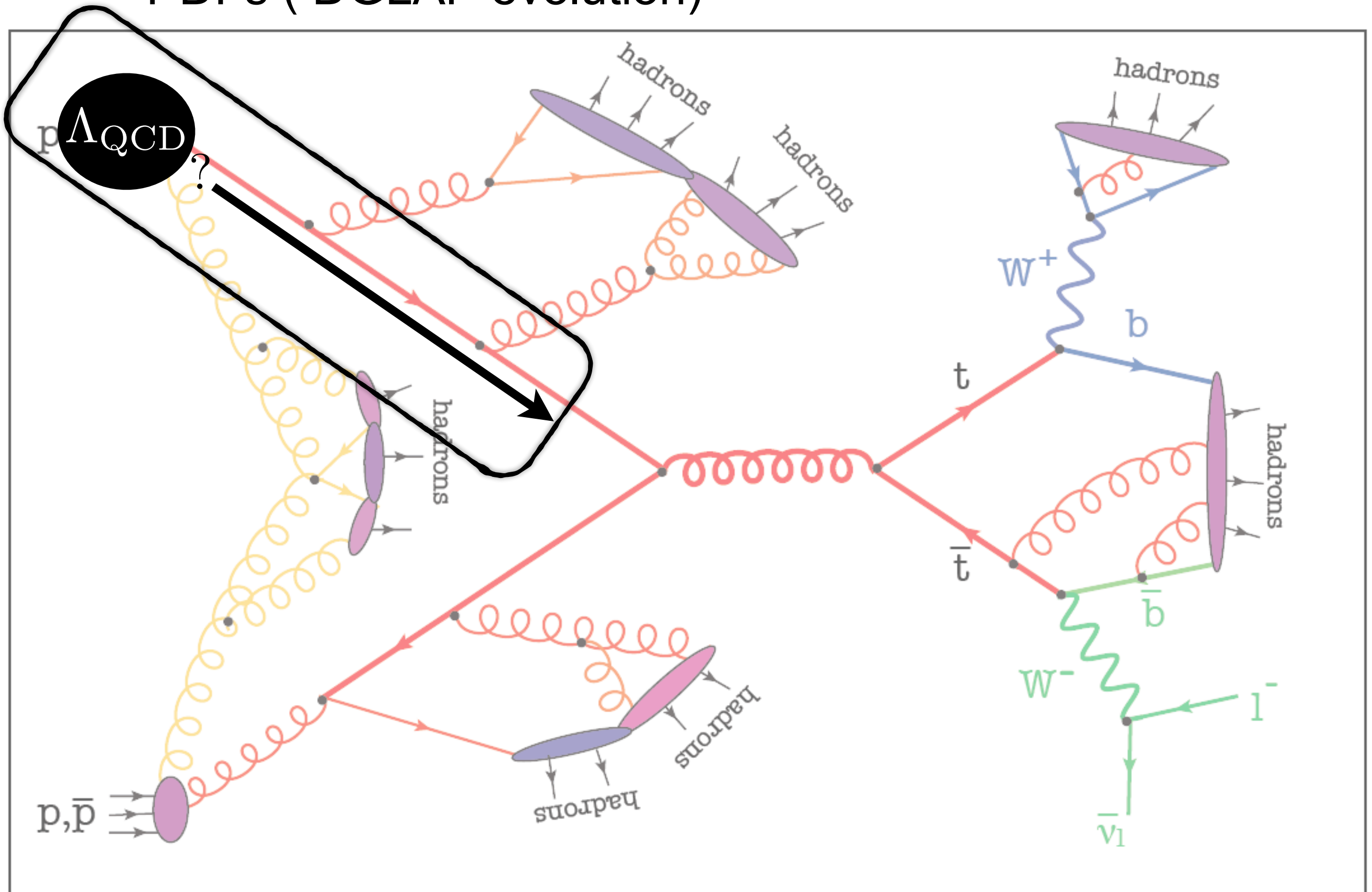
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- Introduction and motivations
- Cross-section measurements
  - Results from 7 TeV data and implications
  - Prospects for 13/14 TeV
- Production asymmetry measurements
  - Results from 7 TeV (& new SM predictions)
  - Prospects for 13/14 TeV



Drawing by Keith Hamilton

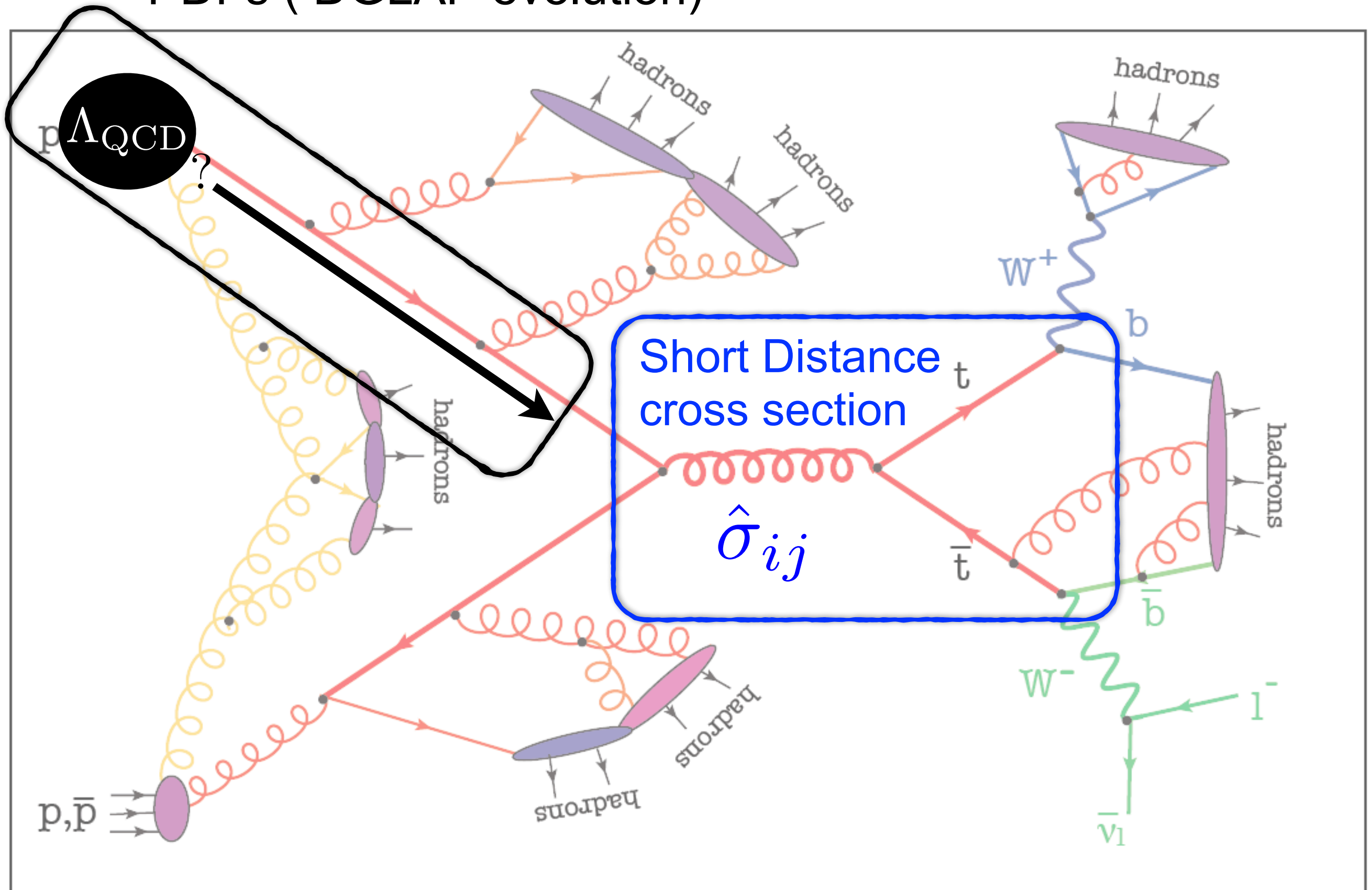
# PDFs ( DGLAP evolution)



Drawing by Keith Hamilton



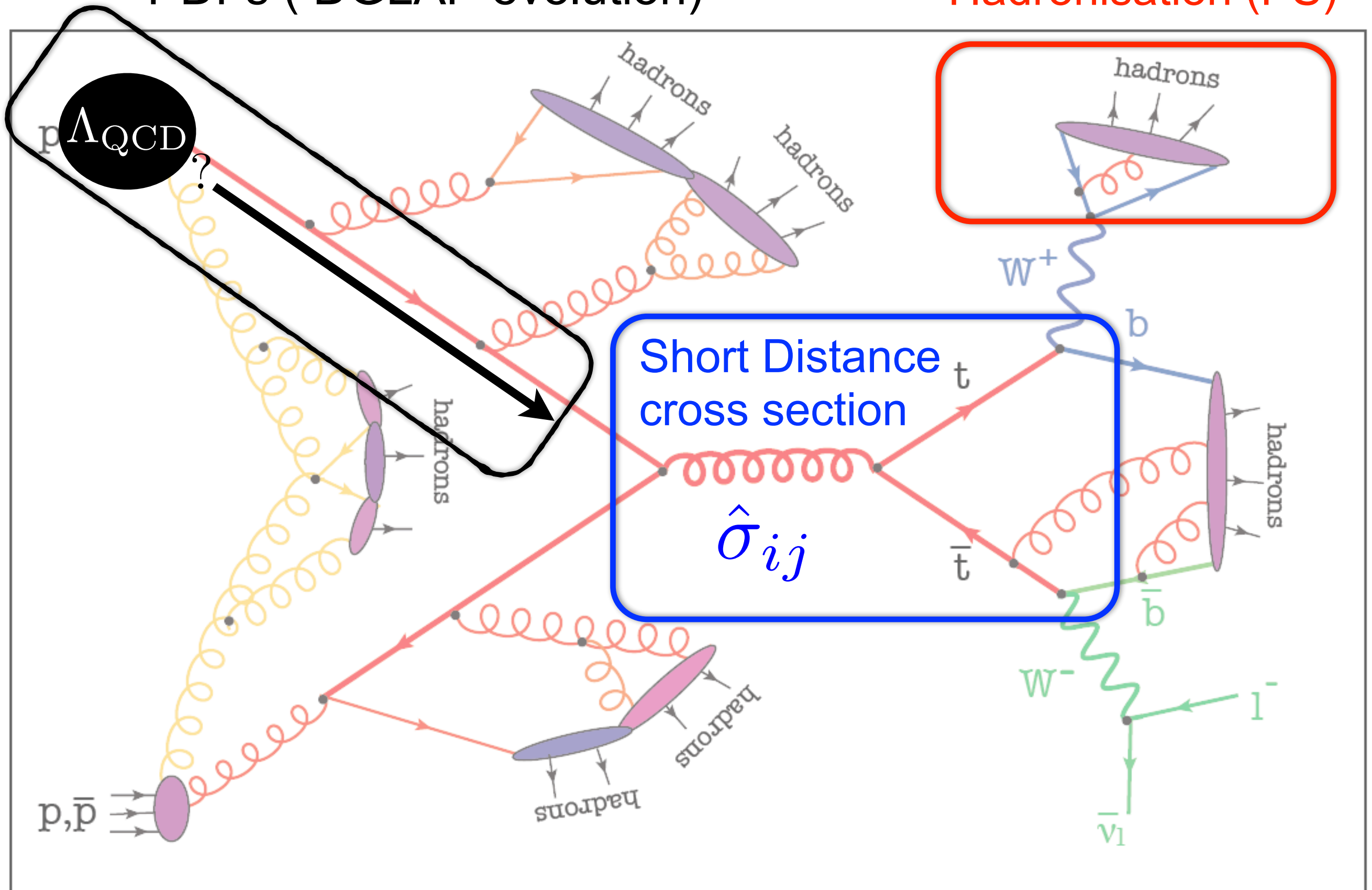
# PDFs ( DGLAP evolution)



Drawing by Keith Hamilton

PDFs ( DGLAP evolution)

Hadronisation (PS)



Drawing by Keith Hamilton

# How to compare with LHC data

$$\sigma_{P_A P_B \rightarrow Q \bar{Q} X} = \sum_{a,b} \int dx_a dx_b f_{a/A}(x_a, \mu_F^2) f_{b/B}(x_b, \mu_F^2) d\hat{\sigma}_{ab \rightarrow Q \bar{Q} X}(\hat{s}, \mu_F^2, \mu_R^2, \alpha_s(\mu_R^2)) \\ + \mathcal{O}\left(\frac{Q^2}{\Lambda_{\text{QCD}}^2}\right)$$

# How to compare with LHC data

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Process **dependent** short-distance cross-section

NLO inclusive P. Nason, S. Dawson, and R. K. Ellis, 1988

NLO differential: P. Nason, S. Dawson, and R. K. Ellis, 1989

NLO interfaced with PS: S. Frixione, P. Nason, and B. R. Webber/(G. Ridolfi), 2003/(2007)

NNLO inclusive: M. Czakon, P. Fiedler, and A. Mitov, 2013

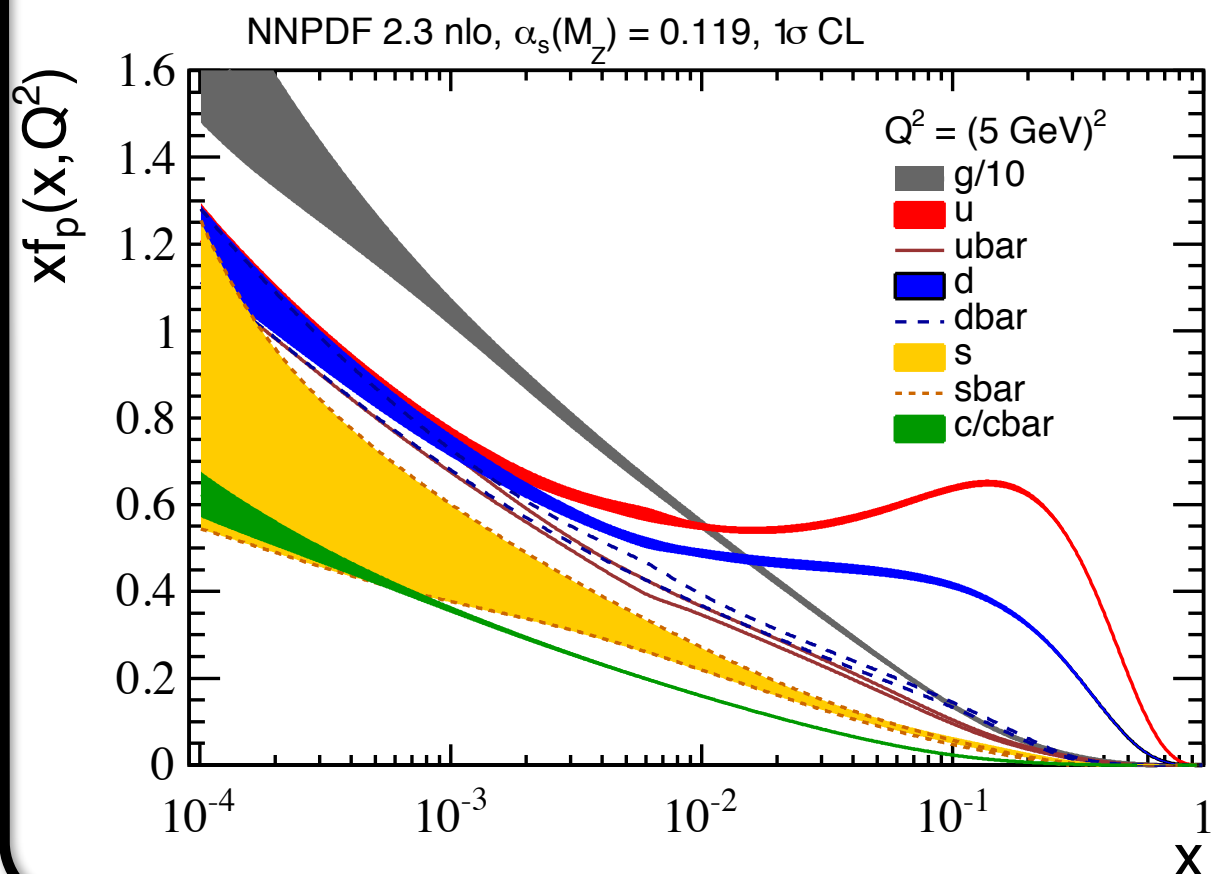
NNLO differential: M. Czakon, P. Fiedler, and A. Mitov, 2014

- +Exhaustive list of resummation calculations
- +Electroweak corrections
- +NLO decay

# How to compare with LHC data

$$\sigma_{P_A P_B \rightarrow Q \bar{Q} X} = \sum_{a,b} \int dx_a dx_b f_{a/A}(x_a, \mu_F^2) f_{b/B}(x_b, \mu_F^2) d\hat{\sigma}_{ab \rightarrow Q \bar{Q} X}(\hat{s}, \mu_F^2, \mu_R^2, \alpha_s(\mu_R^2)) + \mathcal{O}\left(\frac{Q^2}{\Lambda_{\text{QCD}}^2}\right)$$

## Process independent PDFs



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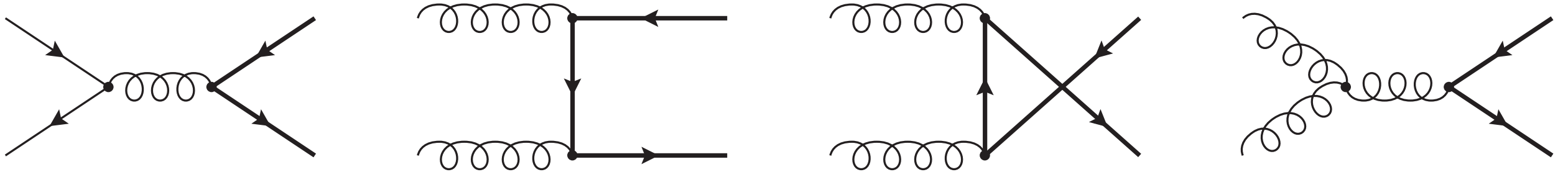
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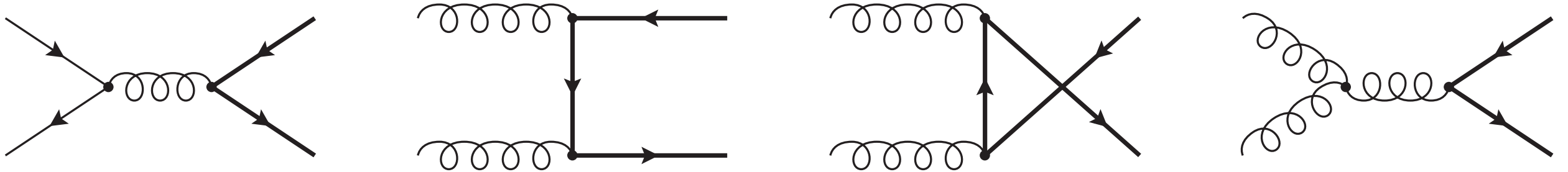
- +Exhaustive list of resummation calculations
- +Electroweak corrections
- +NLO decay

# Theoretical uncertainty, $pp \rightarrow Q_3 \bar{Q}_4 + X$



$$\hat{\sigma}_{ij}(\hat{s}, m_Q^2, \mu_F^2) = \frac{\alpha_s^2(\mu_R)}{m_Q^2} \left( \kappa_{ij}^{(0)} + \alpha_s(\mu_R) \kappa_{ij}^{(1)}(\mu_R) + \dots \right)$$

# Theoretical uncertainty, $pp \rightarrow Q_3 \bar{Q}_4 + X$

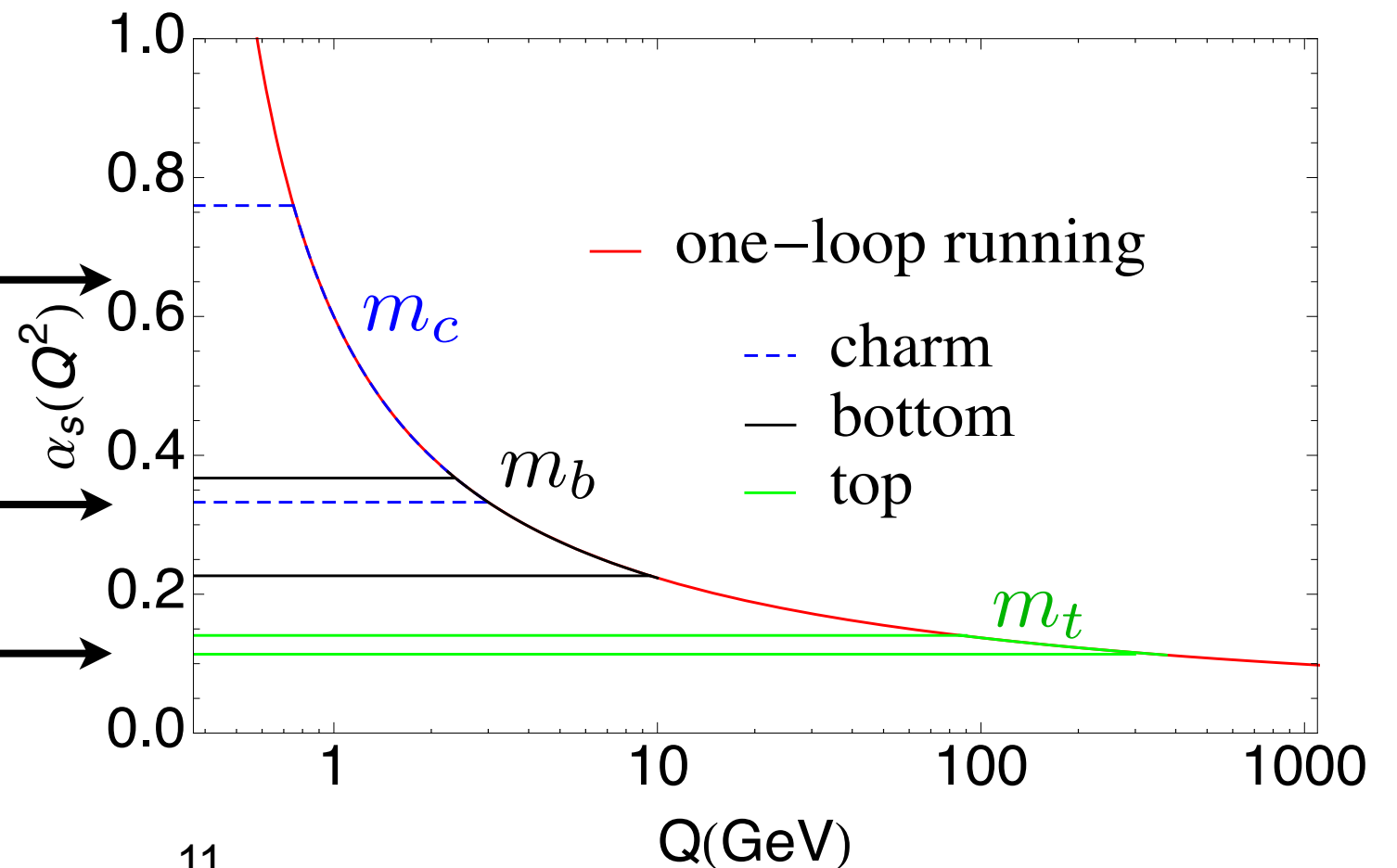


$$\hat{\sigma}_{ij}(\hat{s}, m_Q^2, \mu_F^2) = \frac{\alpha_s^2(\mu_R)}{m_Q^2} \left( \kappa_{ij}^{(0)} + \alpha_s(\mu_R) \kappa_{ij}^{(1)}(\mu_R) + \dots \right)$$

$$\delta\alpha_s(0.5 m_c, 2 m_c) = {}^{+170\%}_{-48\%}$$

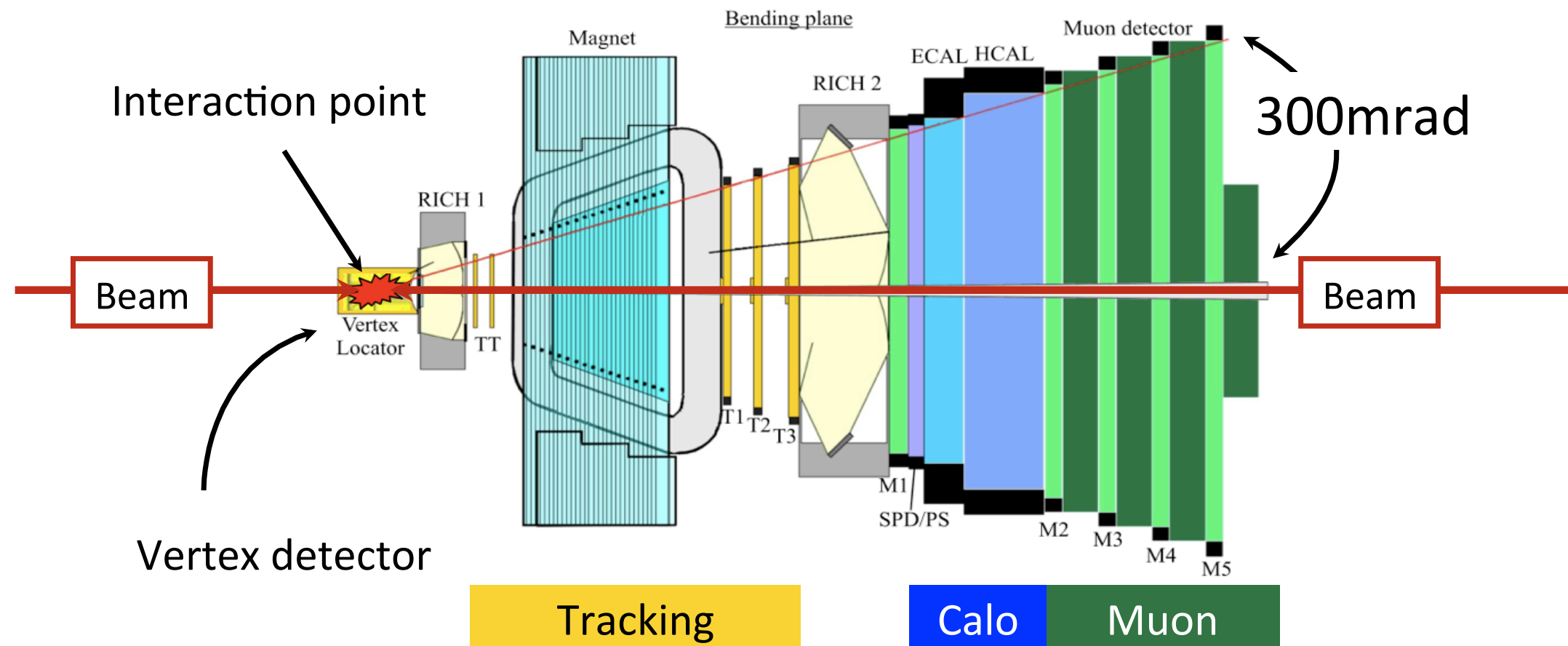
$$\delta\alpha_s(0.5 m_b, 2 m_b) = {}^{+72\%}_{-34\%}$$

$$\delta\alpha_s(0.5 m_t, 2 m_t) = {}^{+25\%}_{-19\%}$$

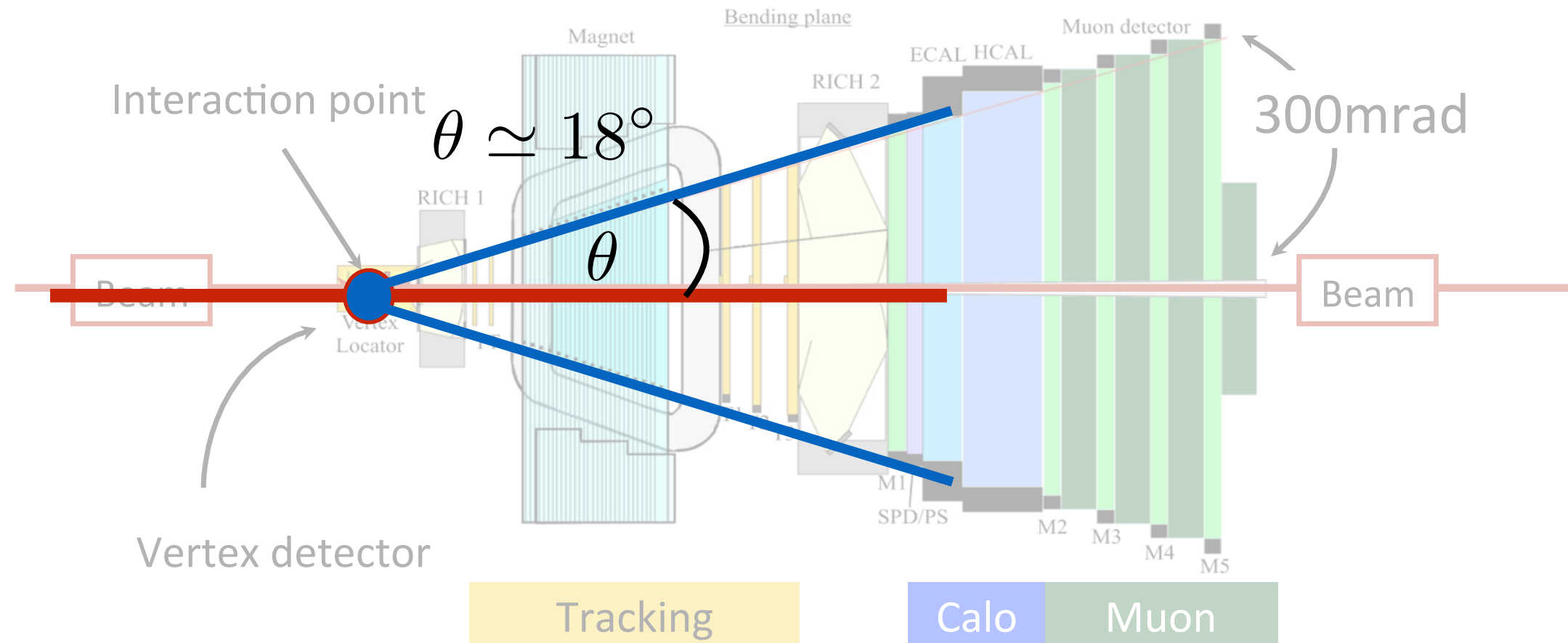




# The LHCb detector and data

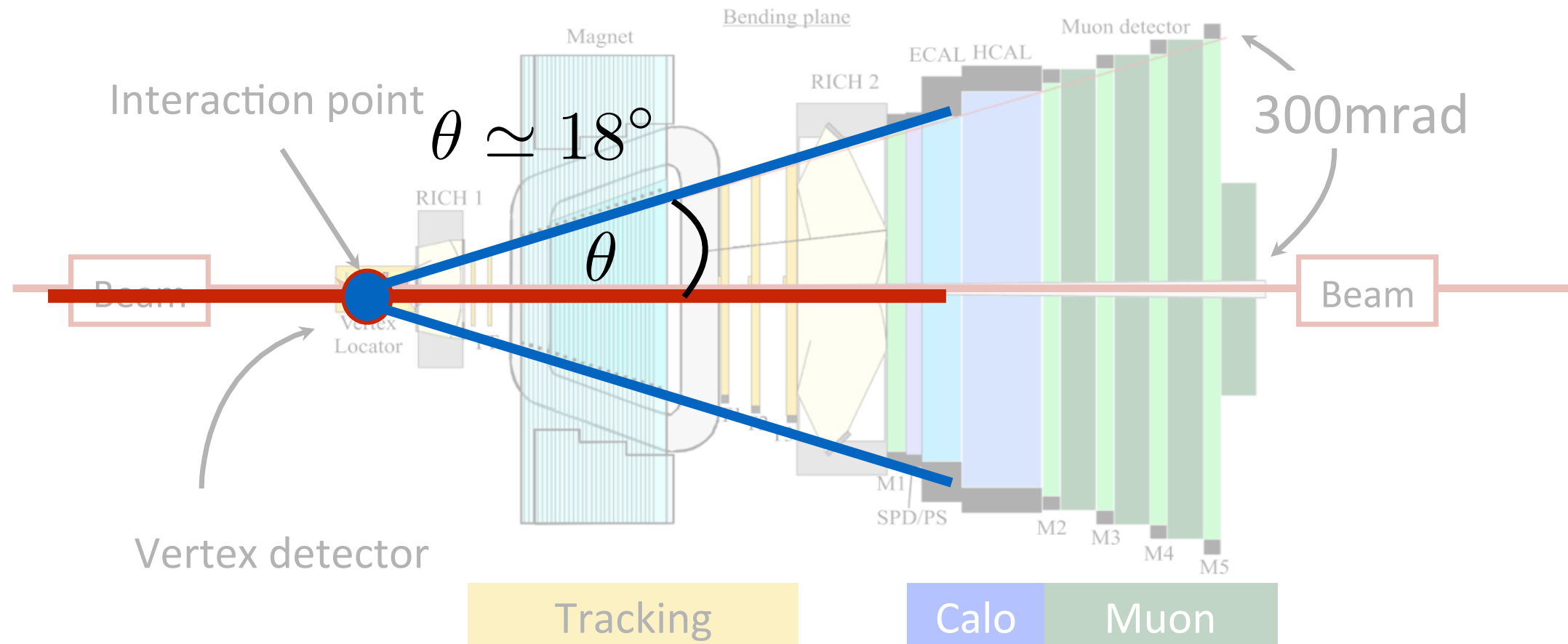


# The LHCb detector and data



LHCb - forward acceptance:  $\eta \in [2.0, 4.5]$

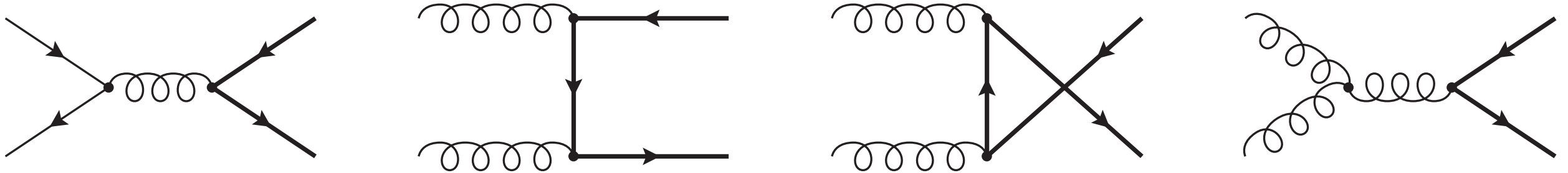
# The LHCb detector and data



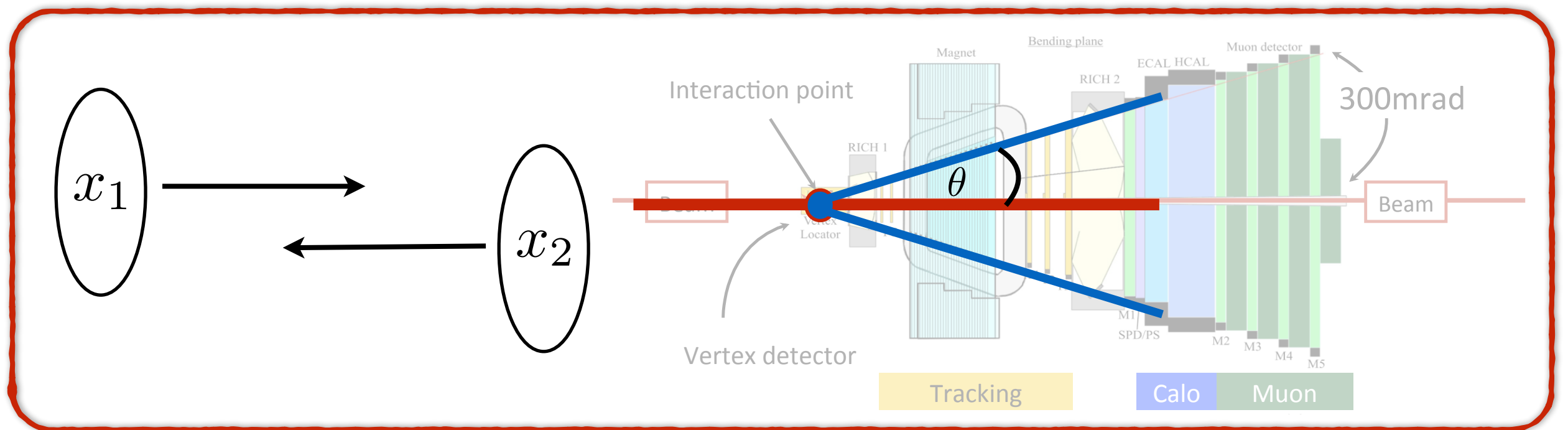
LHCb - forward acceptance:  $\eta \in [2.0, 4.5]$

Data (ifb)	7 TeV	8 TeV	13 TeV	14 TeV (2030)
ATLAS/CMS	5	20	100	3000?
LHCb	<b>1</b>	<b>2</b>	<b>~5</b>	<b>~50</b>

# Why study forward $pp \rightarrow Q_3 \bar{Q}_4 + X$ ?

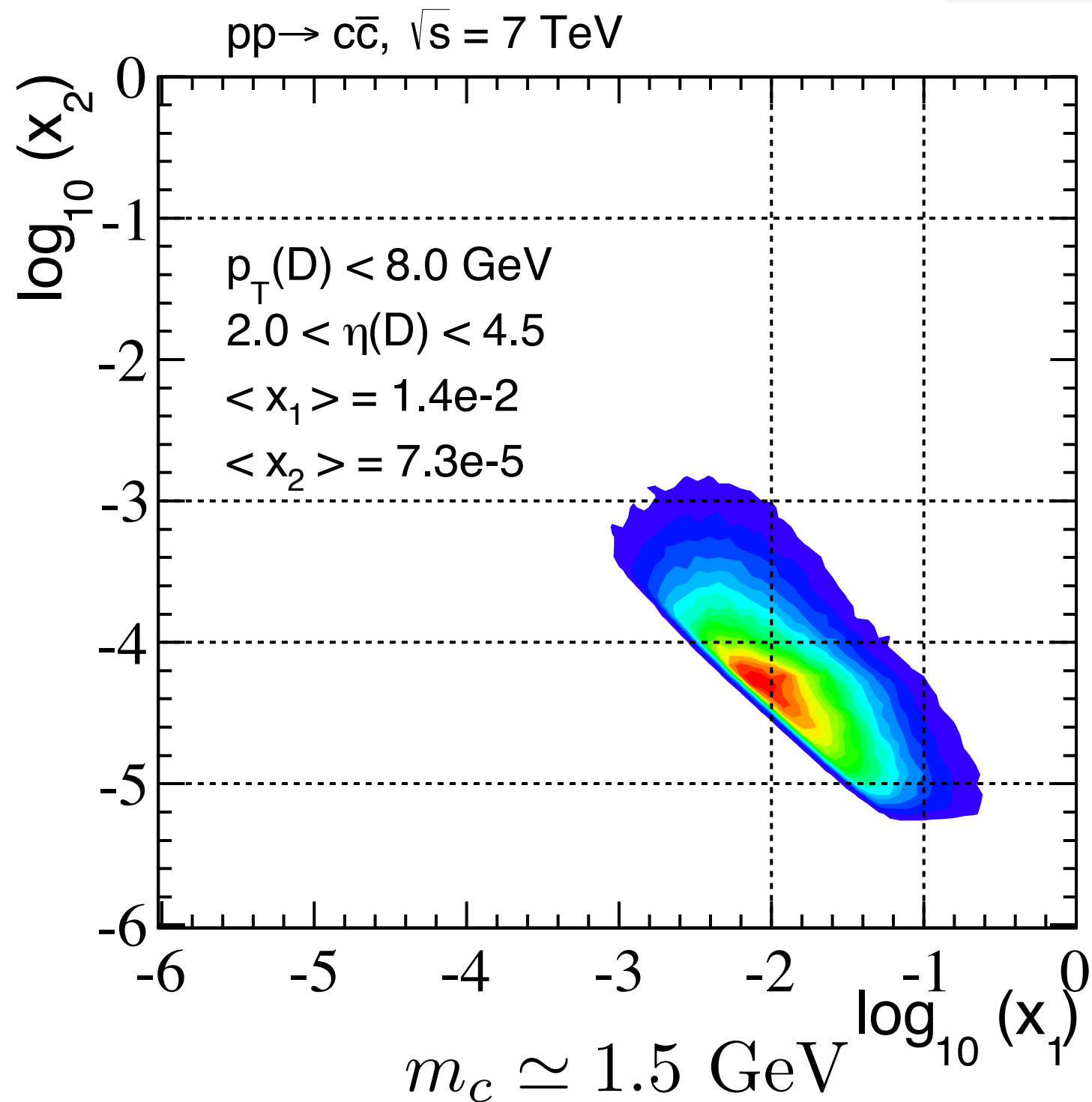


$$x_{1,(2)} = \frac{m_T}{\sqrt{\hat{s}}} (e^{(-)} y_3 + e^{(-)} y_4)$$



$$pp \rightarrow c\bar{c}$$

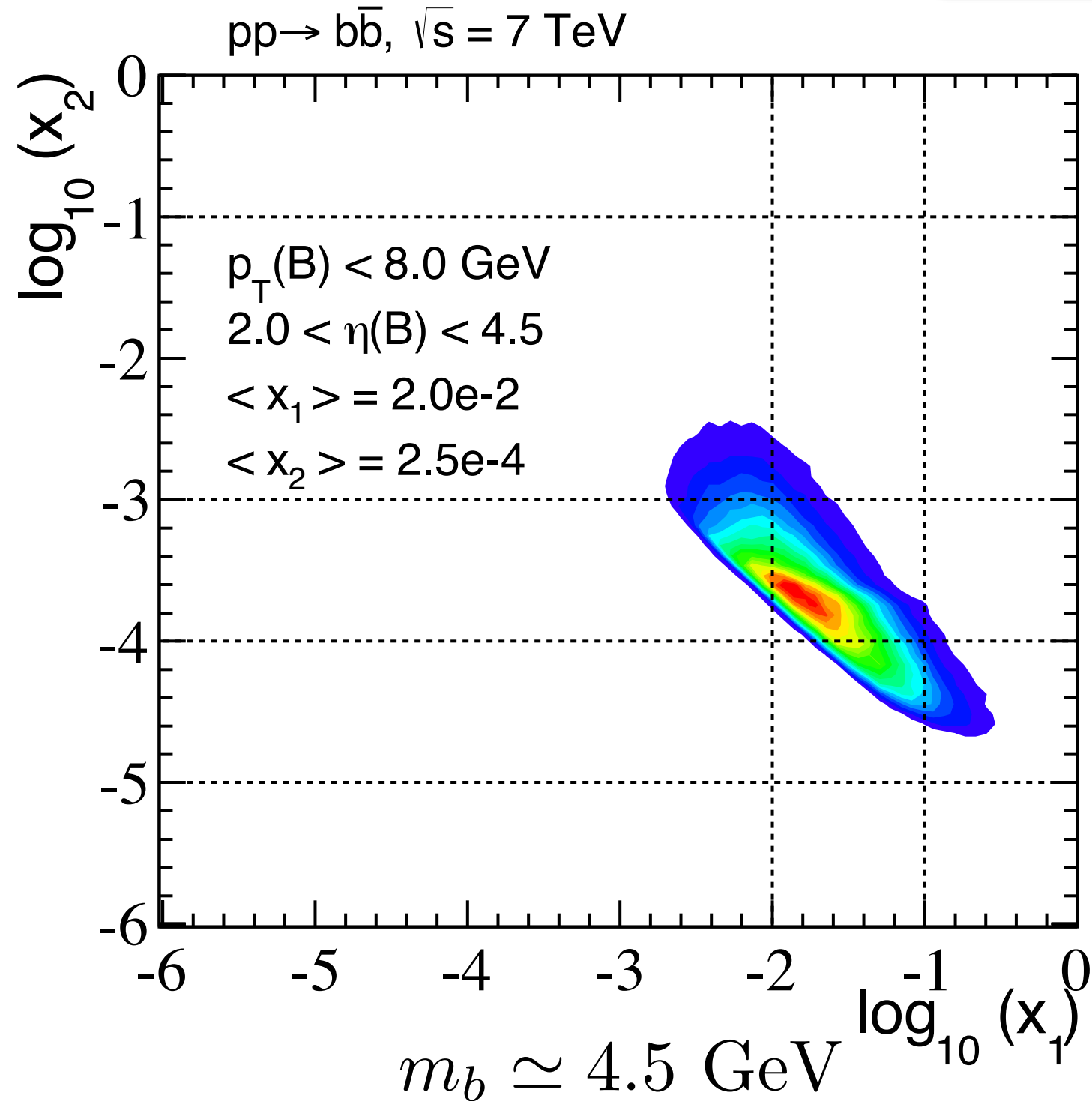
$$x_{1,(2)} = \frac{m_T}{\sqrt{\hat{s}}} (e^{(-)y_3} + e^{(-)y_4})$$



LHCb measurement arXiv: 1302.2864

$$pp \rightarrow b\bar{b}$$

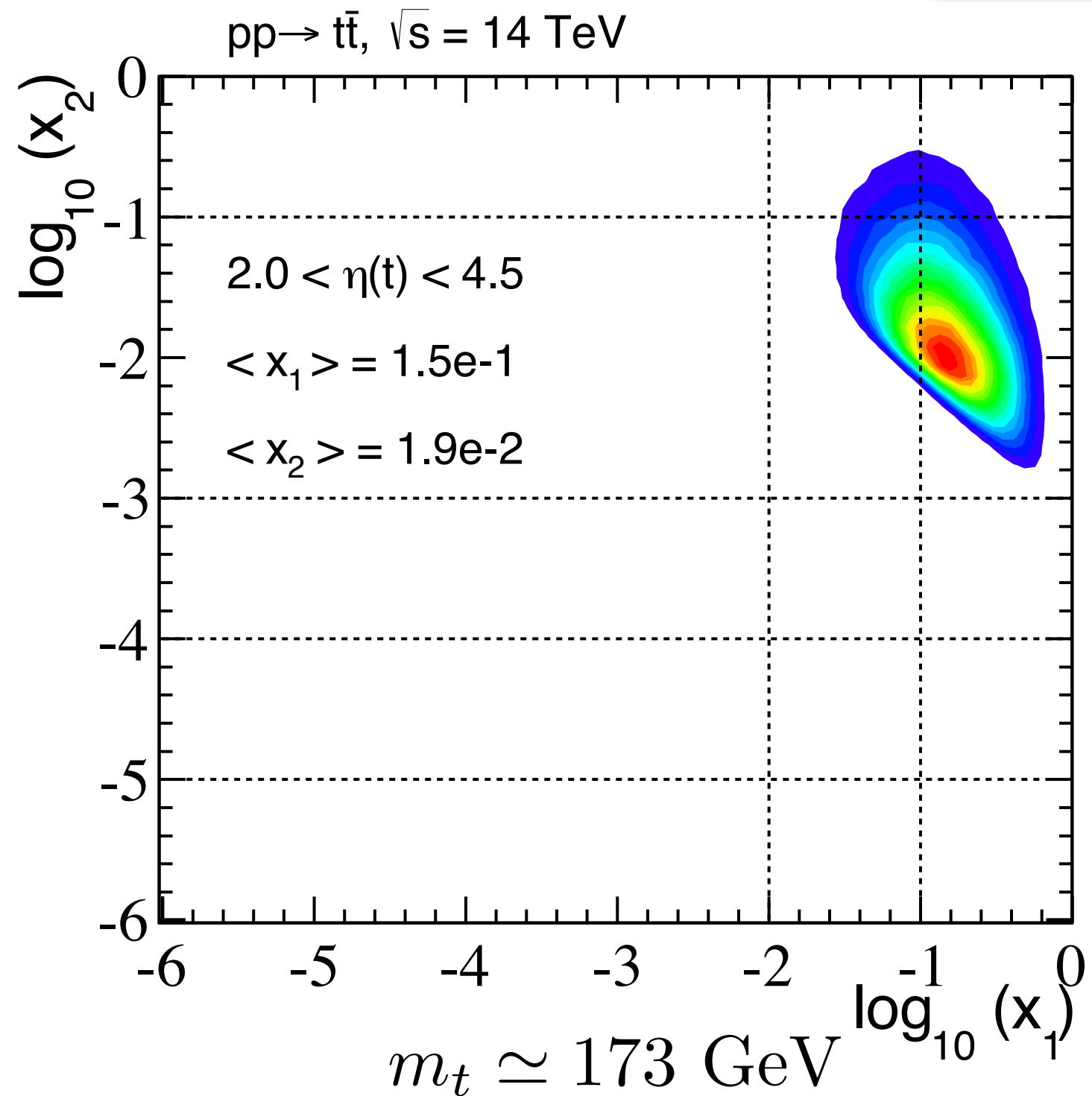
$$x_{1,(2)} = \frac{m_T}{\sqrt{\hat{s}}} (e^{(-)y_3} + e^{(-)y_4})$$



LHCb measurement arXiv: 1306.3663

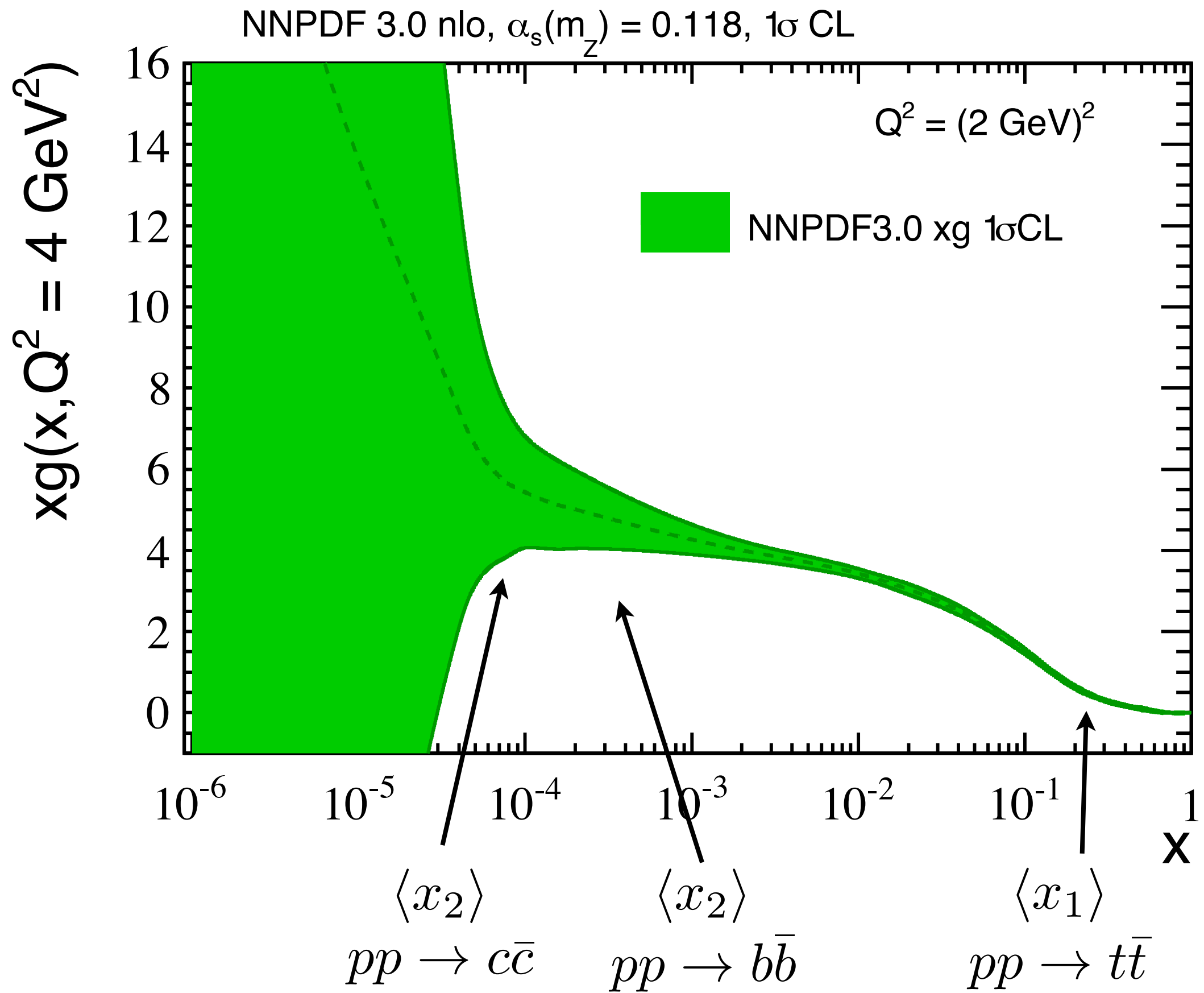
$$pp \rightarrow t\bar{t}$$

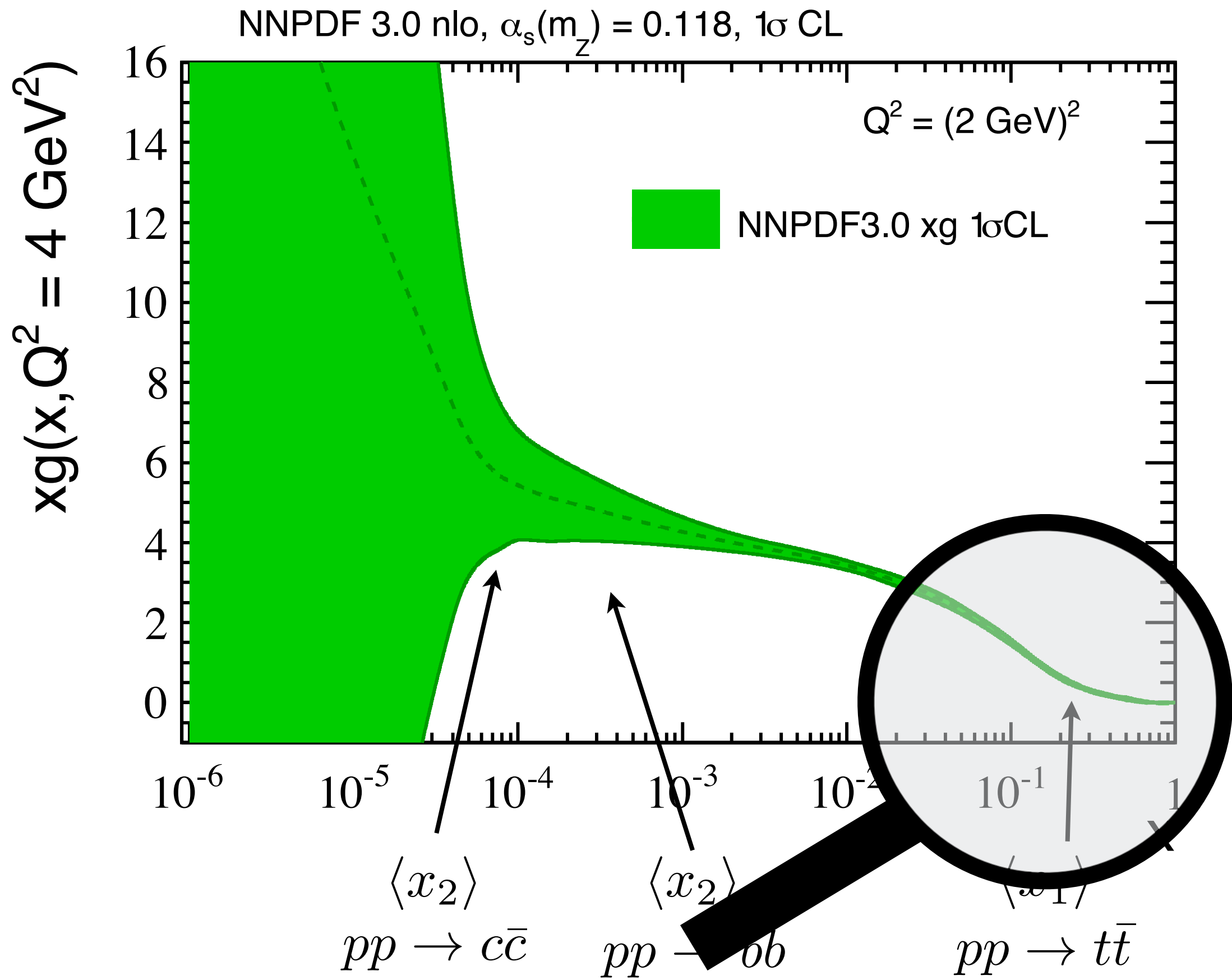
$$x_{1,(2)} = \frac{m_T}{\sqrt{\hat{s}}} (e^{(-)y_3} + e^{(-)y_4})$$

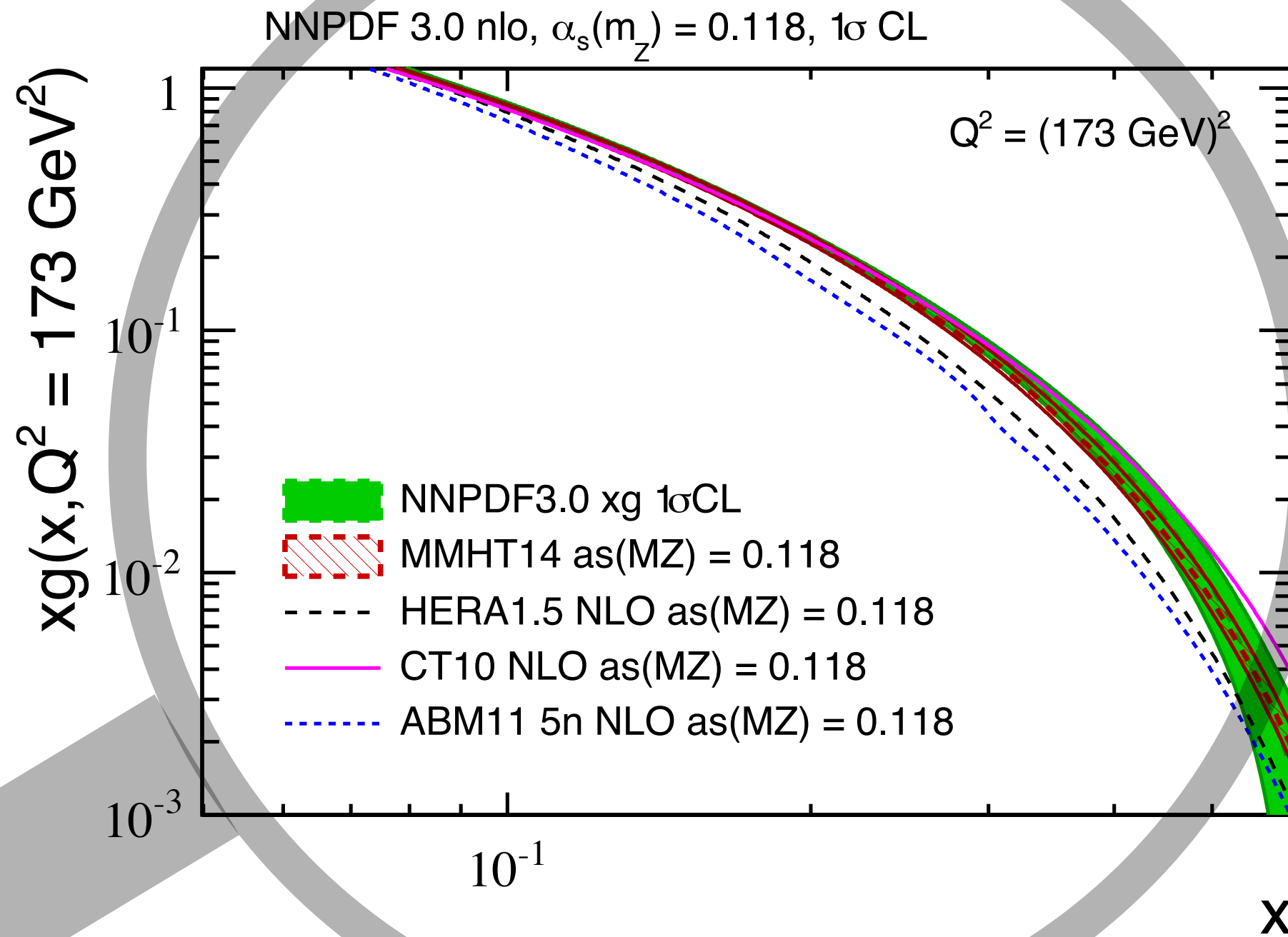


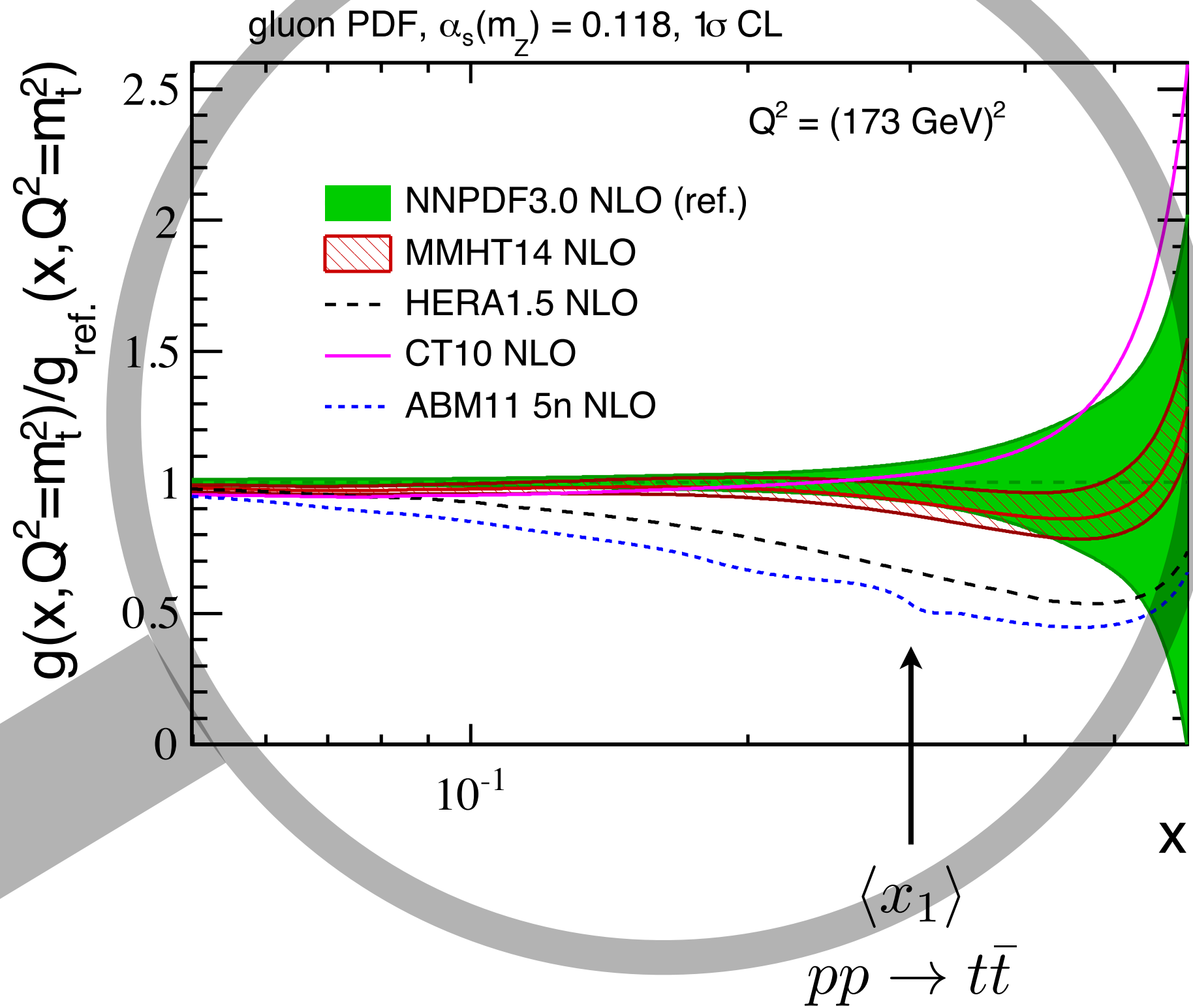
LHCb measurement arXiv: 15??..????











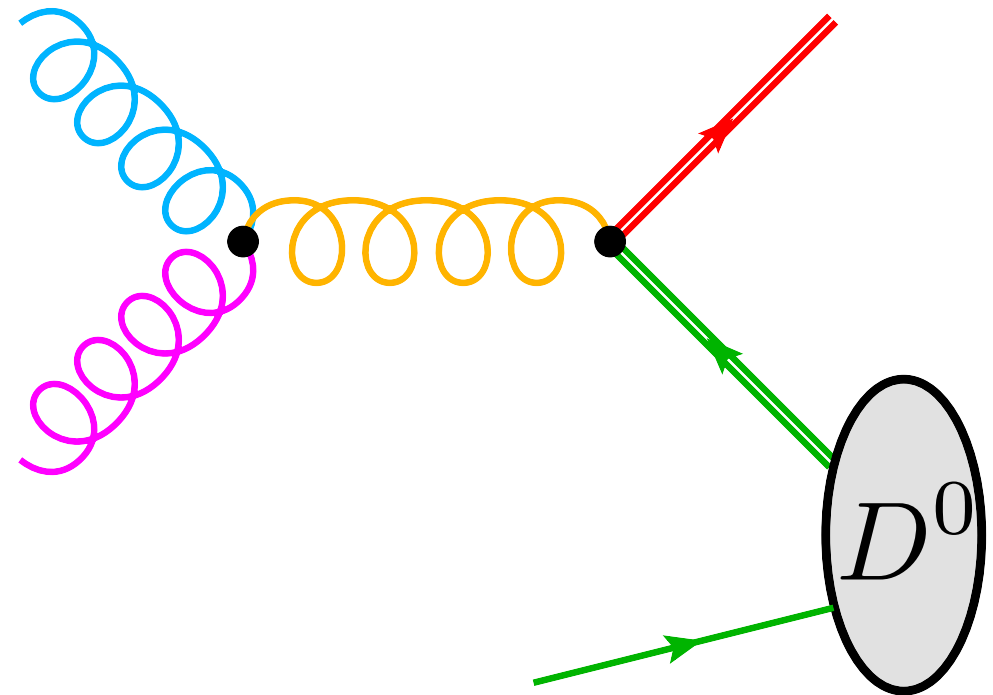
# Cross-section measurements

# D measurement (arXiv: 1302.2864)

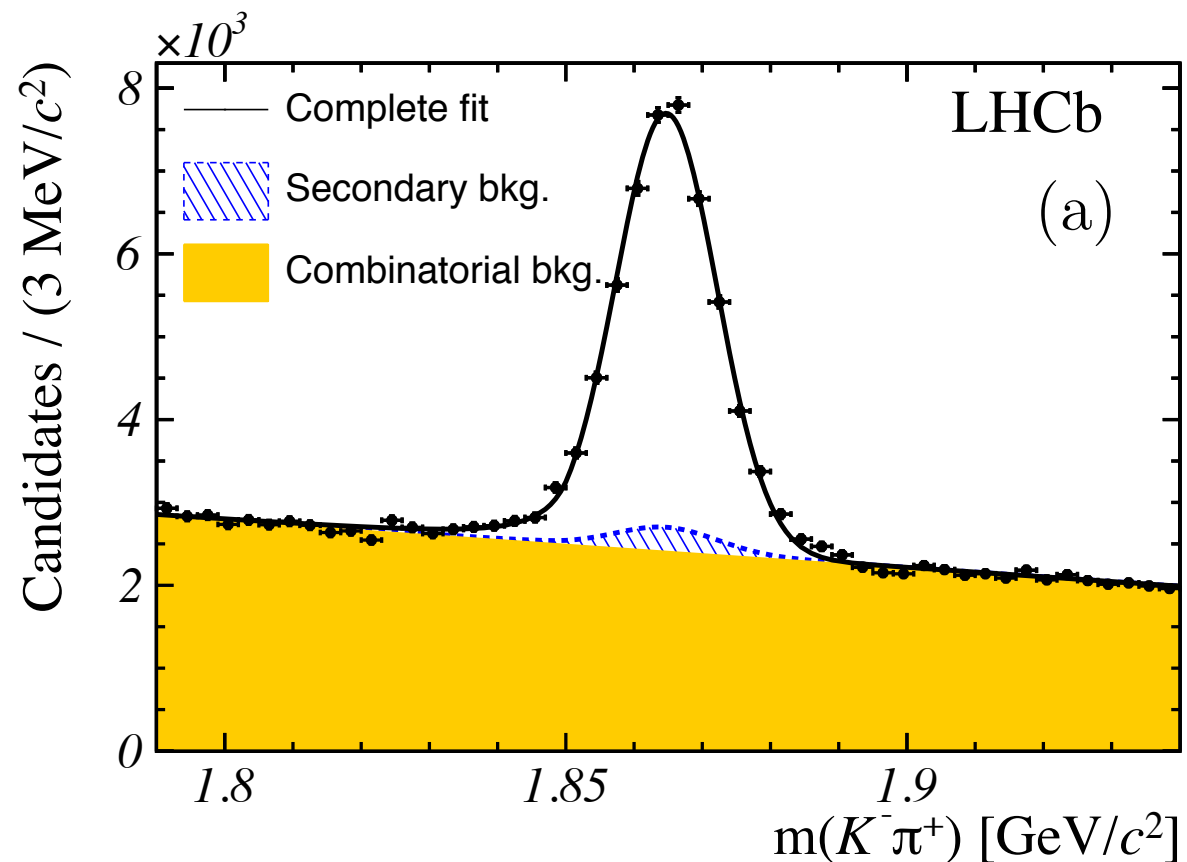
$$pp \rightarrow D + X$$

$$2.0 < y_D < 4.5$$

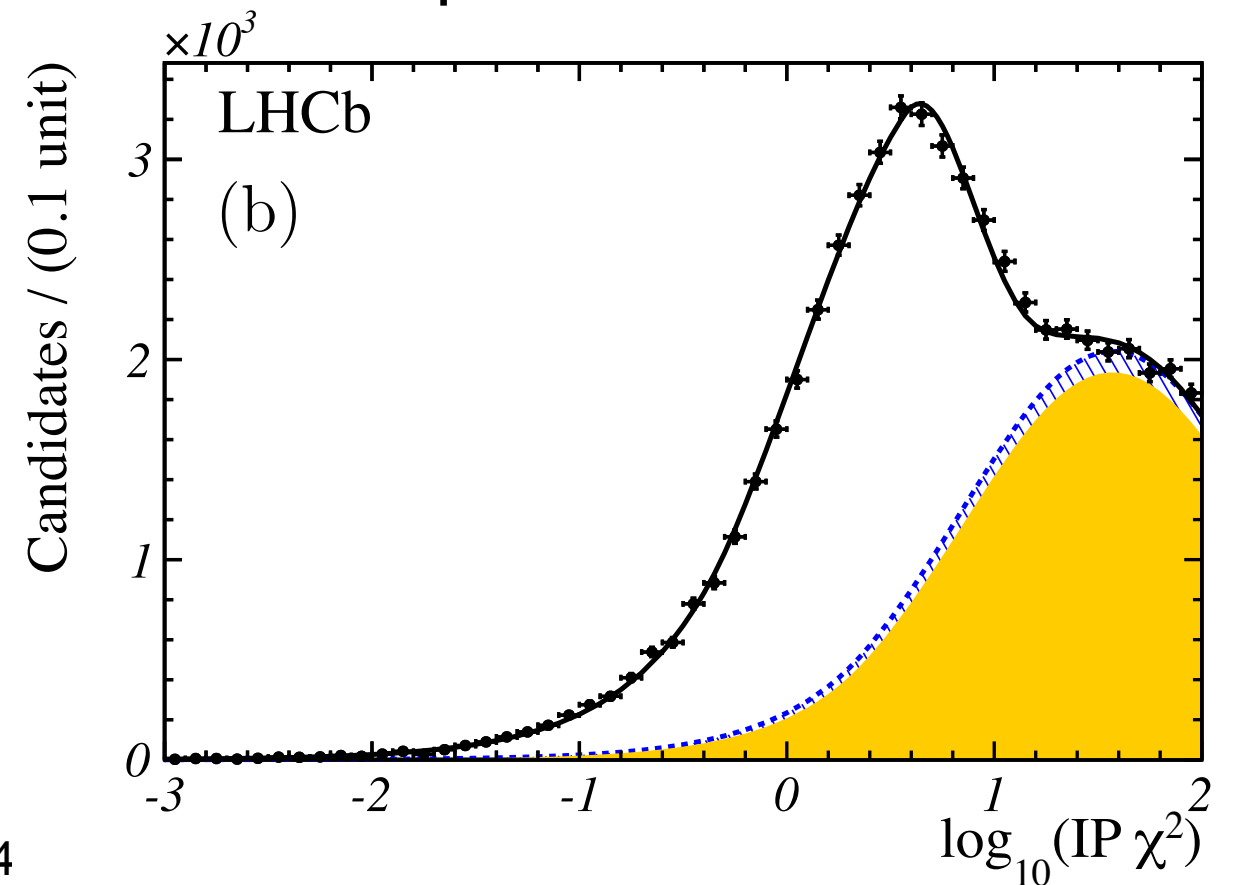
$$D p_T < 8.0 \text{ GeV}$$



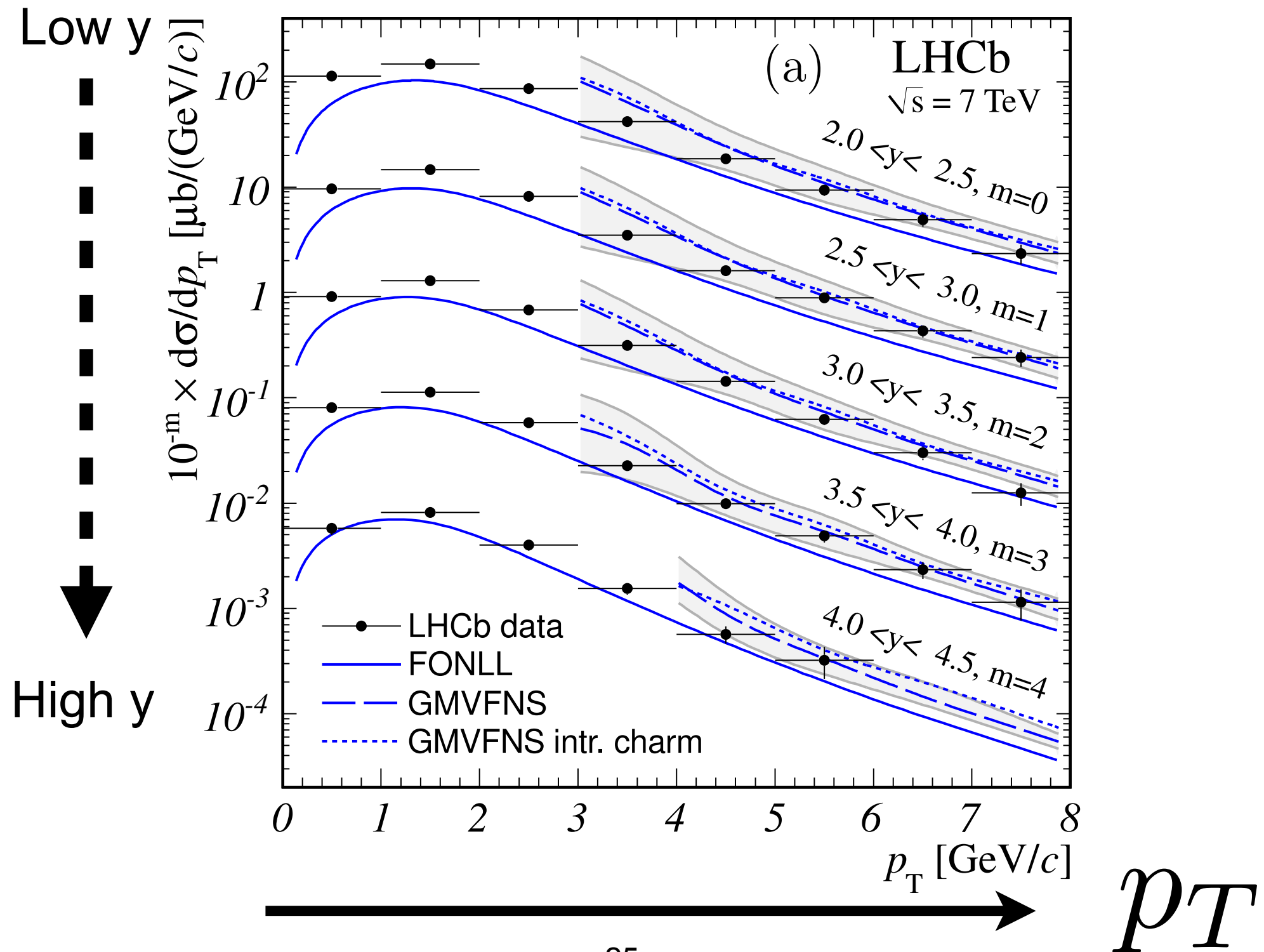
## Mass requirement



## Displaced vertex



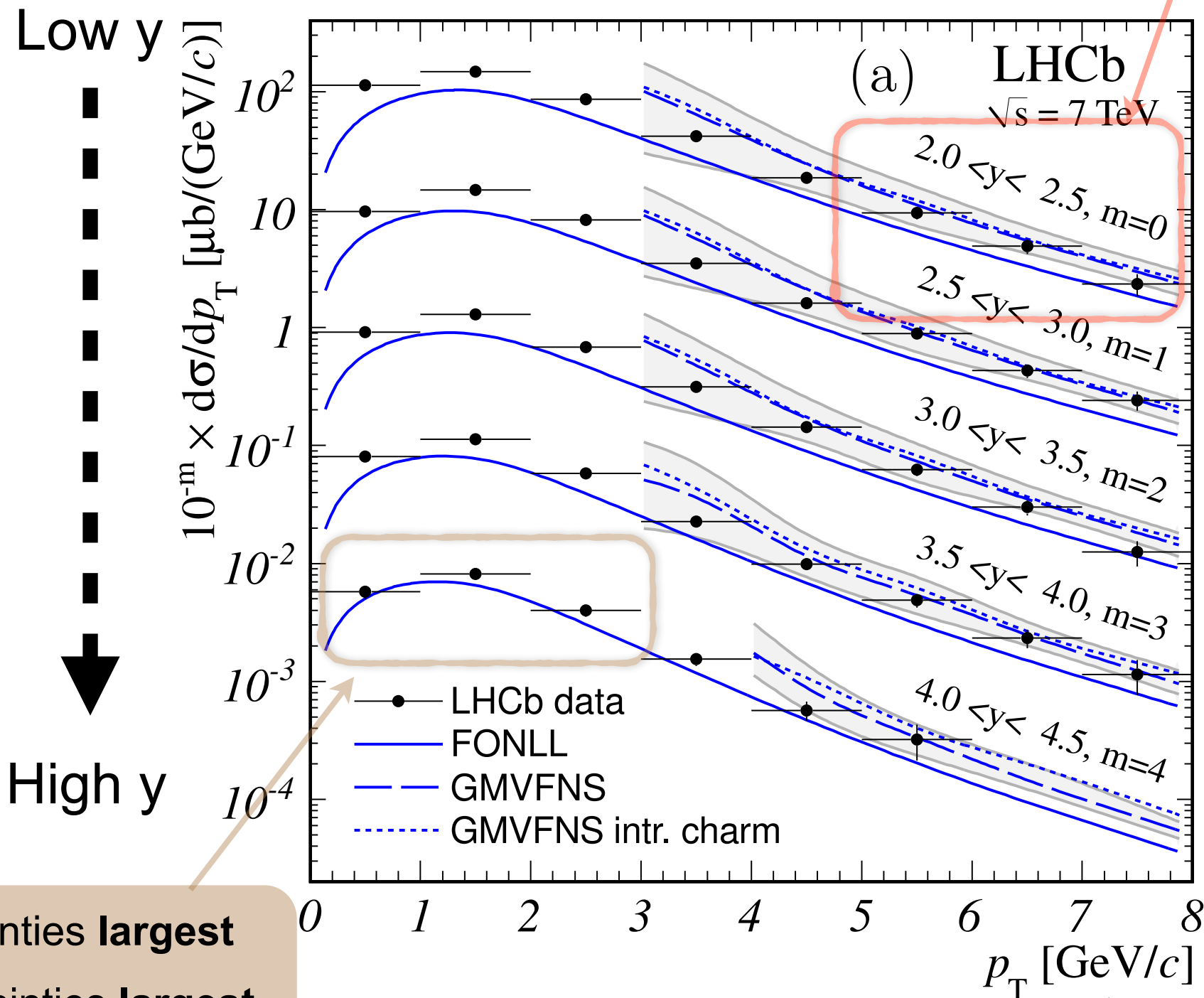
# D measurement (arXiv: 1302.2864)





# D measurement (arXiv: 1302.2864)

PDF Uncertainties **smallest**  
Scale Uncertainties **smallest**

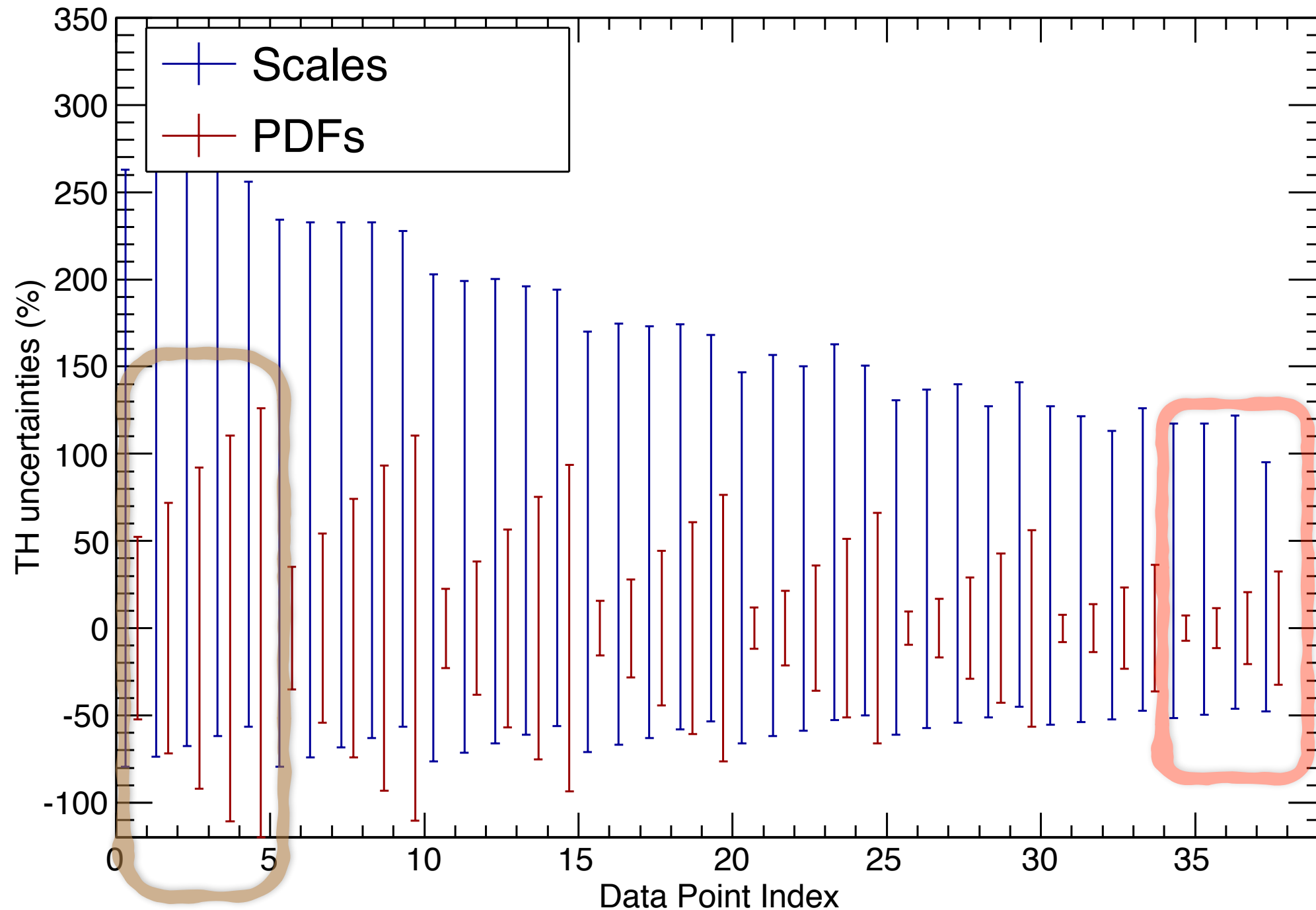


PDF Uncertainties **largest**  
Scale Uncertainties **largest**

$p_T$

# Impact of normalising the data

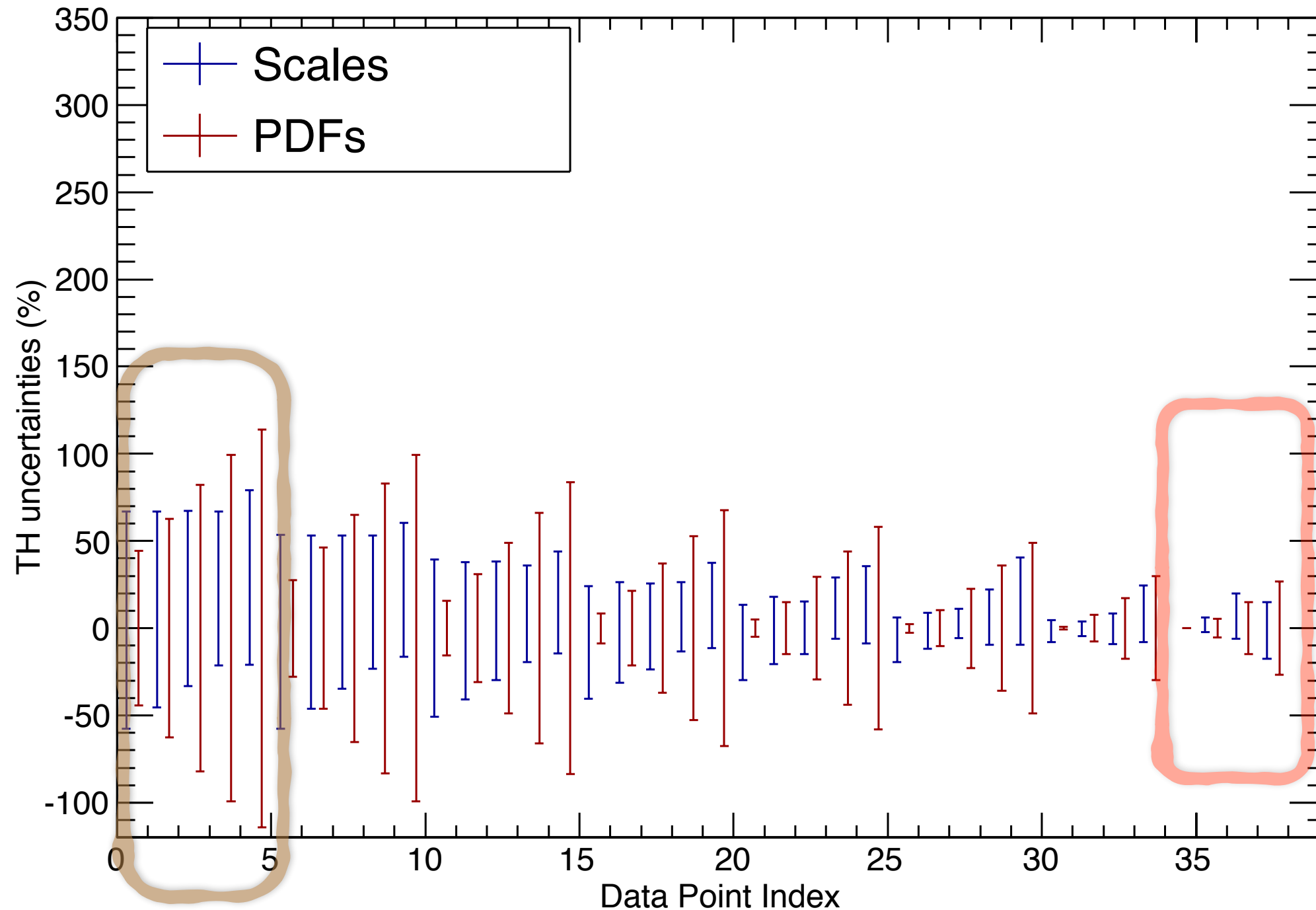
LHCb forward charm production, 7 TeV, D0 mesons, POWHEG



Differential fiducial cross section

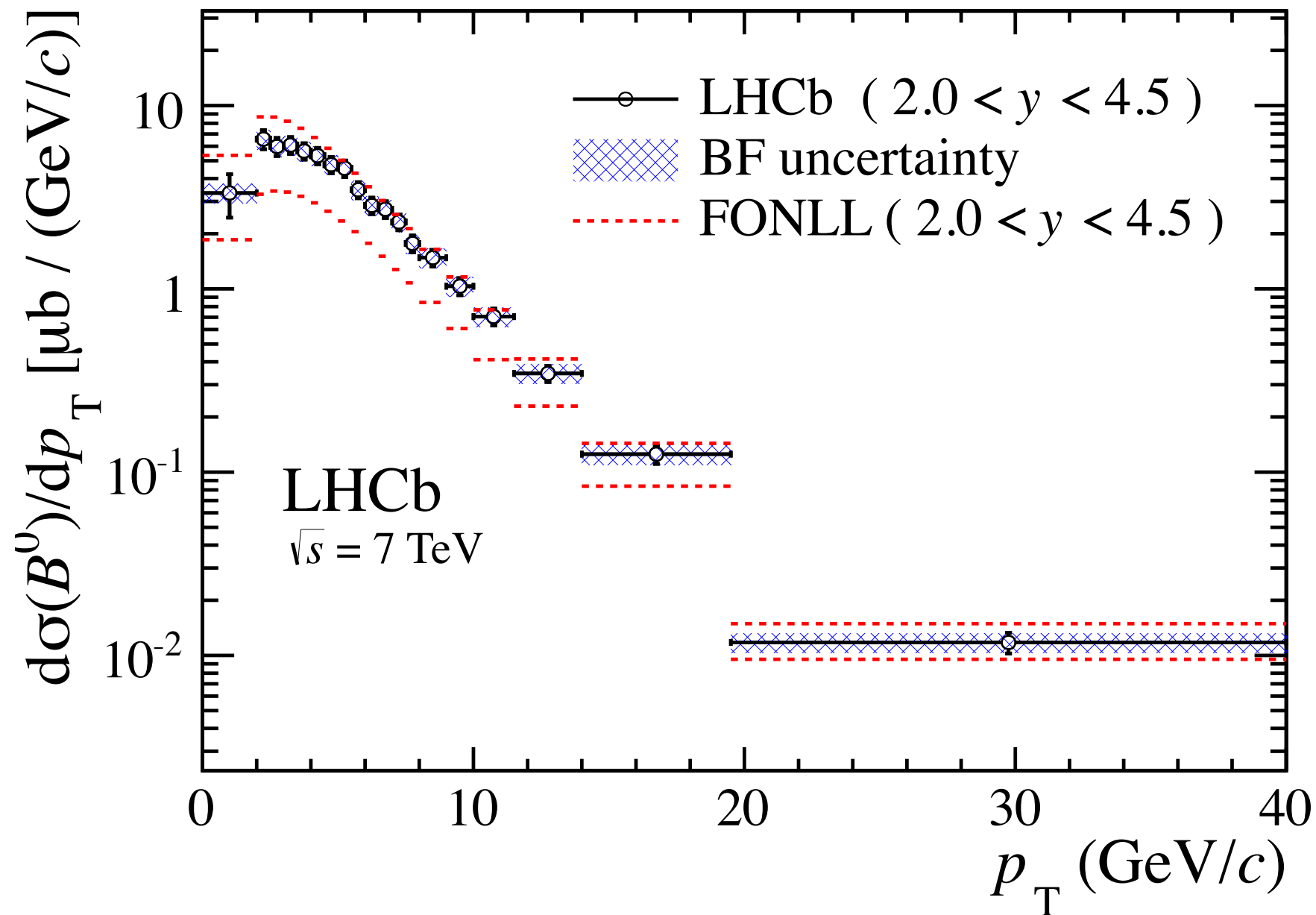
# Impact of normalising the data

LHCb forward charm production, 7 TeV, D0 mesons, POWHEG



Normalised differential fiducial cross section

# B measurement (arXiv: 1306.3663)



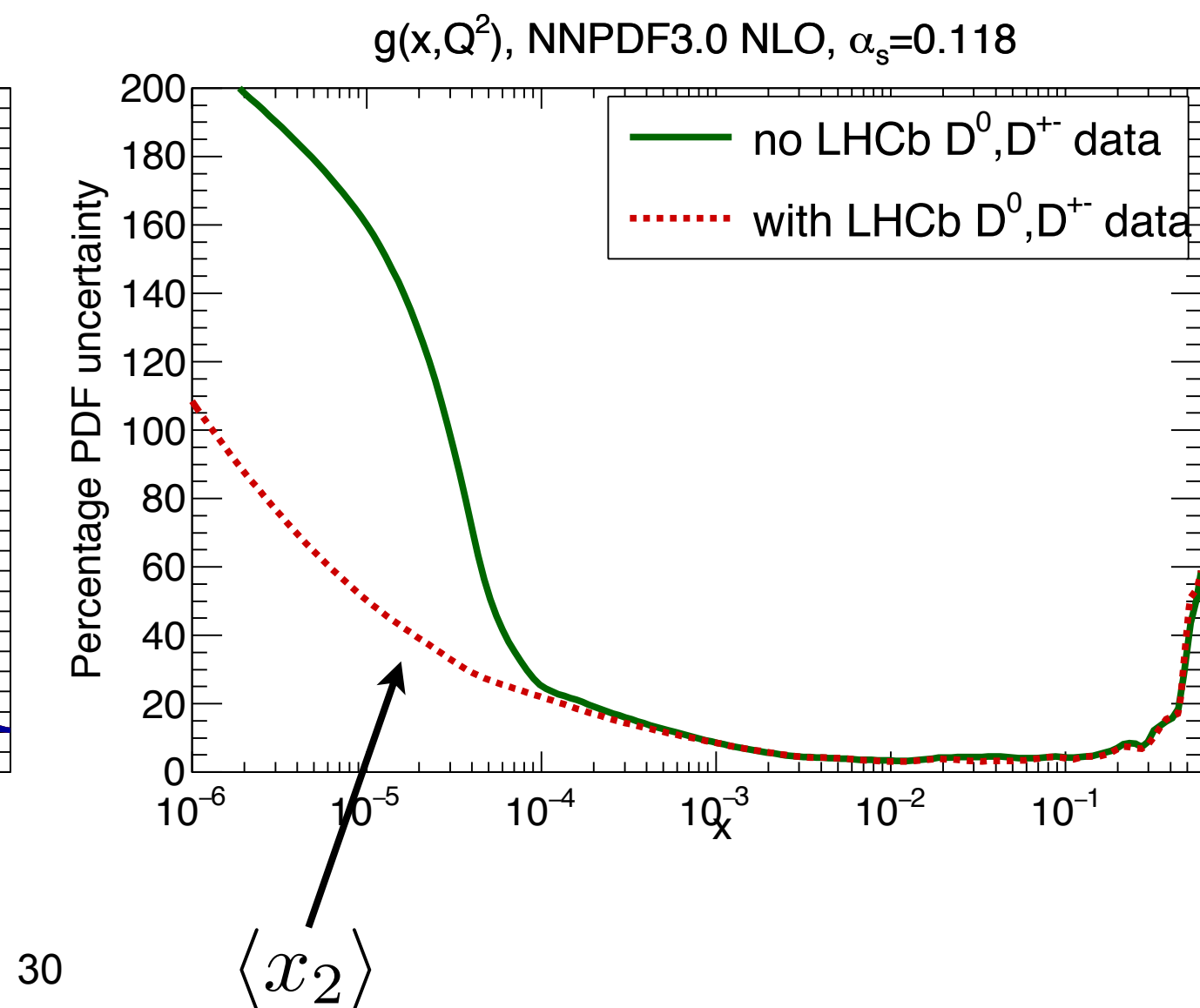
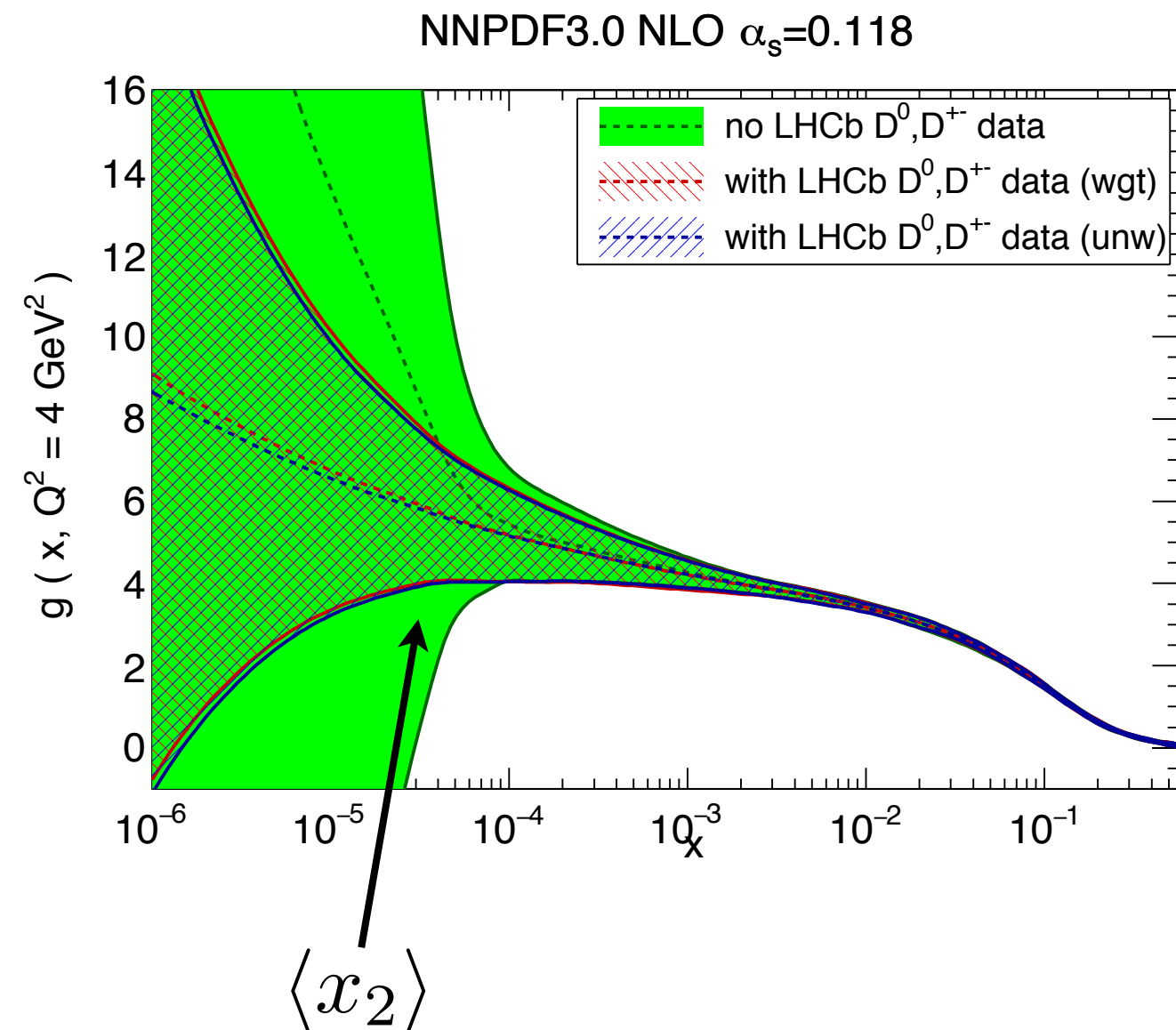
Theory + Data in agreement - within large theoretical uncertainties (scale)

Note, recent paper by PROSA collaboration arXiv: 1503.04581

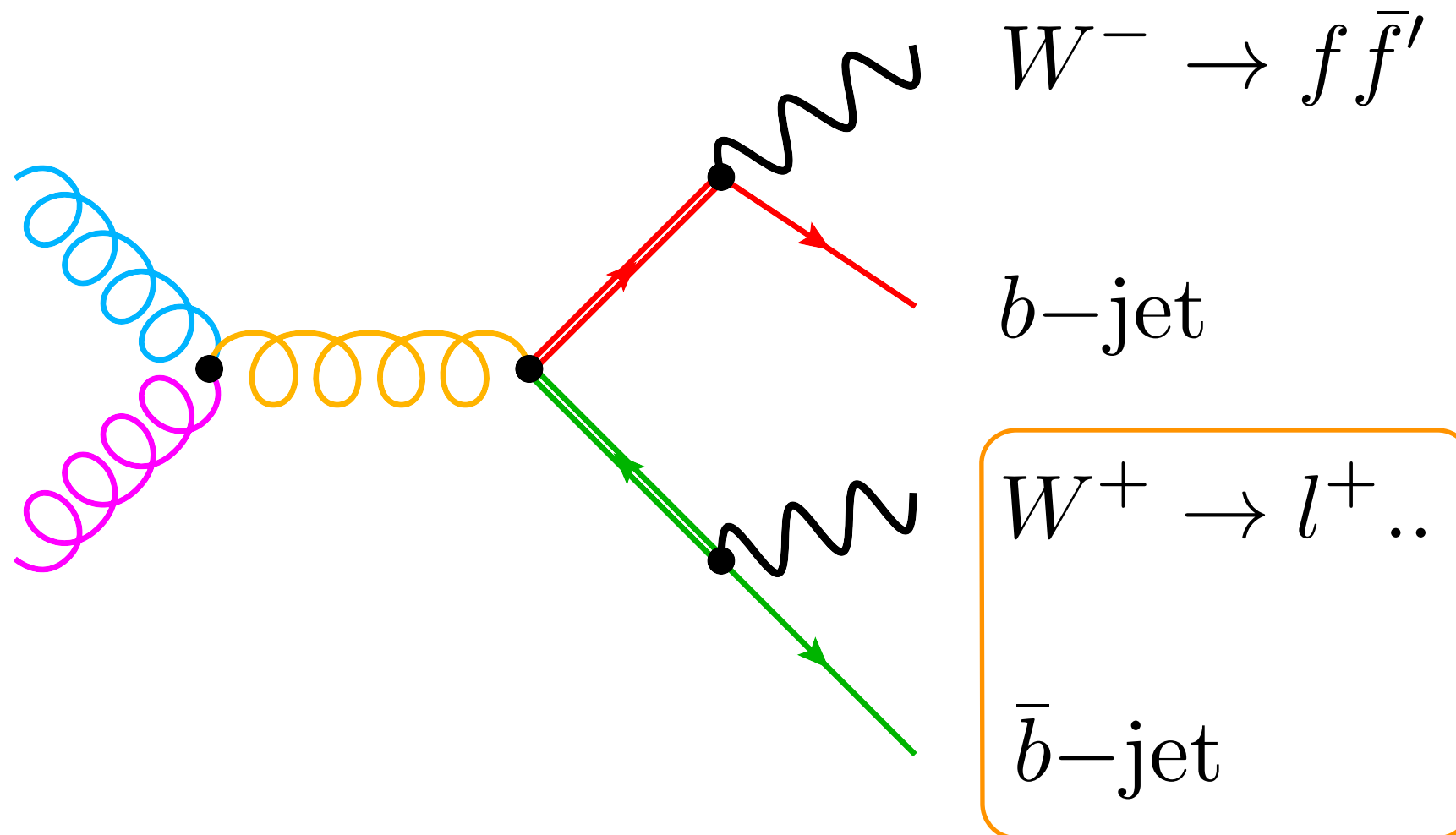
# Preliminary results, reweighting NNPDF3.0

Work in progress with J. Rojo, L. Rottoli, S. Sarkar, J. Talbert

- 1) Normalise LHCb differential charm data to **high-pt, low-y** bin
- 2) Reweight the 100 replicas based on compatibility with LHCb data (here we use the FONLL predictions obtained from public web interface)



# LHCb ~~tt~~ (arXiv: 15xx.xxxx?)



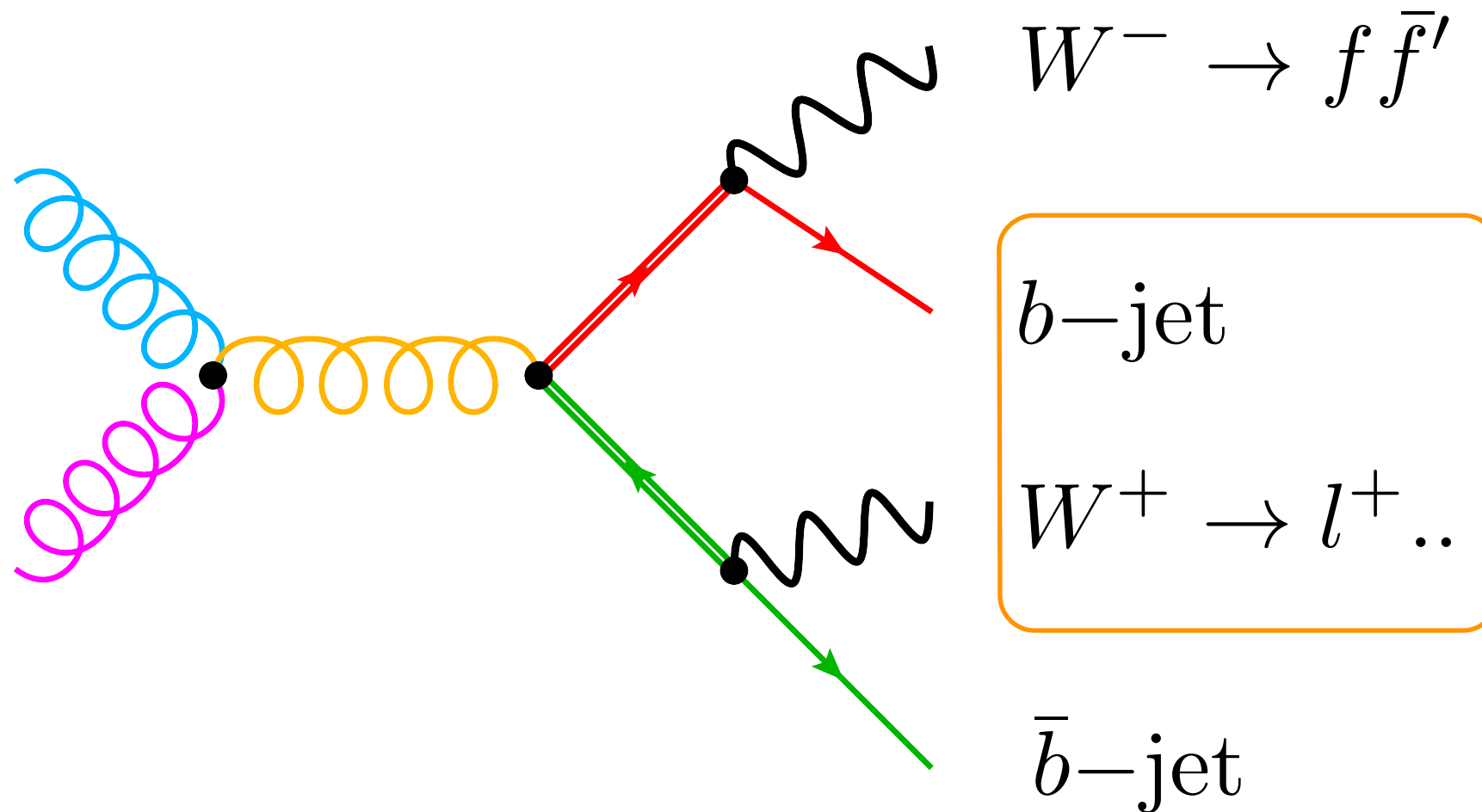
Original proposal (in context of  $t\bar{t}$  asymmetry):  
Kagan, Kamenik, Perez, Stone arXiv: 1103.3747

Follow-up papers:

RG arXiv: 1311.1810 (cross section and PDF constraints)

RG arXiv: 1409.8631 (SM asymmetry predictions)

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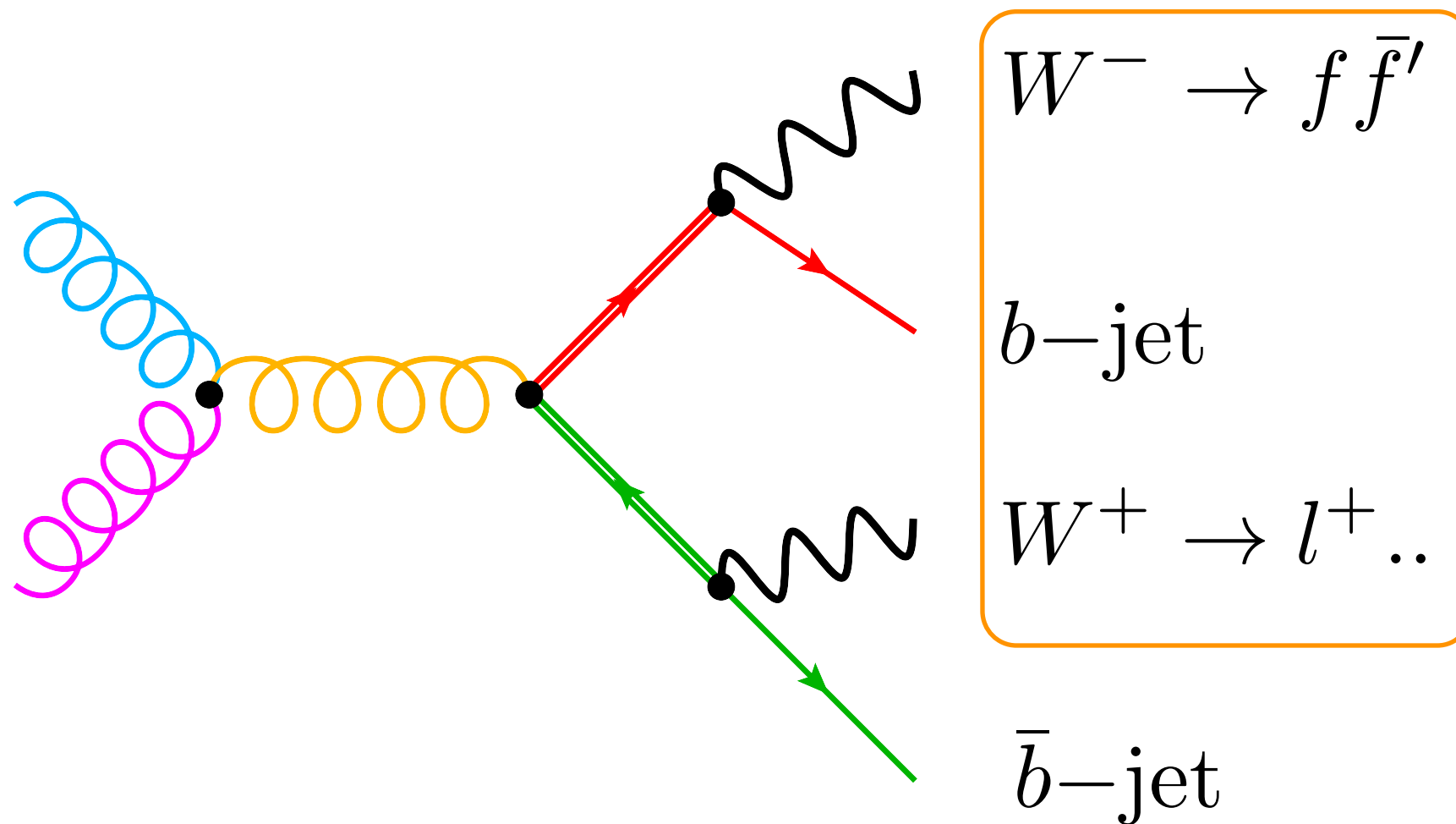
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# Statistical feasibility of top measurements

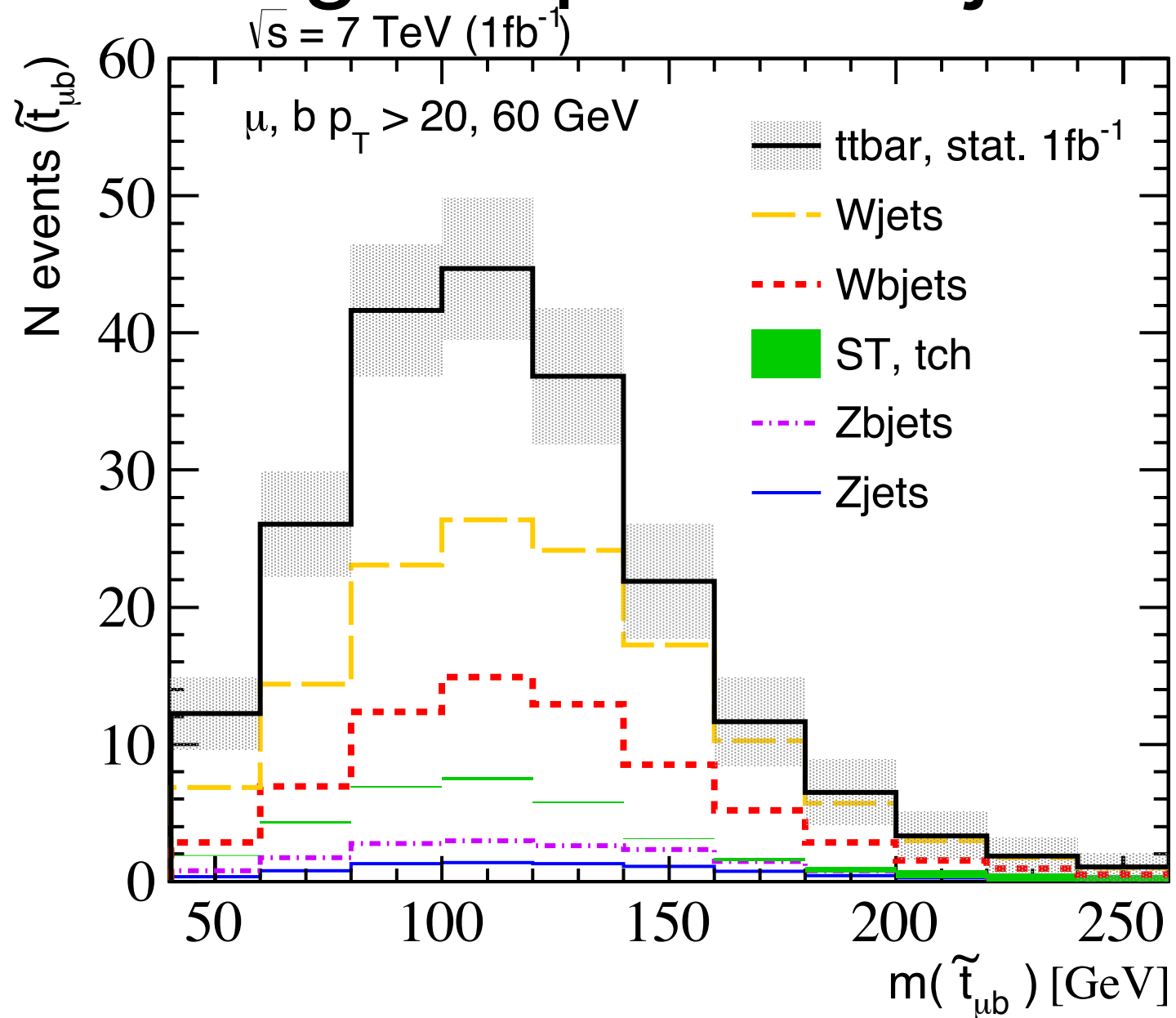
## Set-up

- Signal and background generated with NLO (**POWHEG**) interfaced to PS (**P8**)
- Cluster jets with anti-kt algorithm using  $R = 0.5$  distance parameter
- Truth match parton level b-quarks to jets within  $dR < 0.5$  (b)
- Apply experimental trigger efficiencies (0.75 for high pT muons arxiv: 1204.1620)
- b-tagging assumptions:
  - mis-tag rate 1% (accidentally think a light-jet is a b-jet)
  - efficiency 70% (how often you correctly tag a b-jet)

$$t\bar{t} \rightarrow XYZ$$

Acceptance  
Kinematics  
Isolation

# Single lepton + b-jet



$$t\bar{t} \rightarrow l^{\pm} b X$$

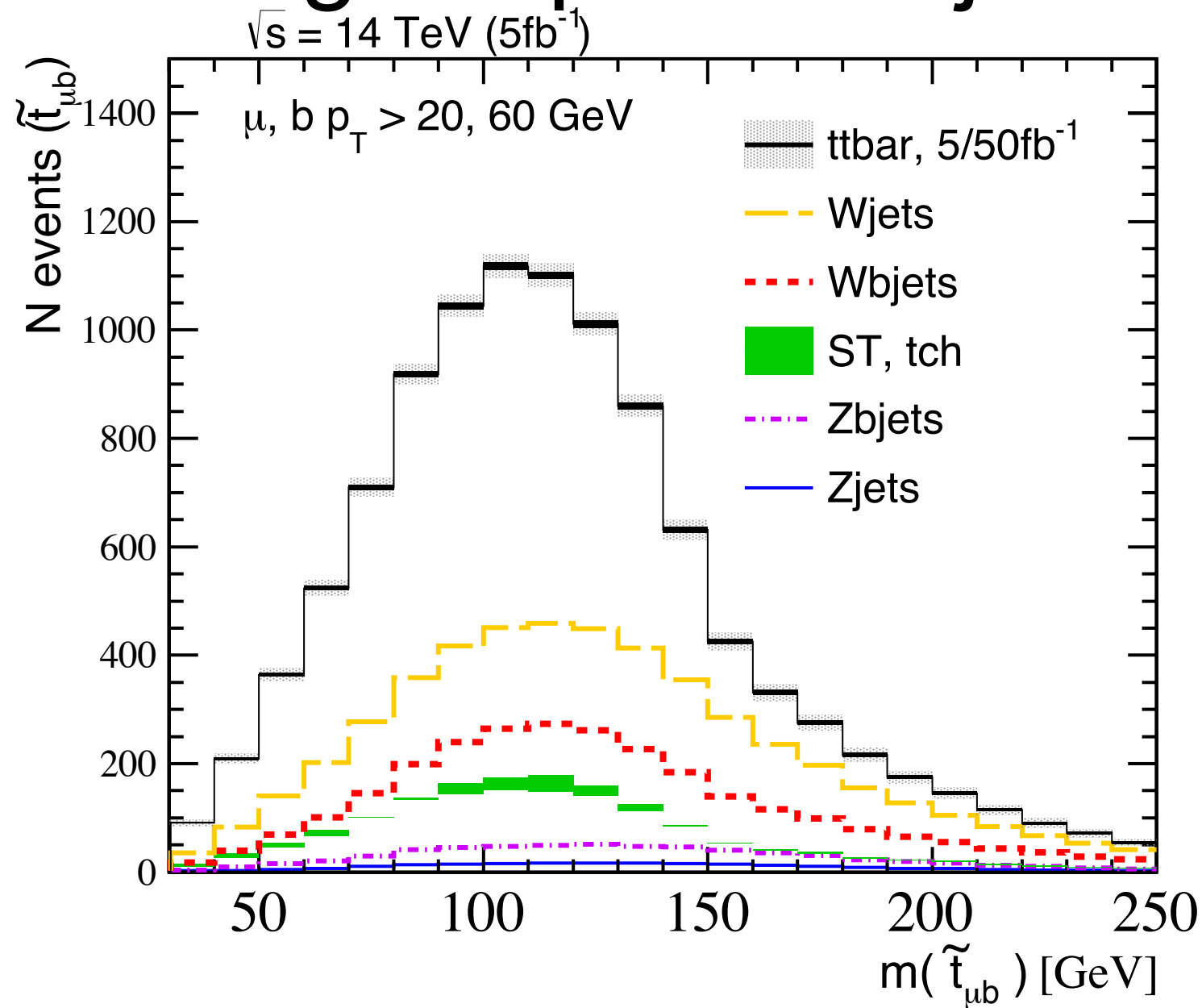
7 TeV

$$2.0 < \eta(l, b) < 4.5$$

$$p_T(l/b) > 20/60 \text{ GeV}$$

$$\Delta R(l^{\pm}, \text{jet}) \geq 0.5$$

# Single lepton + b-jet



$$t\bar{t} \rightarrow l^{\pm} b X$$

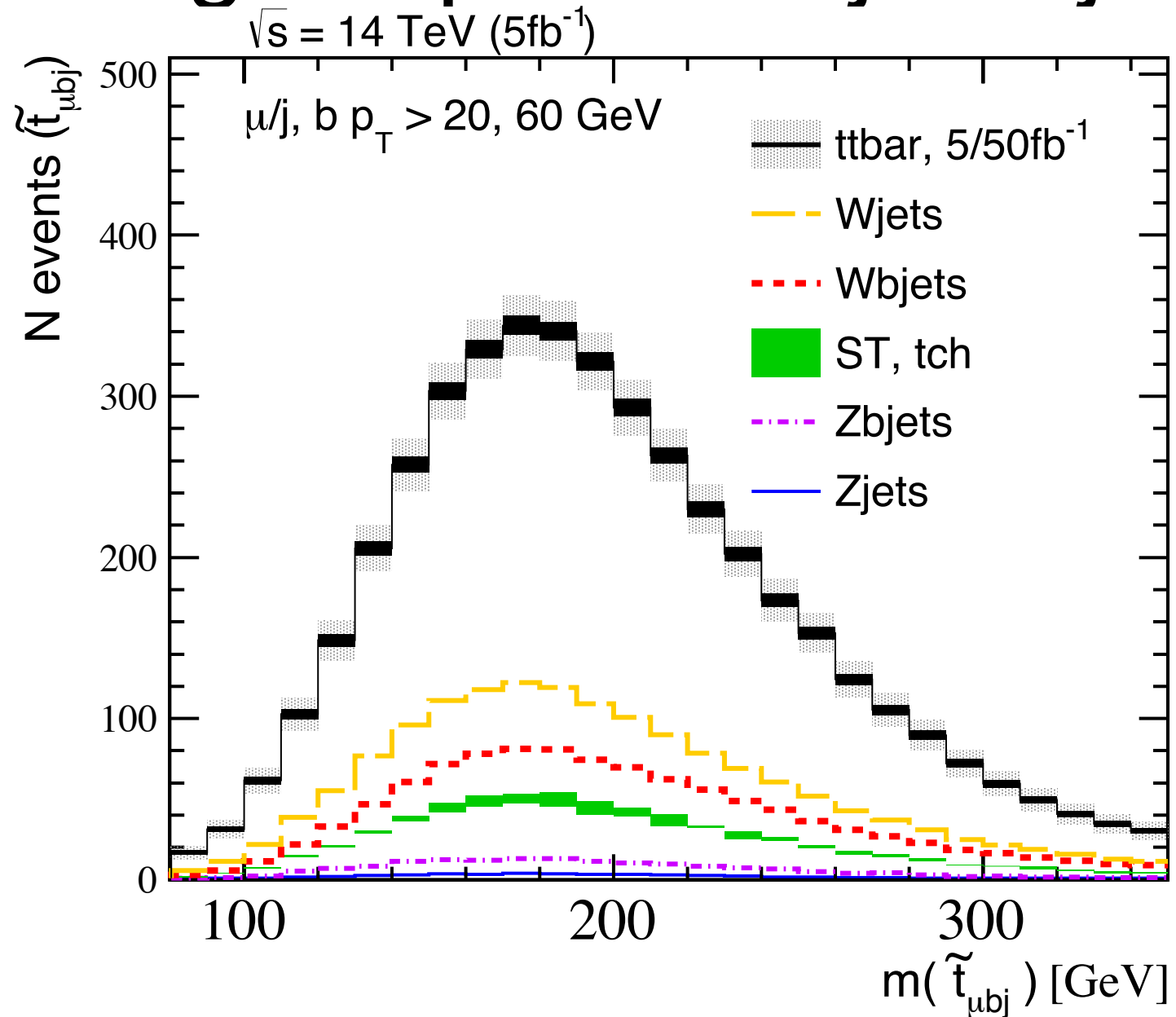
14 TeV

$$2.0 < \eta(l, b) < 4.5$$

$$p_T(l/b) > 20/60 \text{ GeV}$$

$$\Delta R(l^{\pm}, \text{jet}) \geq 0.5$$

# Single lepton + b-jet + jet



$$t\bar{t} \rightarrow l^{\pm} b j X$$

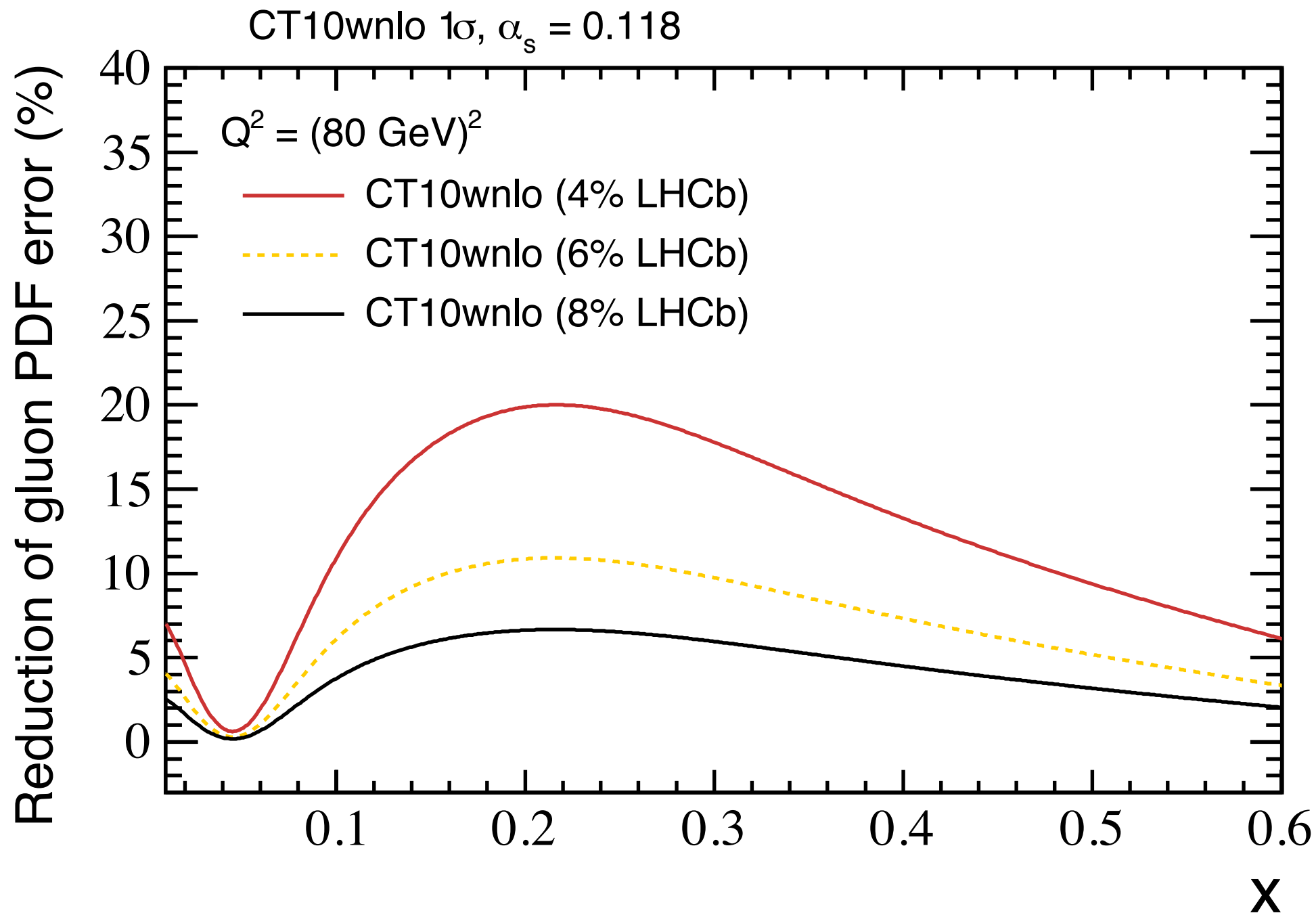
14 TeV

$$2.0 < \eta(l, b) < 4.5$$

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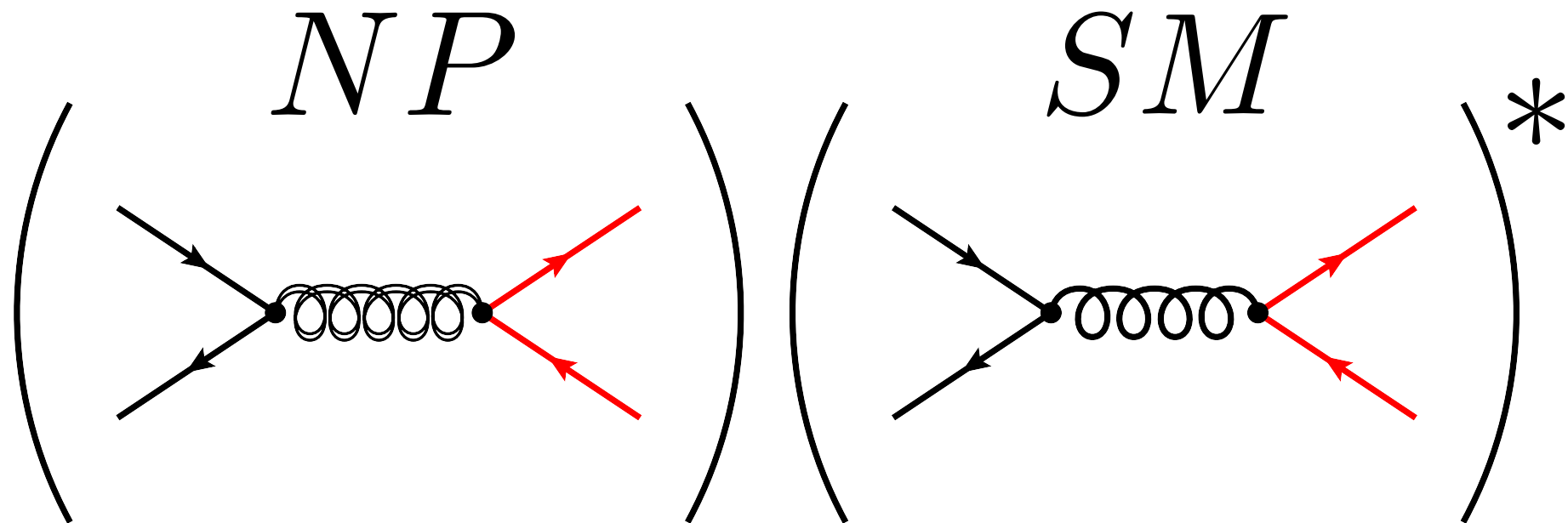
# As a constraint on the gluon PDF



Estimated improvement in gluon PDF with LHCb data  
Very **conservative** (doesn't include kinematic cuts)

# Production asymmetry measurements

# Motivations



1. Can see (N)ew (P)hysics effects through interference
2. A tree-level interference effect can be large!

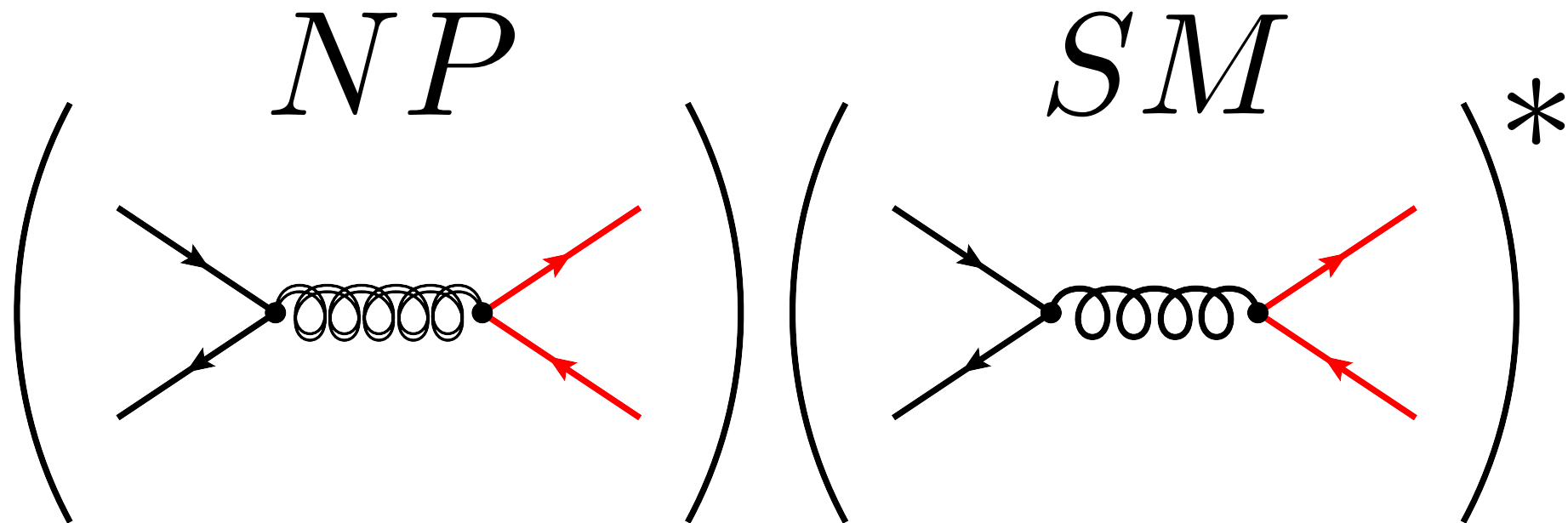
$$A_{fb} = \frac{(N_f - N_b)^{SM} + (N_f - N_b)^{NP}}{(N_f + N_b)^{Total}}$$

$$N_f^{NP} \gg N_b^{NP}, \quad (N_f + N_b)^{NP} \ll (N_f + N_b)^{SM}$$

See for example arXiv:1107.5257, J. Kamenik, J. Shu, J. Zupan



# Motivations



1. Can see (N)ew (P)hysics effects through interference
2. A tree-level interference effect can be large!

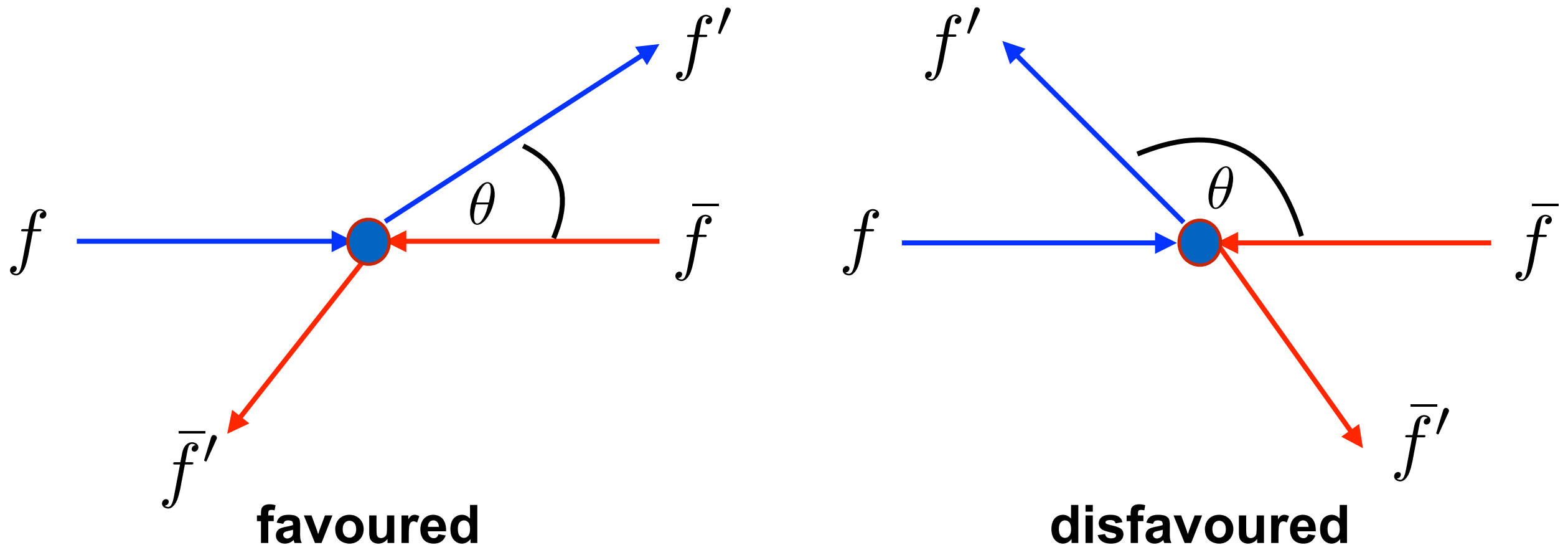
0 at LO in SM for QCD

$$A_{fb} = \frac{\cancel{(N_f - N_b)^{SM}} + (N_f - N_b)^{NP}}{(N_f + N_b)^{Total}}$$

$$N_f^{NP} \gg N_b^{NP}, \quad (N_f + N_b)^{NP} \ll (N_f + N_b)^{SM}$$

# Angular asymmetry in $f\bar{f} \rightarrow f'\bar{f}'$

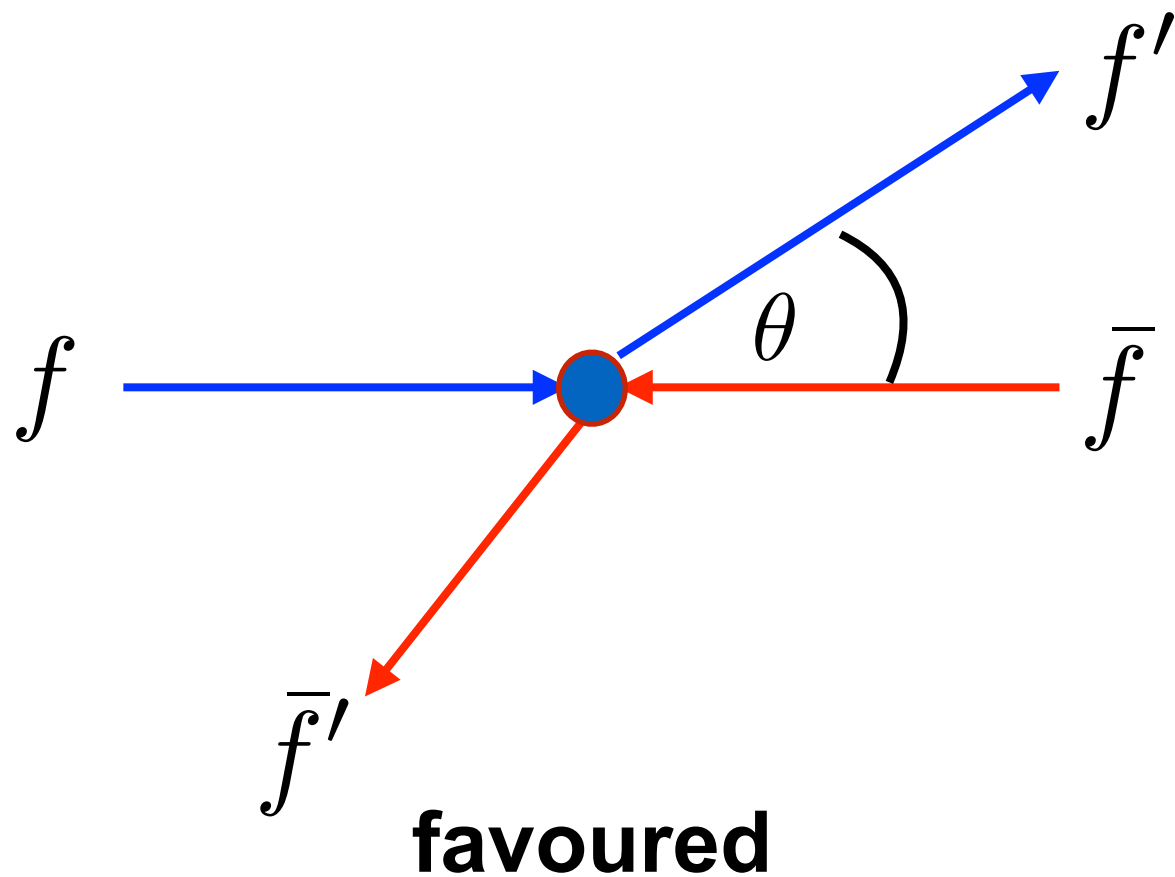
Known for a long time in QCD and QED.....



Nucl. Phys. B57 (1973) 381, F. A. Berends, K. Gaemer, and R. Gastmans,  
Acta Phys. Polon. B14 (1983) 413, F. A. Berends, R. Kleiss, S. Jadach, and Z. Was,  
Phys. Lett. B195(1987) 74 F. Halzen, P. Hoyer, and C. Kim  
Nucl. Phys. B327 (1989) 49 P. Nason, S. Dawson, and R. K. Ellis  
arXiv:hep-ph/9802268, arXiv:hep-ph/9807420 J.H.Kuhn, G. Rodrigo.... many more

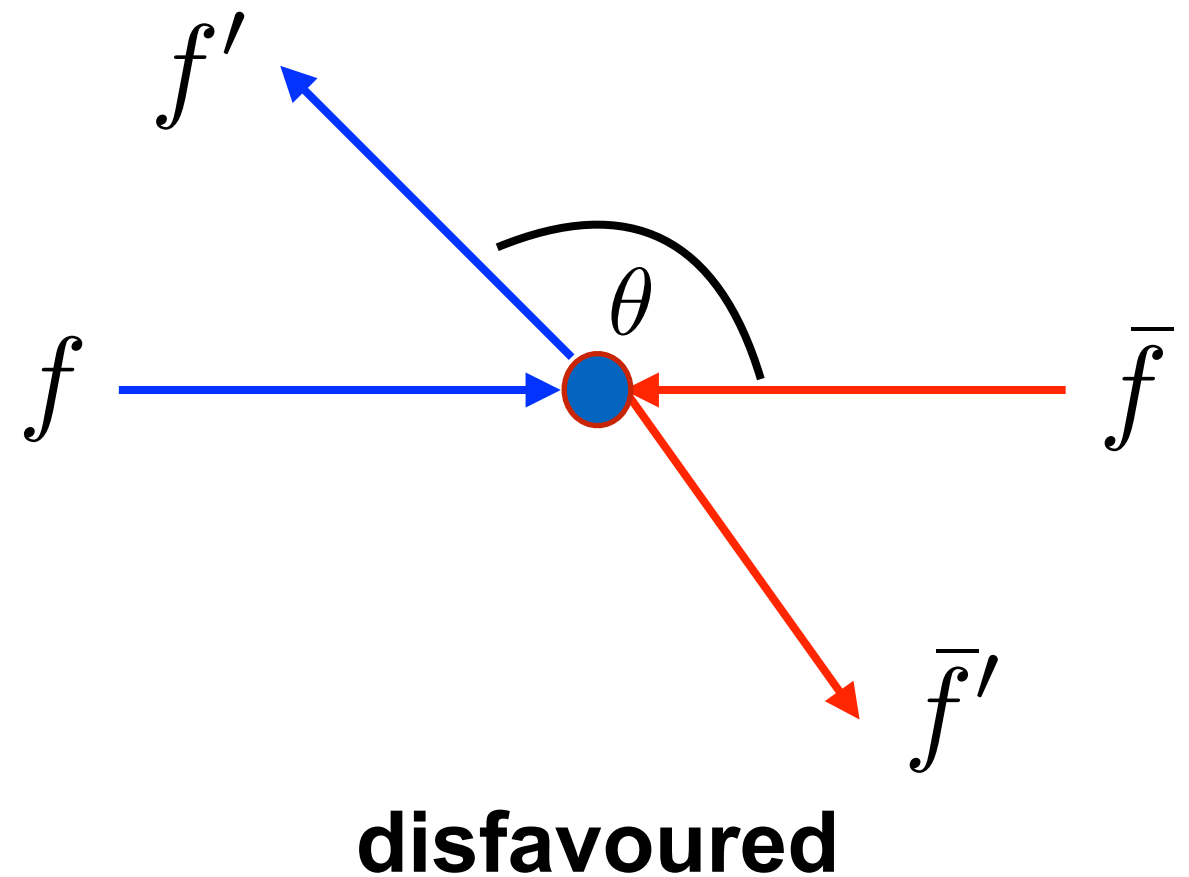
# Angular asymmetry in $f \bar{f} \rightarrow f' \bar{f}'$

Known for a long time in QCD and QED.....



$$\hat{s} = (p_f + p_{\bar{f}})^2$$

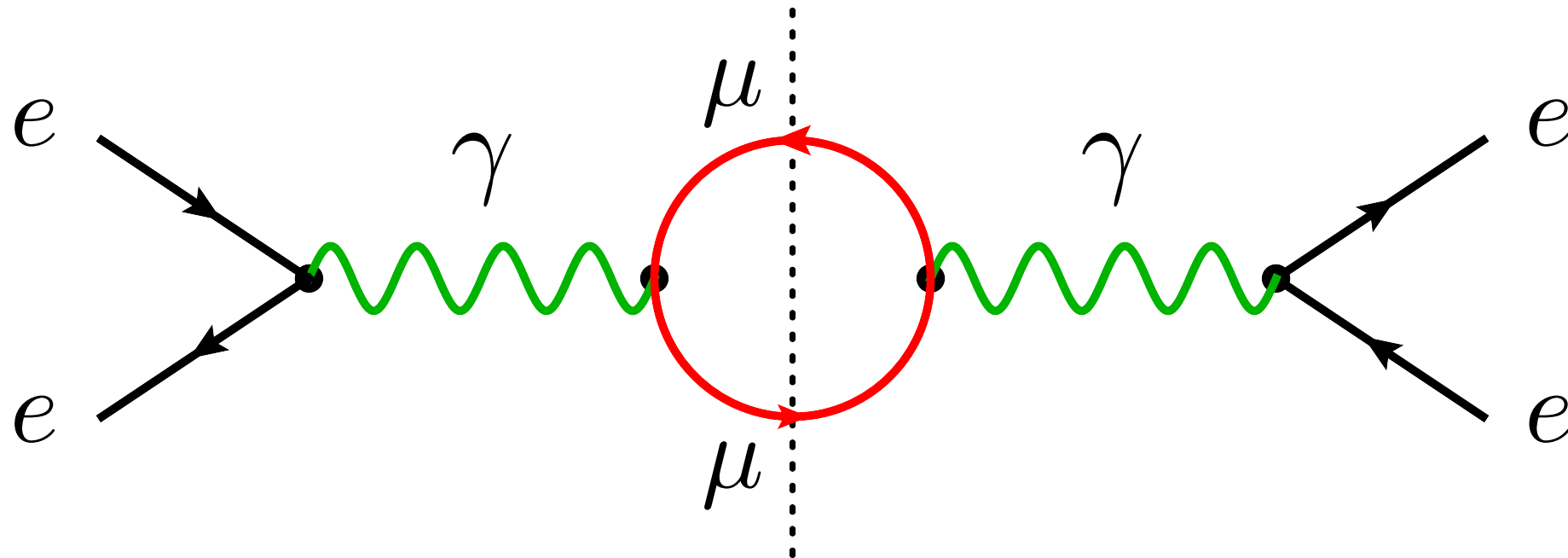
$$t_H = -\frac{\hat{s}}{2} (1 - \beta \cos \theta)$$



$$\beta^2 = 1 - \frac{4m_{f'}^2}{\hat{s}}$$

$$u_H = -\frac{\hat{s}}{2} (1 + \beta \cos \theta)$$

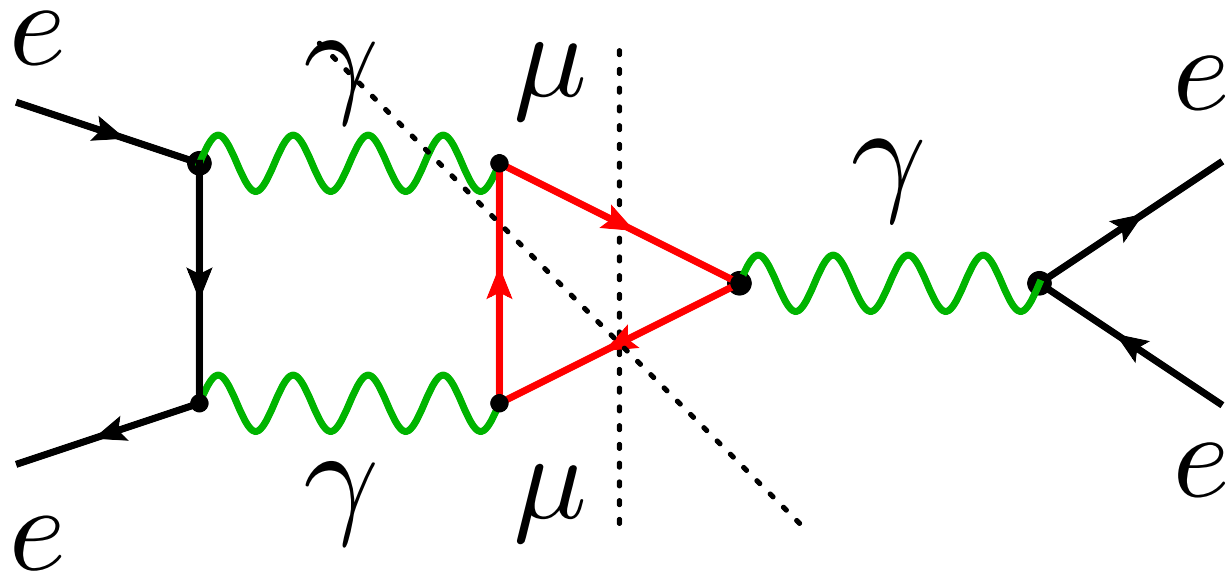
Qualitative example  $e^+e^- \rightarrow \mu^+\mu^-$



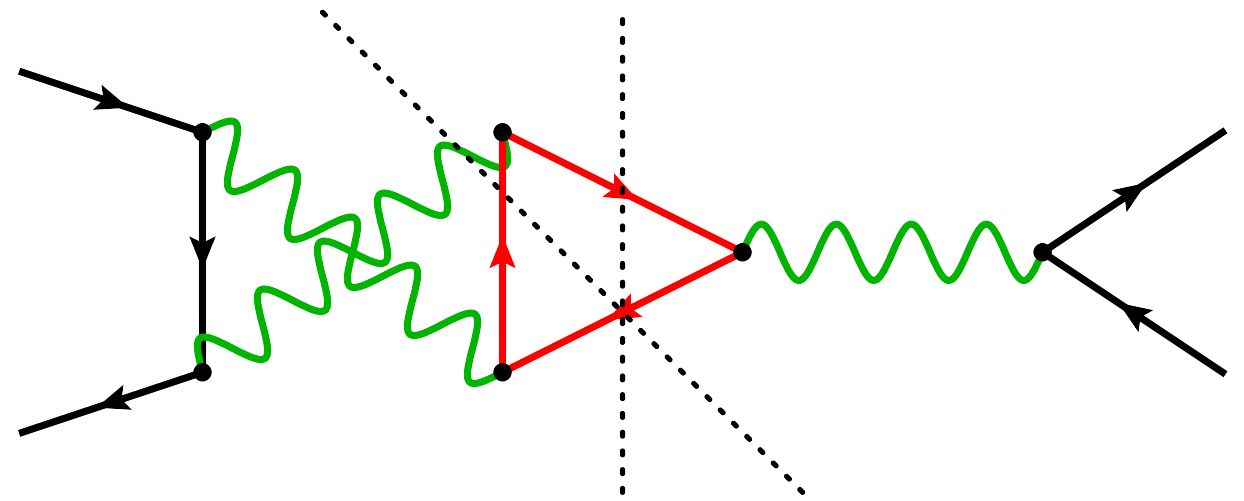
$$\mathcal{M}_{\text{LO}} \cdot \mathcal{M}_{\text{LO}}^*$$

$$d\sigma_{\text{asym}} = \frac{1}{2} (d\sigma(t_H, u_H) - d\sigma(u_H, t_H)) = 0$$

# Qualitative example $e^+e^- \rightarrow \mu^+\mu^-$



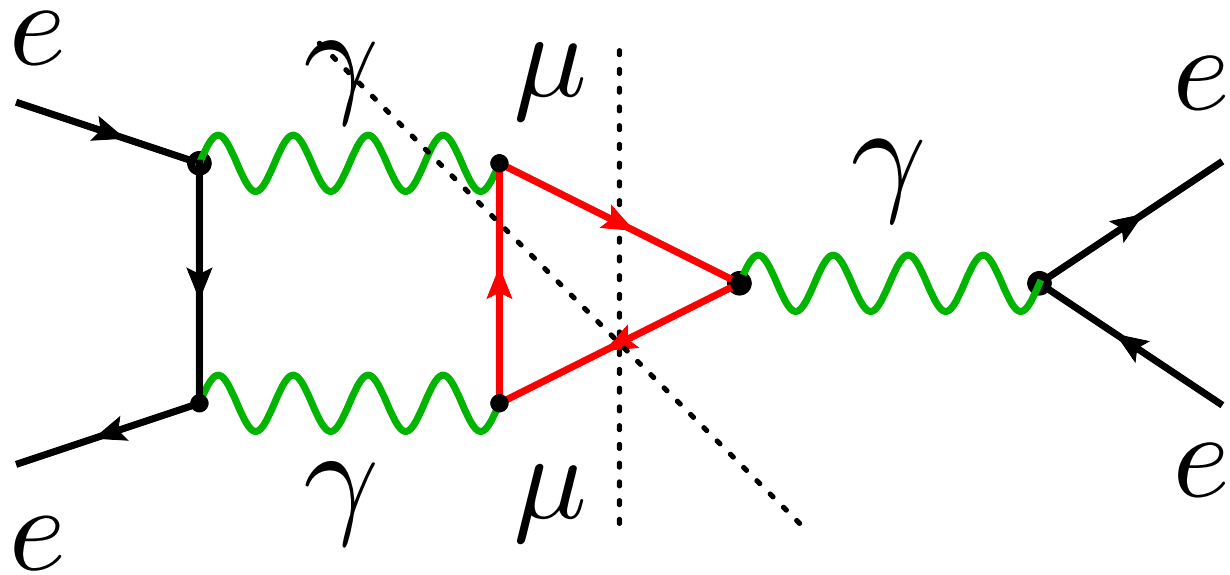
$$\mathcal{M}_A \cdot \mathcal{M}_{\text{LO}}^*$$



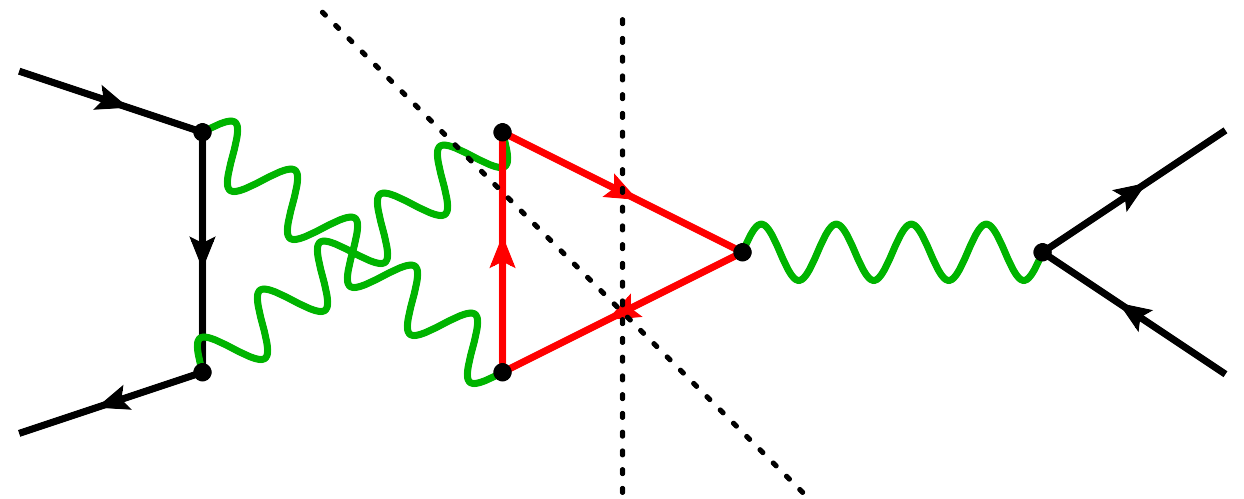
$$\mathcal{M}_B \cdot \mathcal{M}_{\text{LO}}^*$$

$$d\sigma_{\text{asym}} = \frac{1}{2} (d\sigma(t_H, u_H) - d\sigma(u_H, t_H)) \neq 0$$

# Qualitative example $e^+e^- \rightarrow \mu^+\mu^-$



$$\mathcal{M}_A \cdot \mathcal{M}_{\text{LO}}^*$$



$$\mathcal{M}_B \cdot \mathcal{M}_{\text{LO}}^*$$

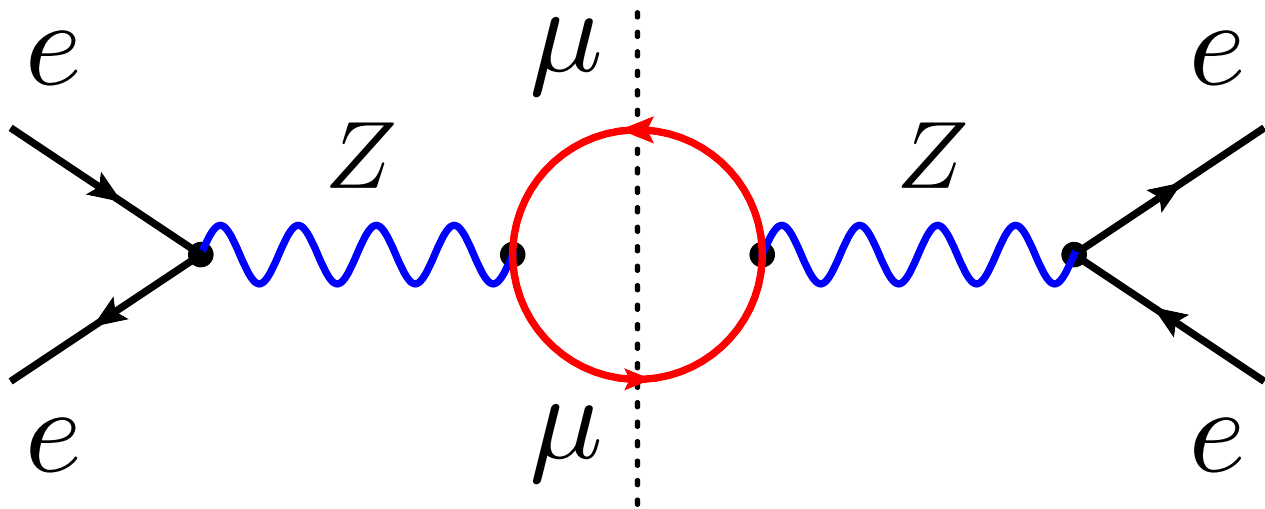
$$d\sigma_{\text{asym}} = \frac{1}{2} (d\sigma(t_H, u_H) - d\sigma(u_H, t_H)) \neq 0$$

$$d\sigma_A(t_H, u_H) = -d\sigma_B(u_H, t_H)$$

Feature of  
box amplitude

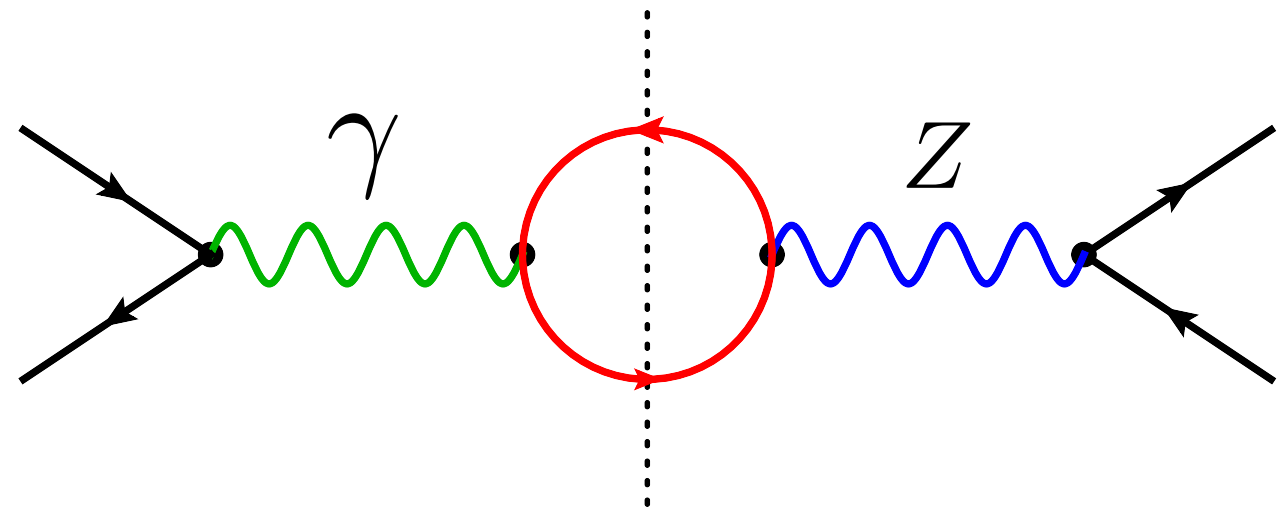
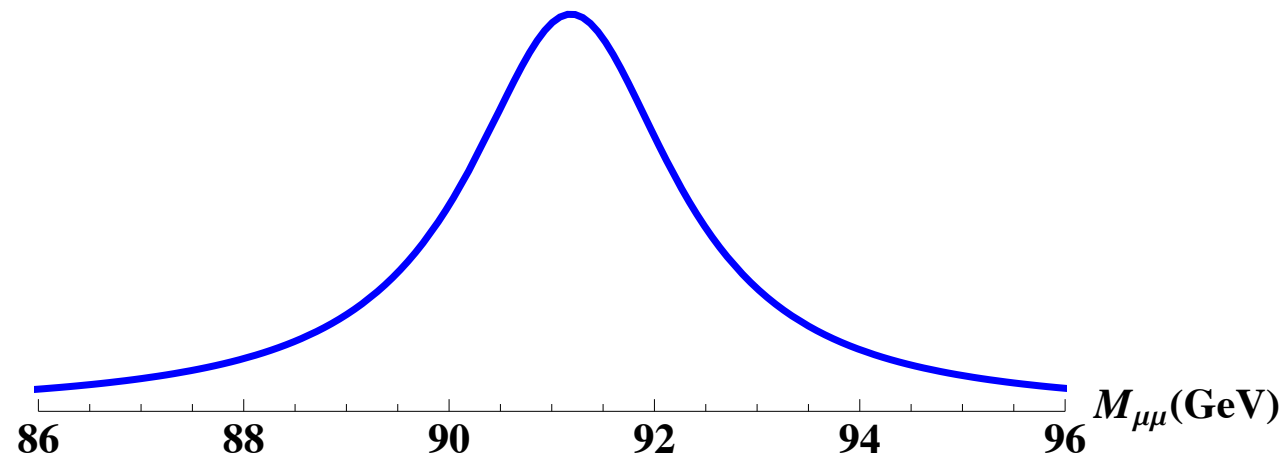
$$d\sigma_{\text{asym}} \propto d\sigma_A(t_H, u_H) + d\sigma_B(t_H, u_H)$$

# Qualitative example $e^+e^- \rightarrow \mu^+\mu^-$



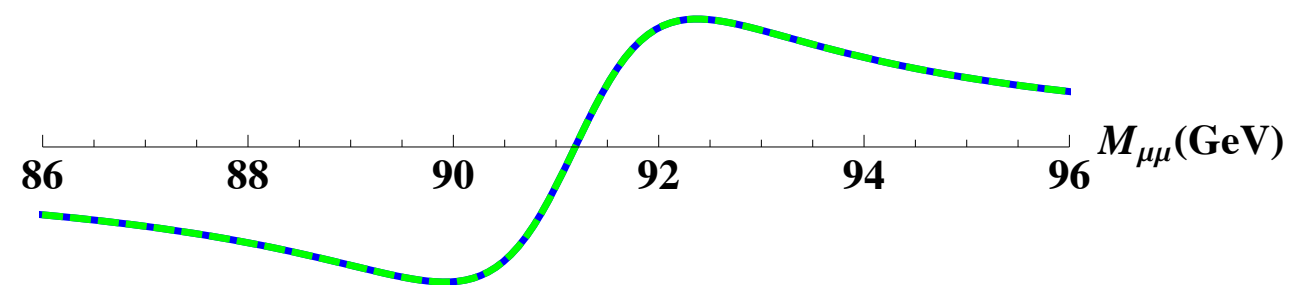
$$\mathcal{M}_Z \cdot \mathcal{M}_Z^*$$

$$d\sigma_{\text{asym}}^{\gamma/Z} \propto \frac{\alpha g_A^e g_A^\mu g_V^e g_V^\mu \beta^2 \kappa^2 \hat{s} \cos \theta}{(\hat{s} - M_Z^2)^2}$$

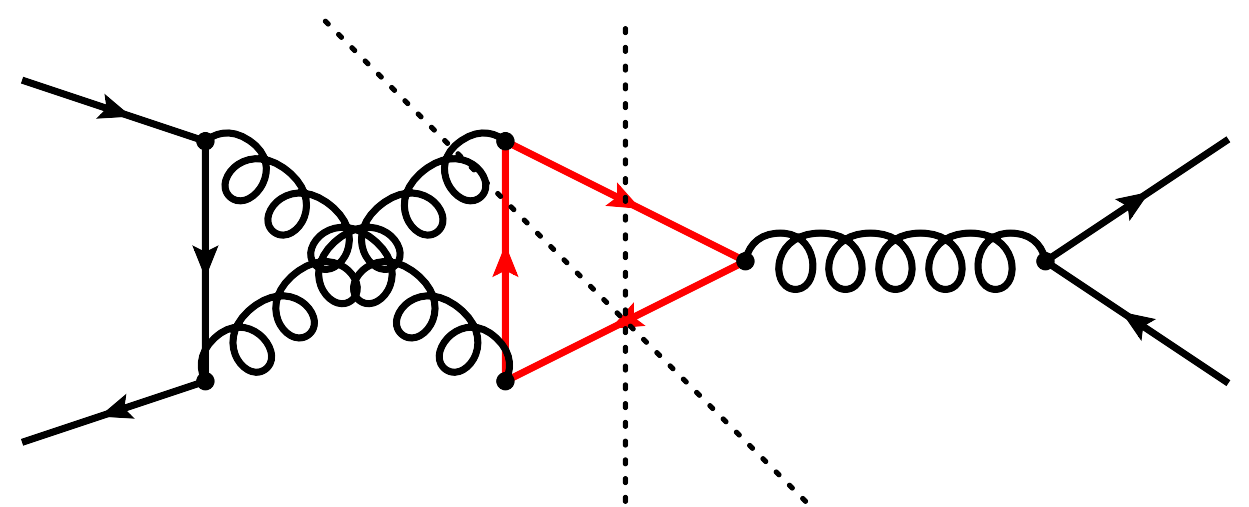
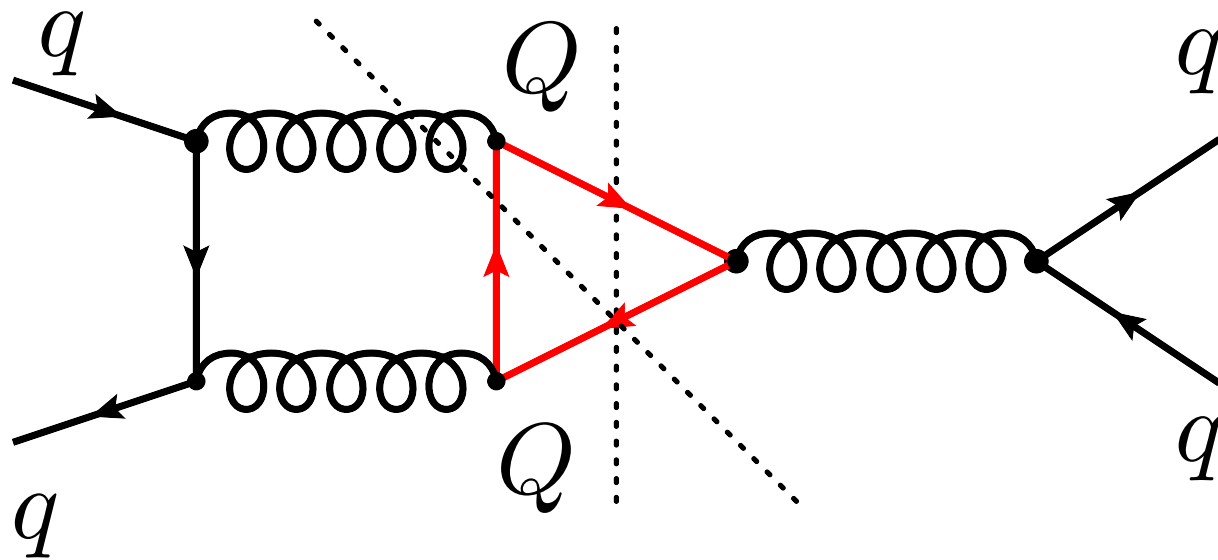


$$\mathcal{M}_\gamma \cdot \mathcal{M}_Z^*$$

$$d\sigma_{\text{asym}}^{\gamma/Z} \propto \frac{\alpha g_A^e g_A^\mu Q^e Q^\mu \beta^2 \kappa \cos \theta}{\hat{s} - M_Z^2}$$

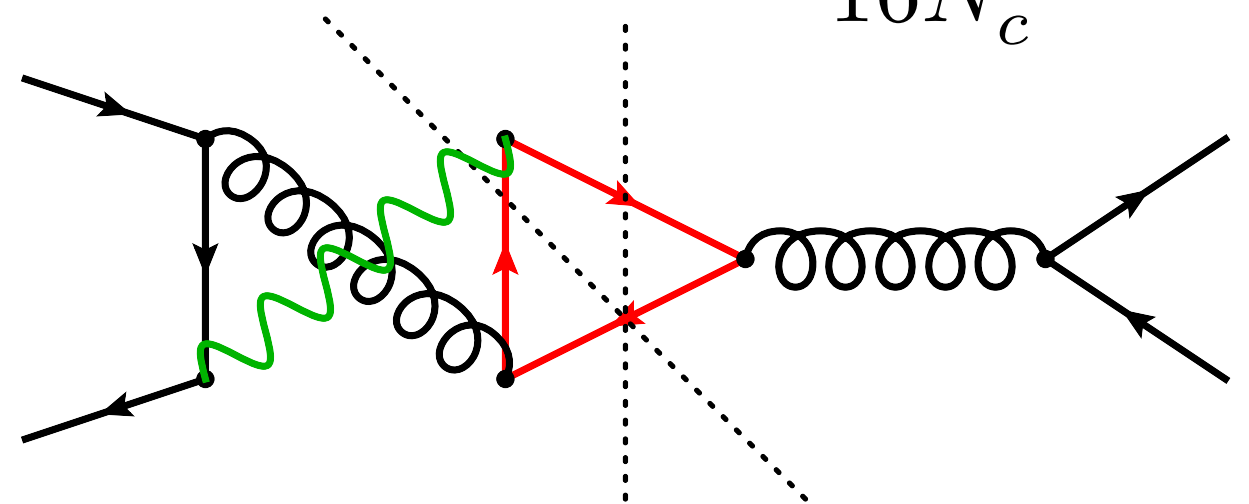
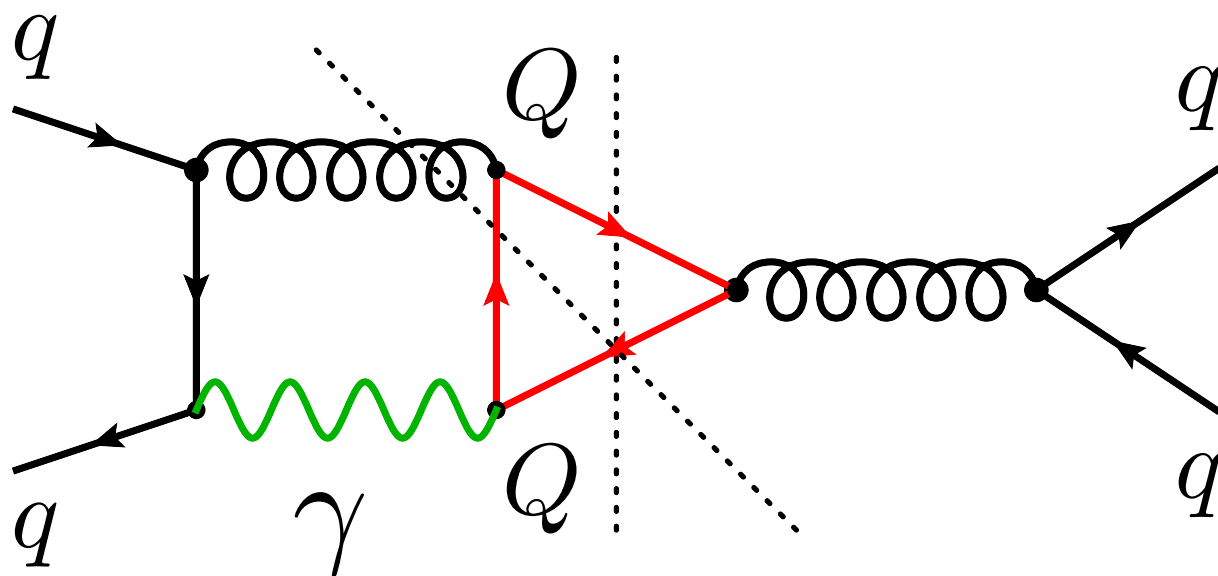


# $Q\bar{Q}$ final state at hadron colliders



Can obtain QCD from QED result:

$$\alpha^3 Q_f^3 Q_{f'}^3 \rightarrow \alpha_s^3 \frac{d_{\text{ABC}}^2}{16N_c^2}$$



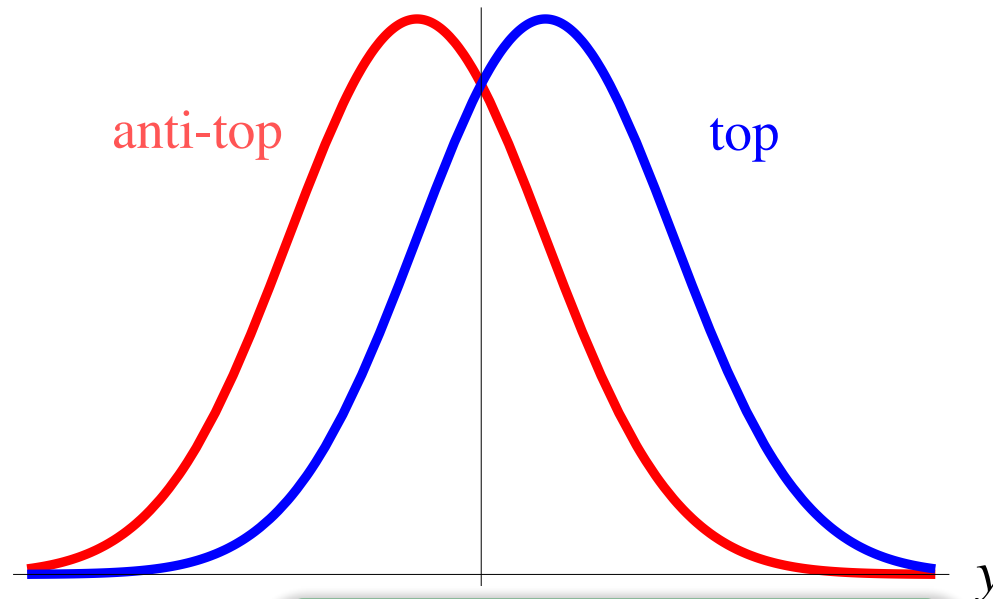
Can obtain QED-QCD from QED result:  $\alpha^3 Q_f^3 Q_{f'}^3 \rightarrow 3 \left( \alpha Q_f Q_{f'} \alpha_s^2 \frac{C_F}{2N_c} \right)$

**COMMENT:** Since  $q\bar{q} \rightarrow Q\bar{Q}X$ ,  $X = \gamma, g, Z, W^\pm$  contribute to asym. By crossing symmetry, so do  $qX \rightarrow Q\bar{Q}q$ ,  $\bar{q}X \rightarrow Q\bar{Q}\bar{q}$

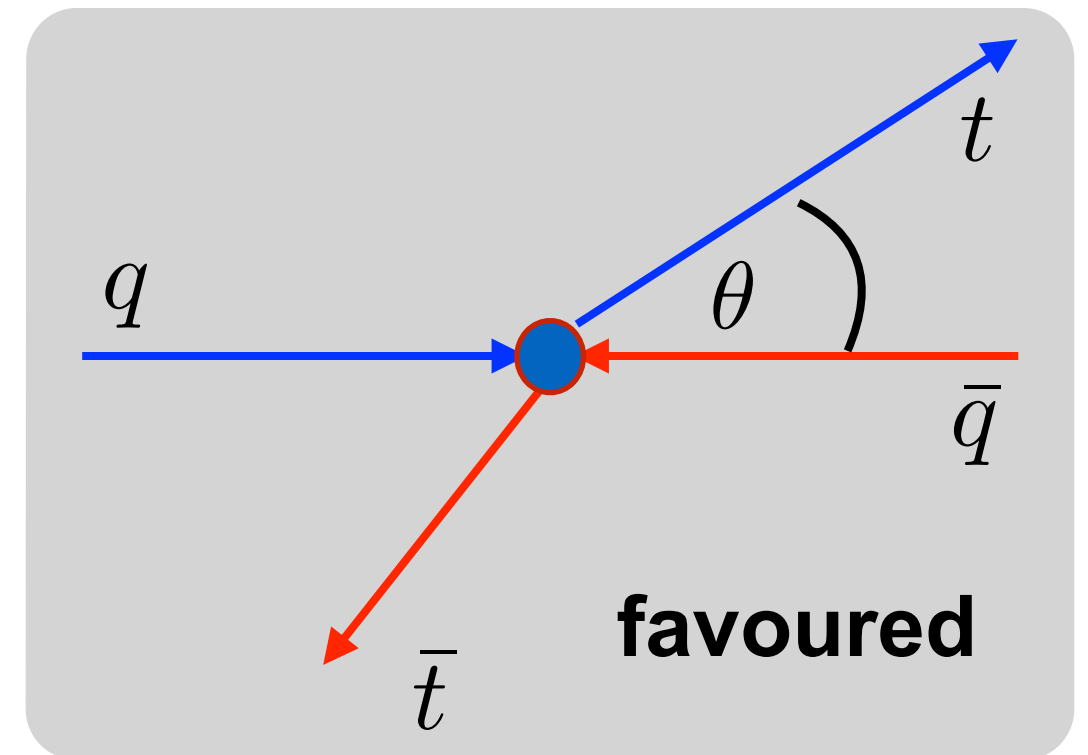


# Results from the Tevatron

Tevatron  $p\bar{p} \rightarrow Q\bar{Q}$



nnlo QCD + nlo ewk  
Czakon,Fielder,Mitov



## Inclusive results with all data

CDF Collaboration, arXiv:1211.1003.

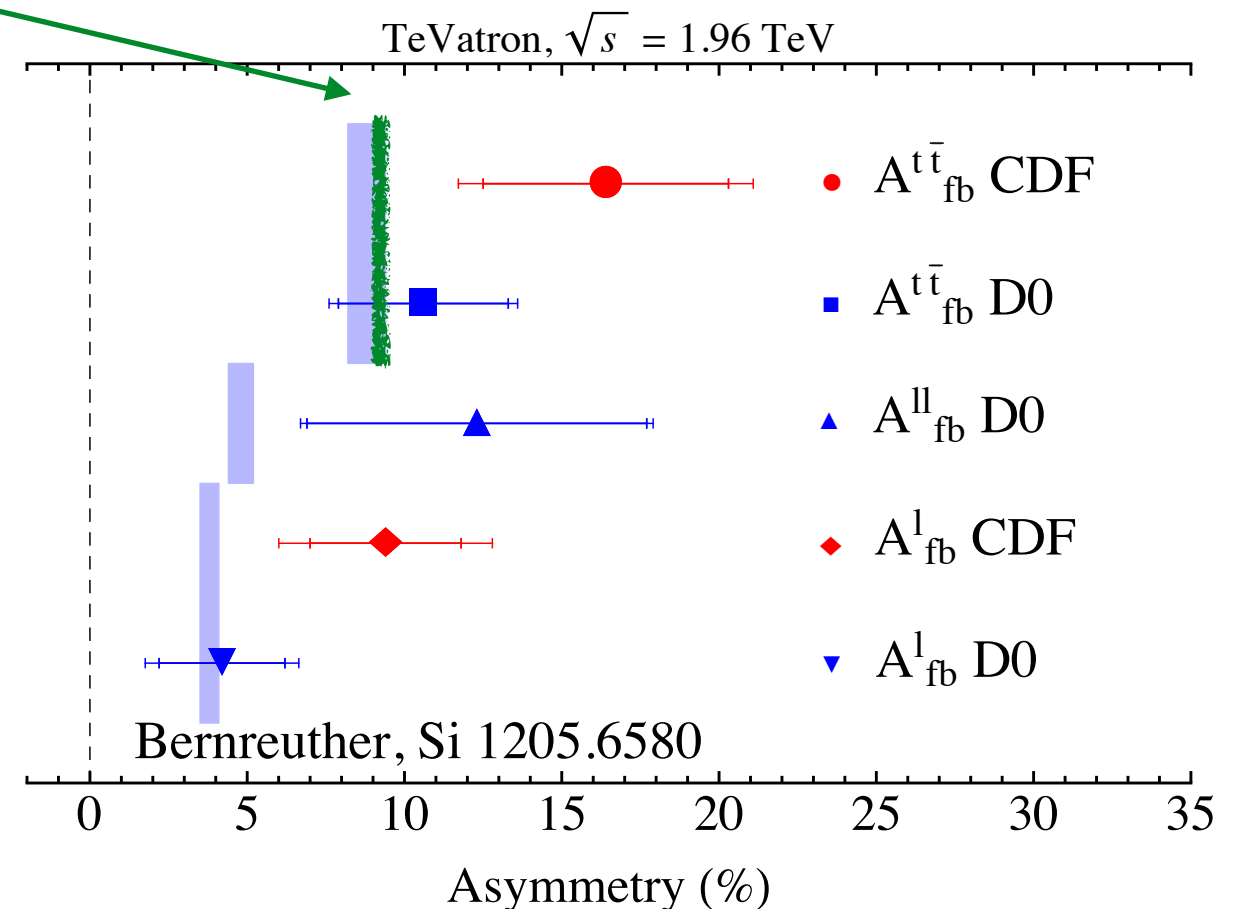
D0 Collaboration, arXiv:1405.0421.

D0 Collaboration, 1308.6690.

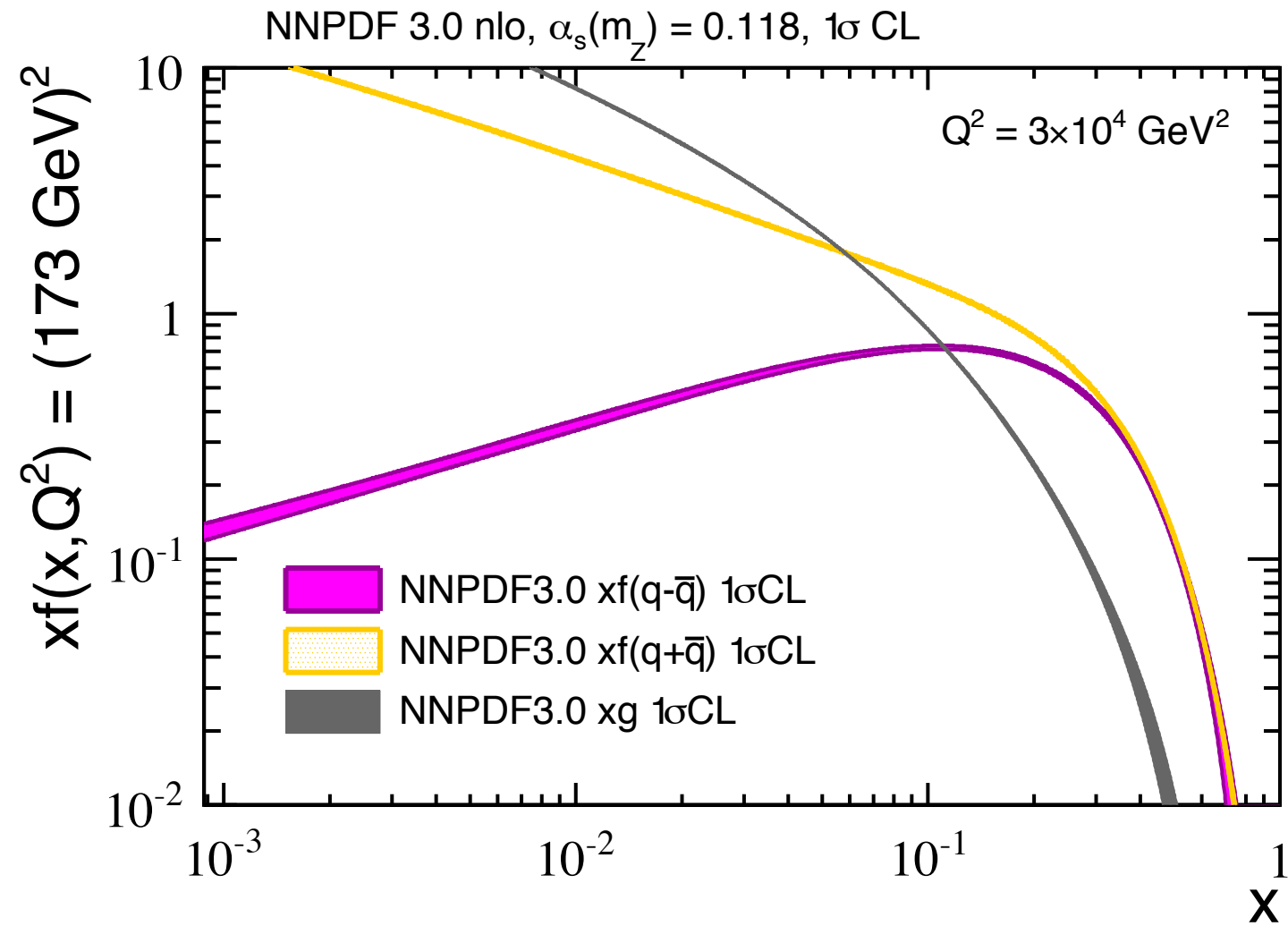
CDF Collaboration, arXiv:1308.1120.

D0 Collaboration, arXiv:1403.1294.

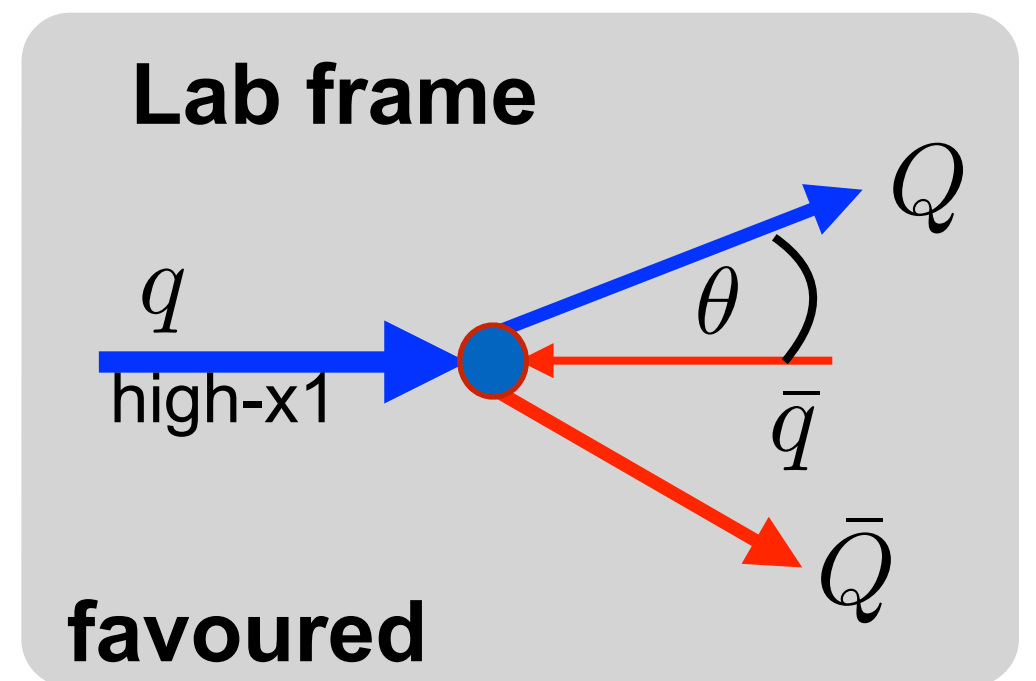
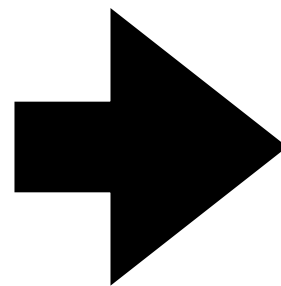
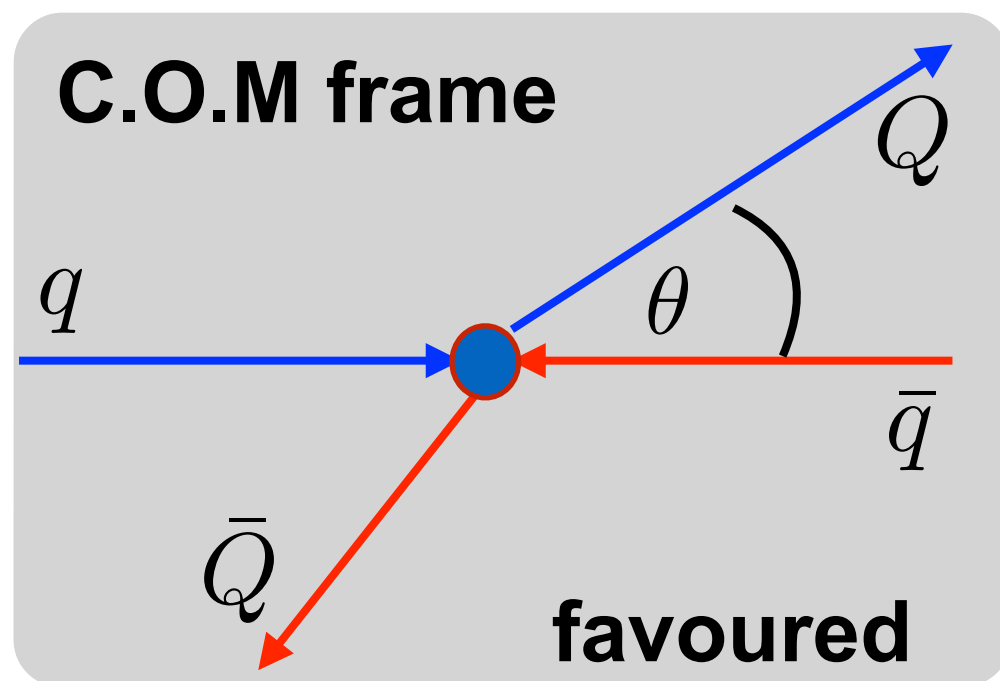
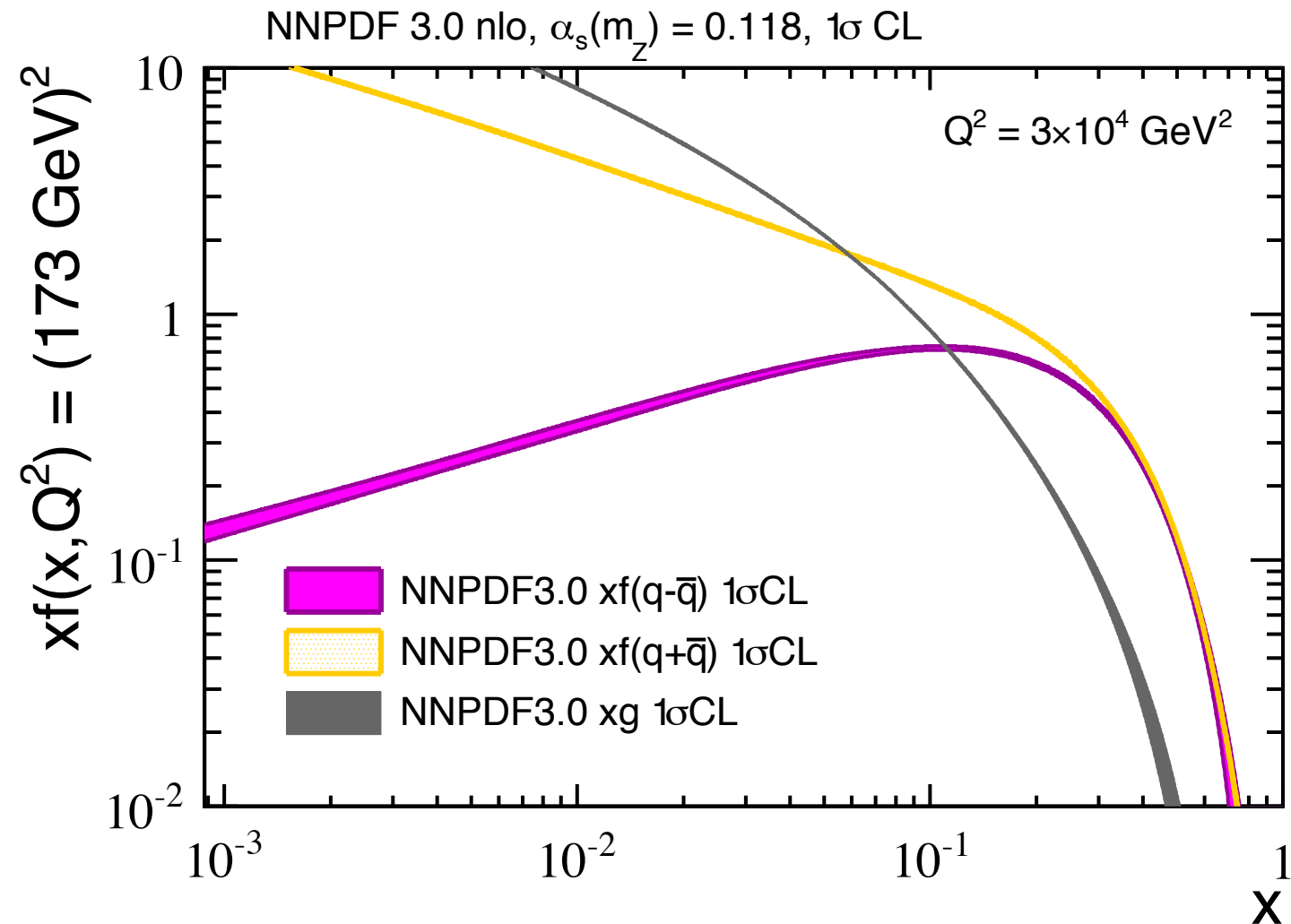
$$\chi^2/N_{\text{d.o.f.}} \simeq 7.1/5 \simeq 1.3\sigma$$



# What about the LHC?



# What about the LHC?



# First measurement of the charge asymmetry in beauty-quark pair production at a hadron collider

The LHCb collaboration<sup>†</sup>

## Abstract

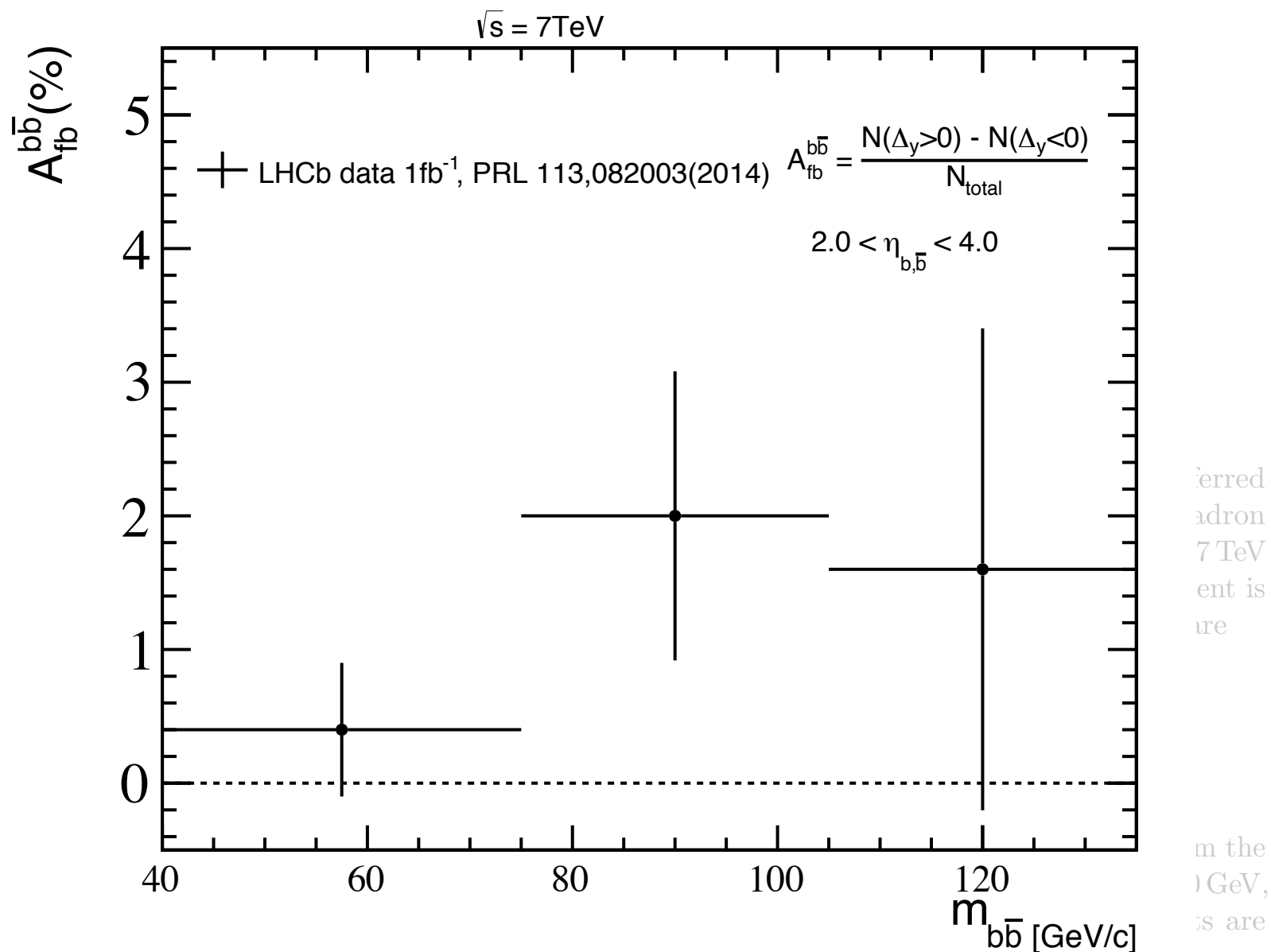
The difference in the angular distributions between beauty quarks and antiquarks, referred to as the charge asymmetry, is measured for the first time in  $b\bar{b}$  pair production at a hadron collider. The data used correspond to an integrated luminosity of  $1.0\text{ fb}^{-1}$  collected at 7 TeV center-of-mass energy in proton-proton collisions with the LHCb detector. The measurement is performed in three regions of the invariant mass of the  $b\bar{b}$  system. The results obtained are

$$\begin{aligned} A_C^{b\bar{b}}(40 < M_{b\bar{b}} < 75 \text{ GeV}/c^2) &= 0.4 \pm 0.4 (\text{stat}) \pm 0.3 (\text{syst})\%, \\ A_C^{b\bar{b}}(75 < M_{b\bar{b}} < 105 \text{ GeV}/c^2) &= 2.0 \pm 0.9 (\text{stat}) \pm 0.6 (\text{syst})\%, \\ A_C^{b\bar{b}}(M_{b\bar{b}} > 105 \text{ GeV}/c^2) &= 1.6 \pm 1.7 (\text{stat}) \pm 0.6 (\text{syst})\%, \end{aligned}$$

where  $A_C^{b\bar{b}}$  is defined as the asymmetry in the difference in rapidity between jets formed from the beauty quark and antiquark. The beauty jets are required to satisfy  $2 < \eta < 4$ ,  $E_T > 20 \text{ GeV}$ , and have an opening angle in the transverse plane  $\Delta\phi > 2.6 \text{ rad}$ . These measurements are consistent with the predictions of the Standard Model.

- Measure forward-backward asymmetry of b-jets using 7TeV data
- Charge tag b-jets using semi-leptonic B-decays
- Measurement performed in bins of  $M_{b\bar{b}}$

$$2.0 < \eta < 4.0, \quad E_T > 20 \text{ GeV}, \quad \Delta\phi > 2.6 \text{ rad}$$



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# SM prediction (RG, U. Haisch, B. Pecjak, E. Re)

$$A_{\text{FC}}^{Q\bar{Q}} = \frac{\sigma(\Delta y > 0) - \sigma(\Delta y < 0)}{\sigma(\Delta y > 0) + \sigma(\Delta y < 0)} \quad \Delta y = y_b - y_{\bar{b}}$$

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Symmetric NLO QCD  
P. Nason, S. Dawson, R. K. Ellis,  
Nucl. Phys. B 303 607 (1988)  
Implemented in POWHEG-BOX

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J. H. Kuhn and G. Rodrigo,  
Phys. Rev. D 59, 054017 (1999)

Use analytic formula

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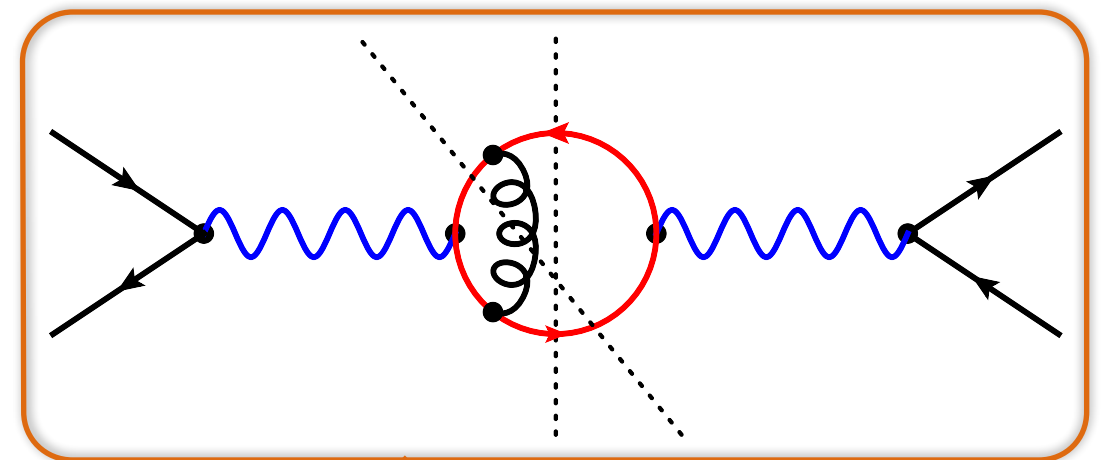
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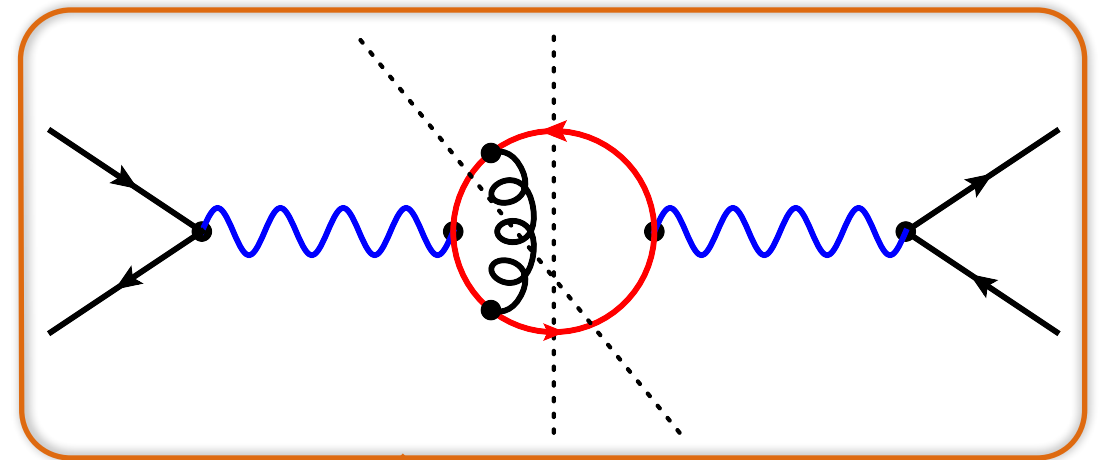
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J. H. Kuhn and G. Rodrigo,  
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Use analytic formula

'tricky'  
part



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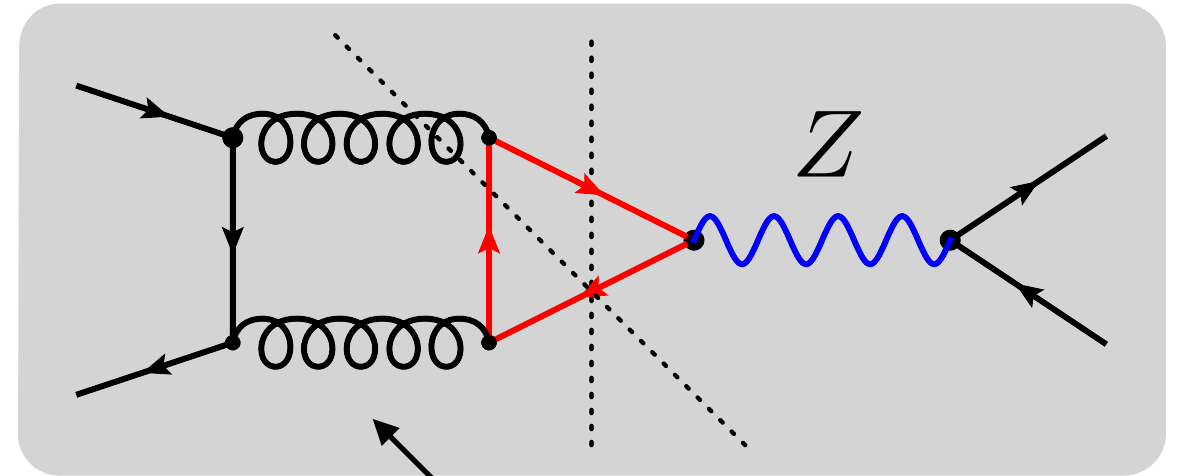
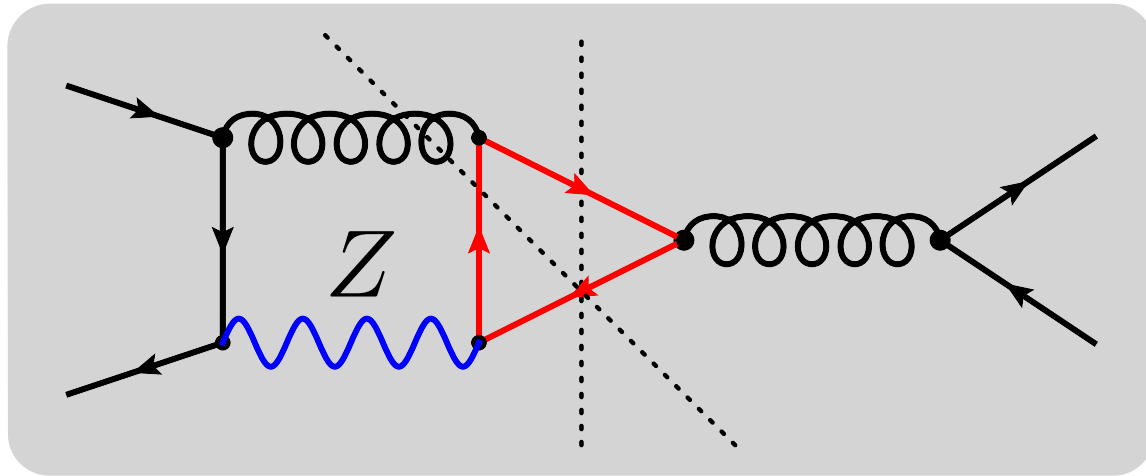
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# Resonant contributions



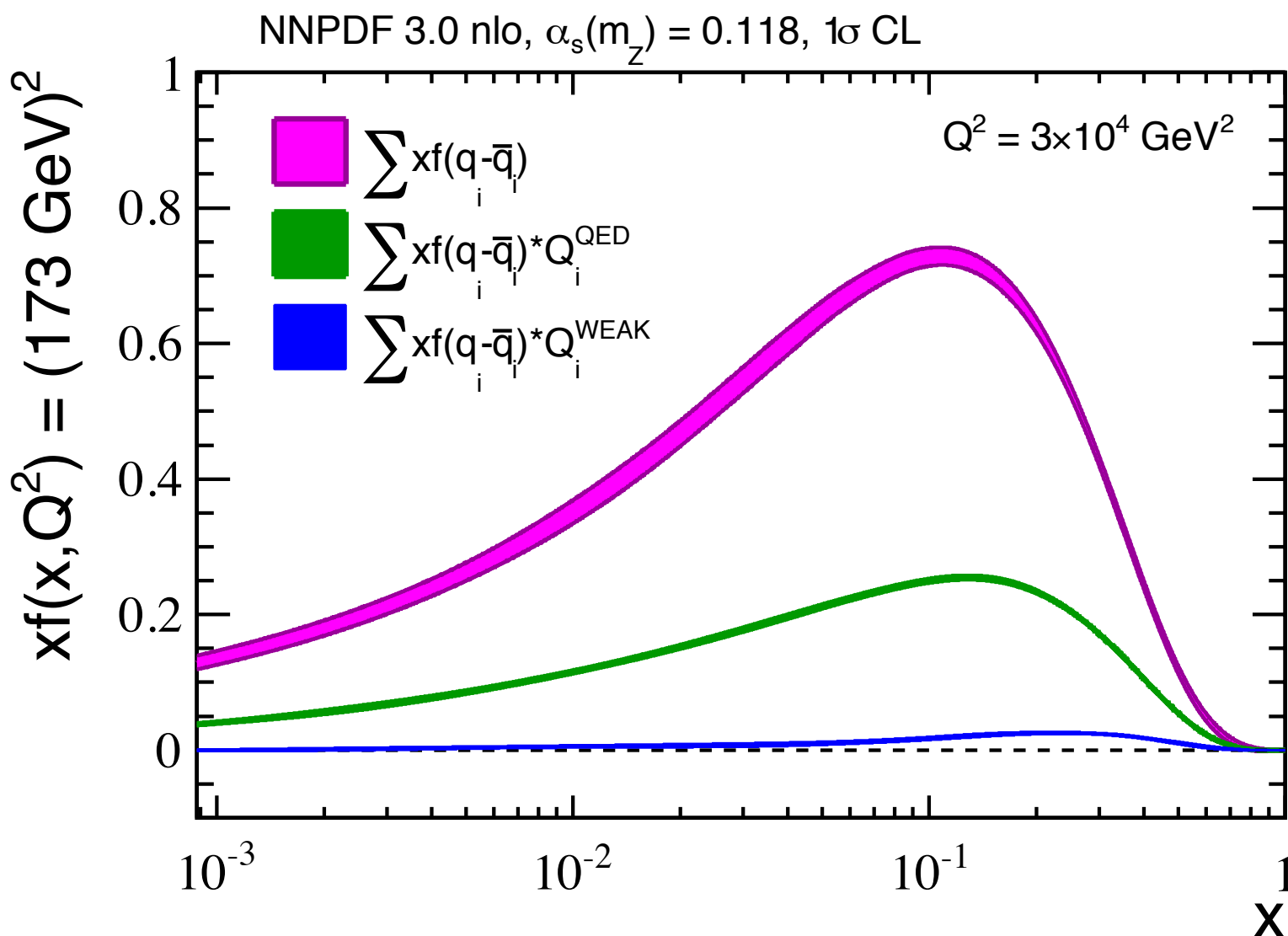
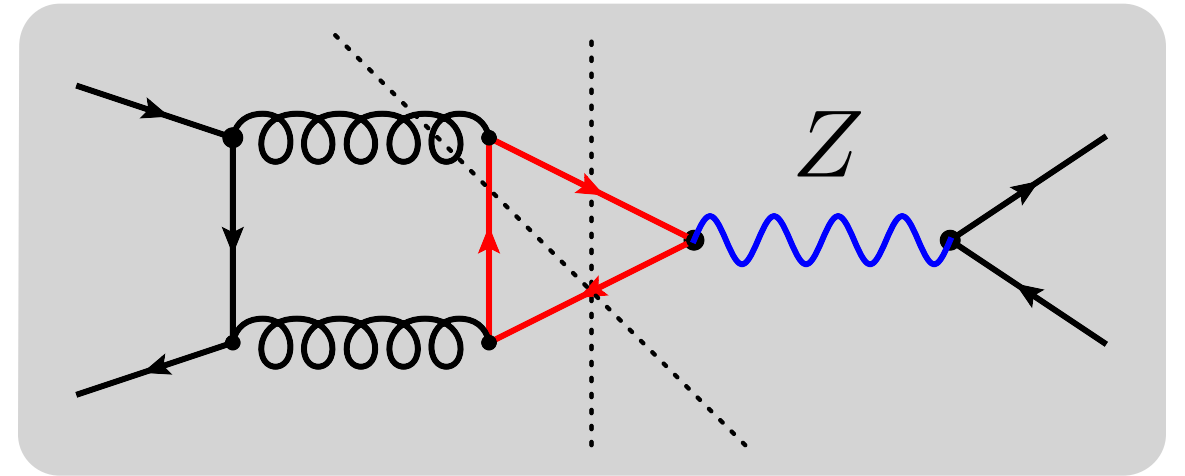
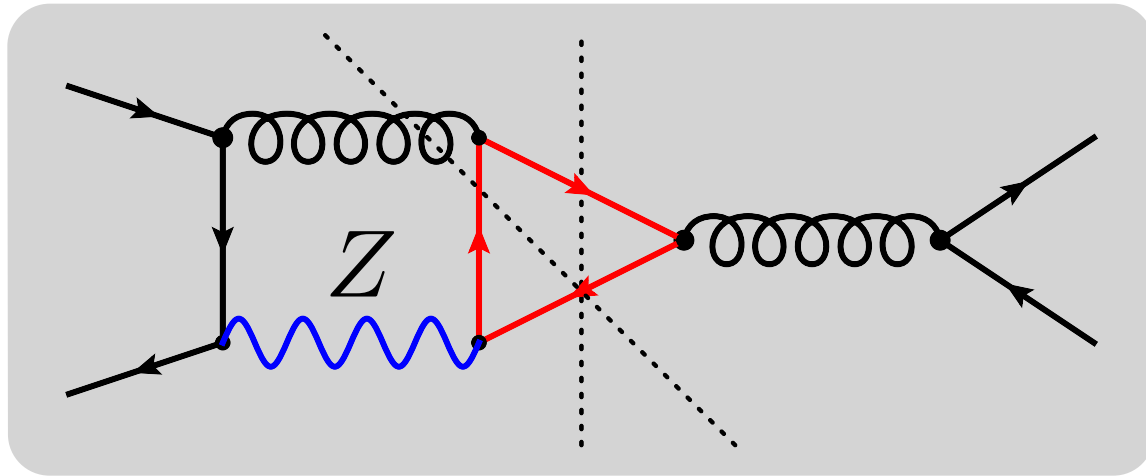
$$(\Im \mathcal{M}_A) \cdot \mathcal{M}_{\text{LO}}^*$$

- Compute squared matrix elements (use FeynArts and FormCalc)
- Evaluate virtual (using OneLOops package - dim reg)
- Compute soft function (integrate gluon PS in d-dim to Ecut)
- Combine virtual+soft and real emission into Integrand
- Link to LHAPDF and do integration with VEGAS (CUBA library)

$$\mu_W^2 = M_W^2 - iM_W\Gamma_W, \quad \mu_Z^2 = M_Z^2 - iM_Z\Gamma_Z$$

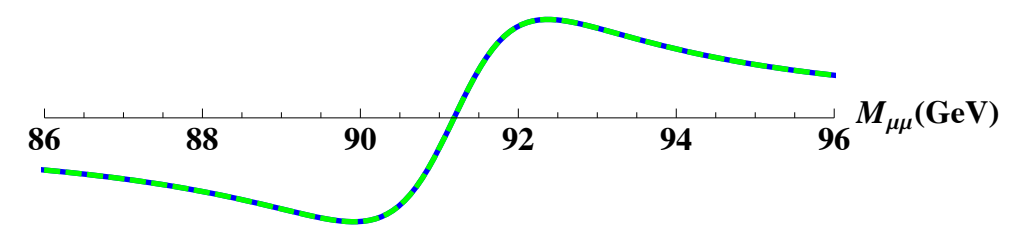
$$c_w^2 = 1 - s_w^2 = \mu_W^2 / \mu_Z^2$$

# Resonant contributions



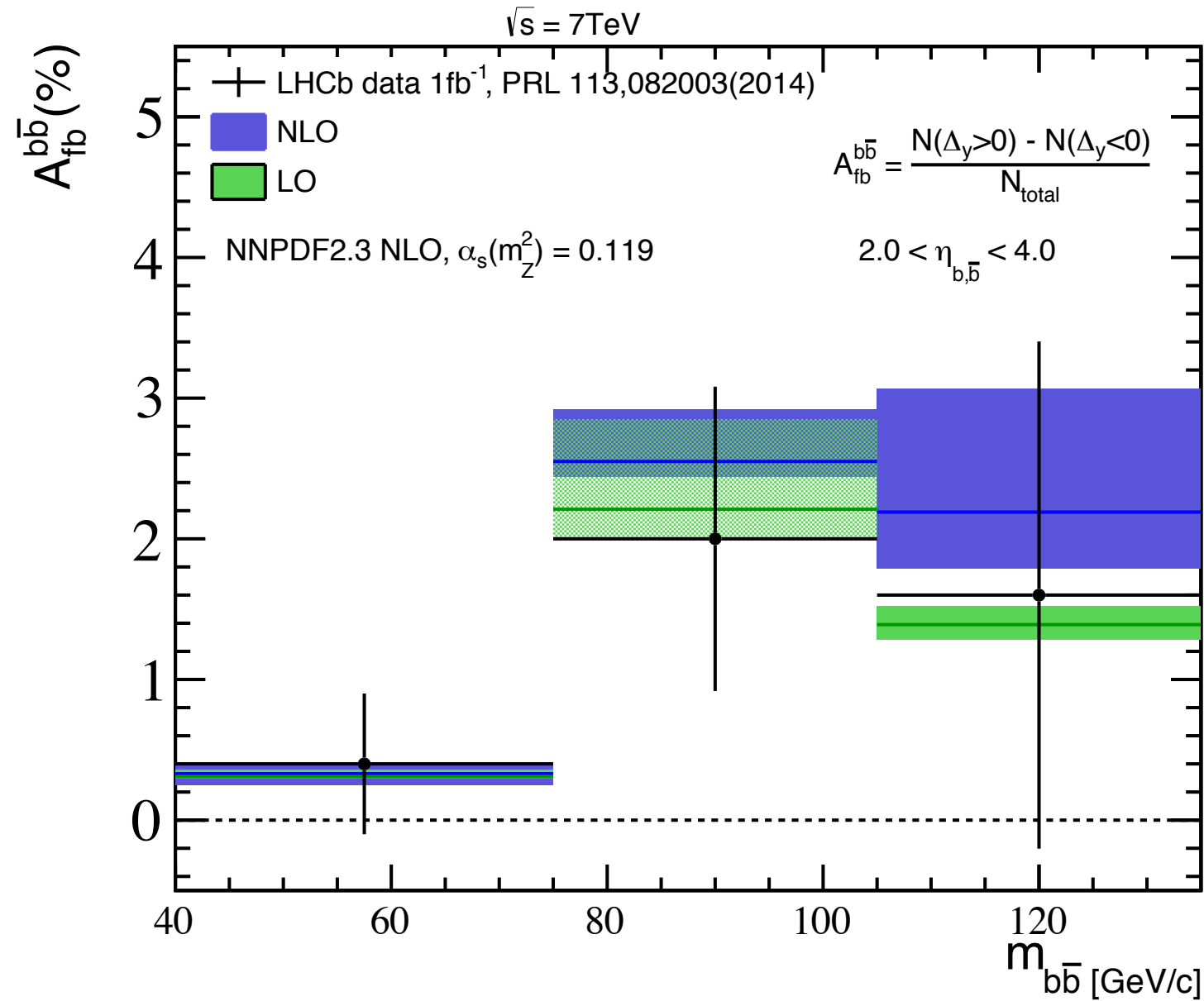
$$Q_u^{\text{WEAK}} = \frac{1}{2} - \frac{4}{3} s_w^2$$

$$Q_d^{\text{WEAK}} = -\frac{1}{2} + \frac{2}{3} s_w^2$$



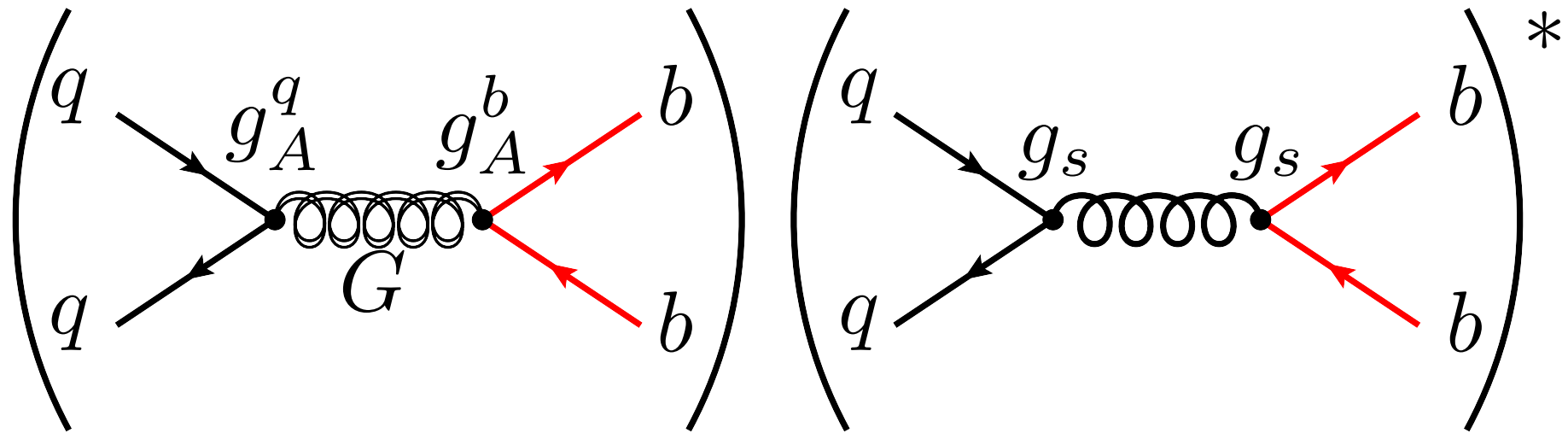
PDF cancellation (2up 1down)  
Cancellation integrating over res.

# Preliminary Result



$$A_{\text{FC}}^{Q\bar{Q}} = \frac{\alpha_s^3 \sigma_a^{s(0)} + \alpha_s^2 \alpha \sigma_a^{se(0)} + \alpha^2 \left( \sigma_a^{e(0)} + \alpha_s \sigma_a^{e(1)} \right)}{\alpha_s^2 \left( \sigma_s^{s(0)} + \alpha_s \sigma_s^{s(1)} \right) + \alpha^2 \left( \sigma_s^{e(0)} + \alpha_s \sigma_s^{e(1)} \right)}.$$

# Future measurements at 13 TeV



Example: ‘light axigluon’ with flavour universal couplings

G. Marques Tavares, M. Schmaltz, Phys. Rev. D 84 (2011) 054008

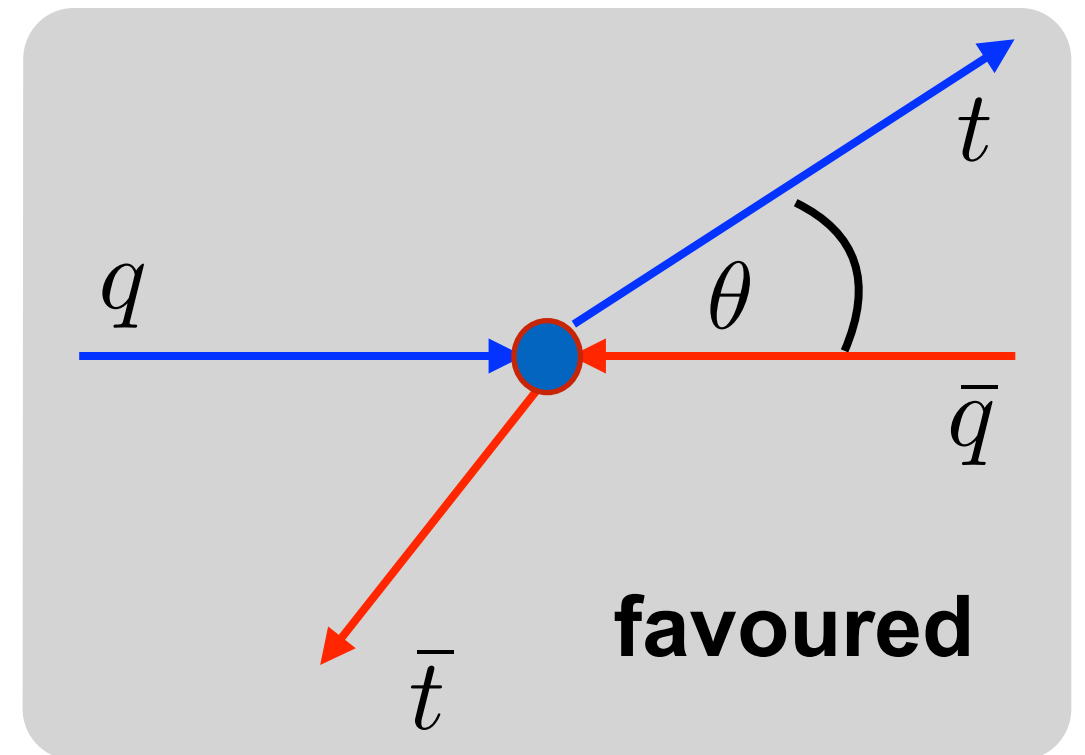
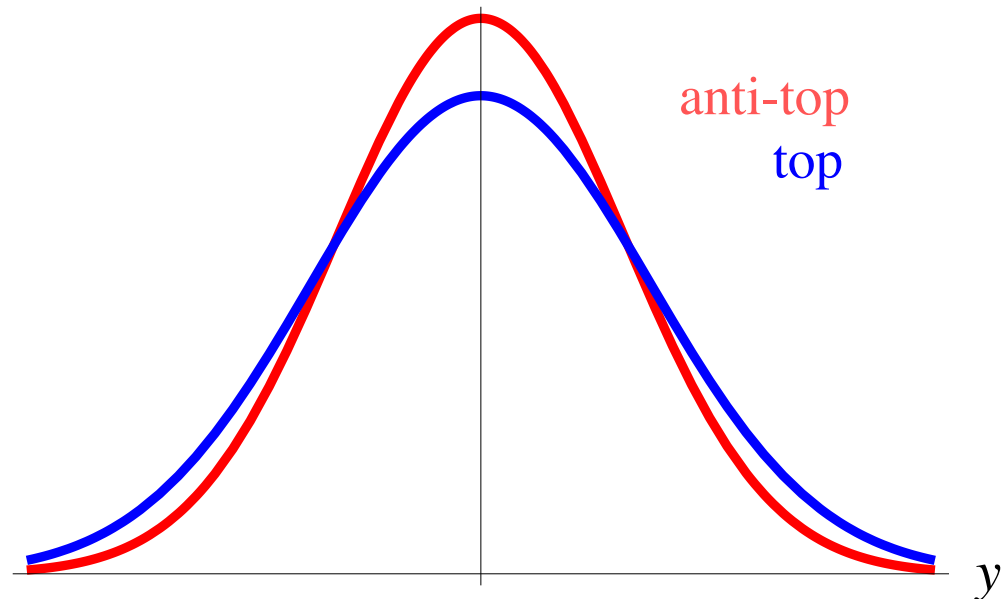
$$M_G < M_{t\bar{t}} , \quad g_A^q g_A^{b,t} > 0$$

What about tension in precision Electroweak observables?

	SM	Exp.
$A_{\text{FB}}^b$	$0.1032^{+0.0004}_{-0.0006}$	$0.0992 \pm 0.0016$
$R_b$	$0.21474 \pm 0.00003$	$0.21629 \pm 0.00066$

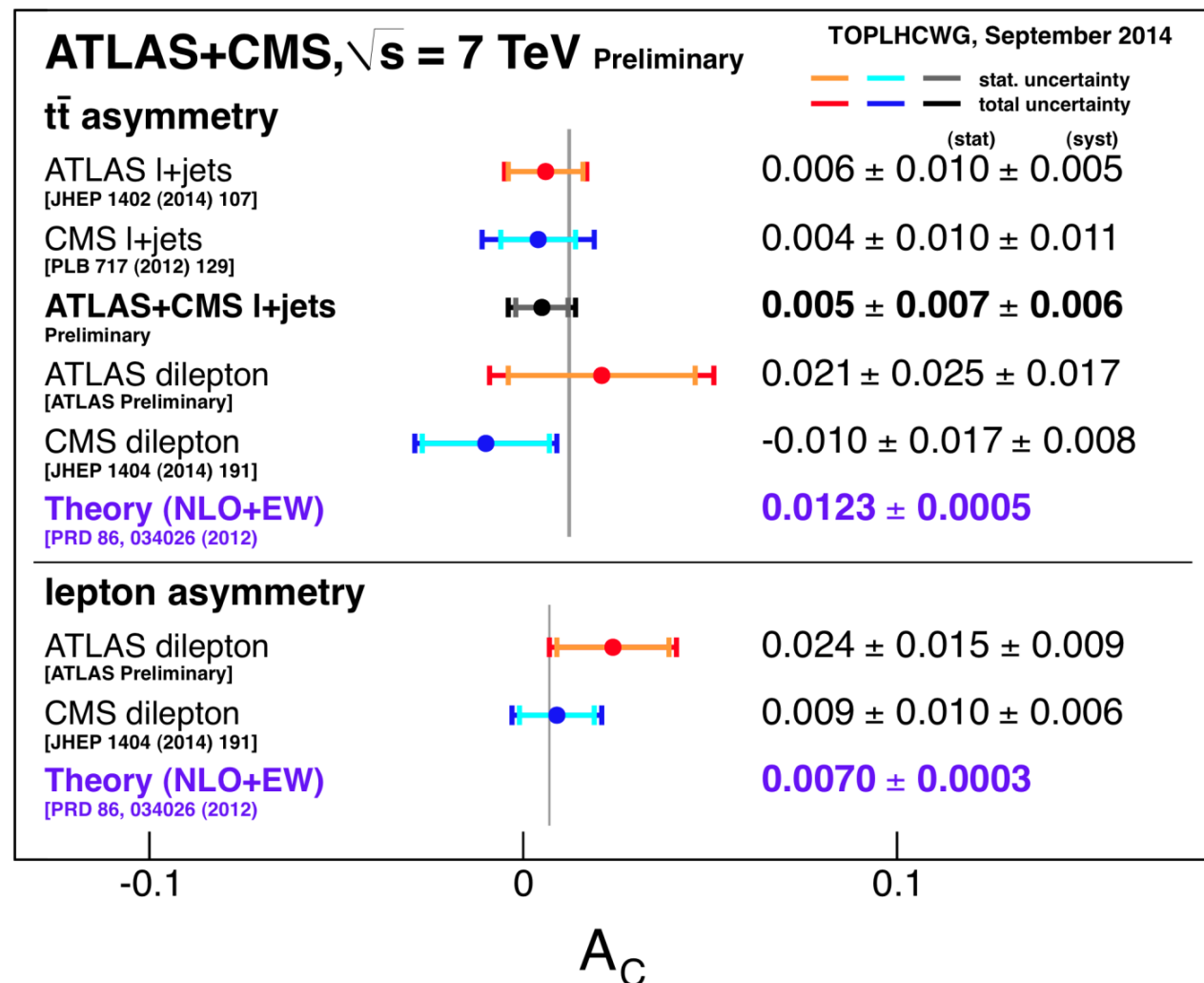
# Results from ATLAS/CMS

LHC  $pp \rightarrow t\bar{t}$



- Results consistent with SM / 0
  - Heavily diluted by gluon-fusion
- $$A_C < 1\%, \quad \delta A_{\text{syst}} \simeq 0.5\%$$

- Need better observables



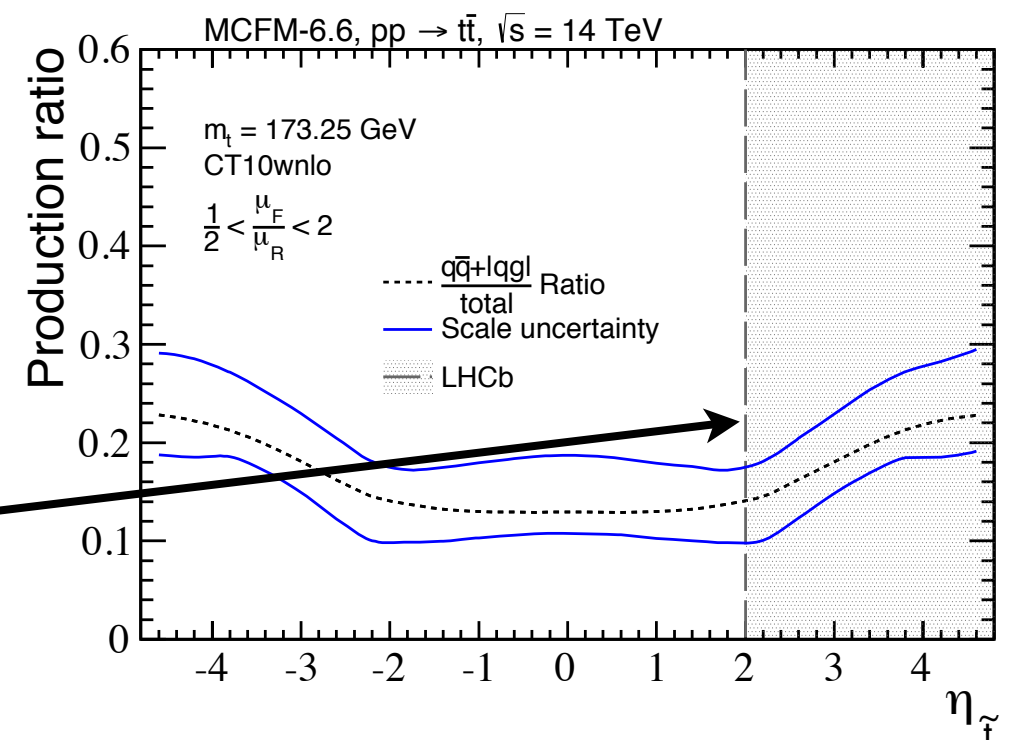
# Proposals to overcome dilution

- S. Berge and S. Westhoff, JHEP 1307 (2013) 179  
“Incline asymmetry” and the “Energy asymmetry”
- J. Anguilar-Saavedra, E. Ivarez, A. Juste, and F. Rubbo. JHEP 1404 (2014) 188  
Associated production  $pp \rightarrow t\bar{t}\gamma$
- F. Maltoni, M. Mangano, I. Tsinikos, M. Zaro. PLB 736 (2014) 252,  
Associated production  $pp \rightarrow t\bar{t}W^{\pm}$
- A. L. Kagan, J. F. Kamenik, G. Perez, and S. Stone. Phys. Rev. Lett. 107 (2011) 082003  
Measure the asymmetry at LHCb

Production mechanism ratio:

$$\frac{q\bar{q} + |qg|}{total}$$

LHCb probes unique region





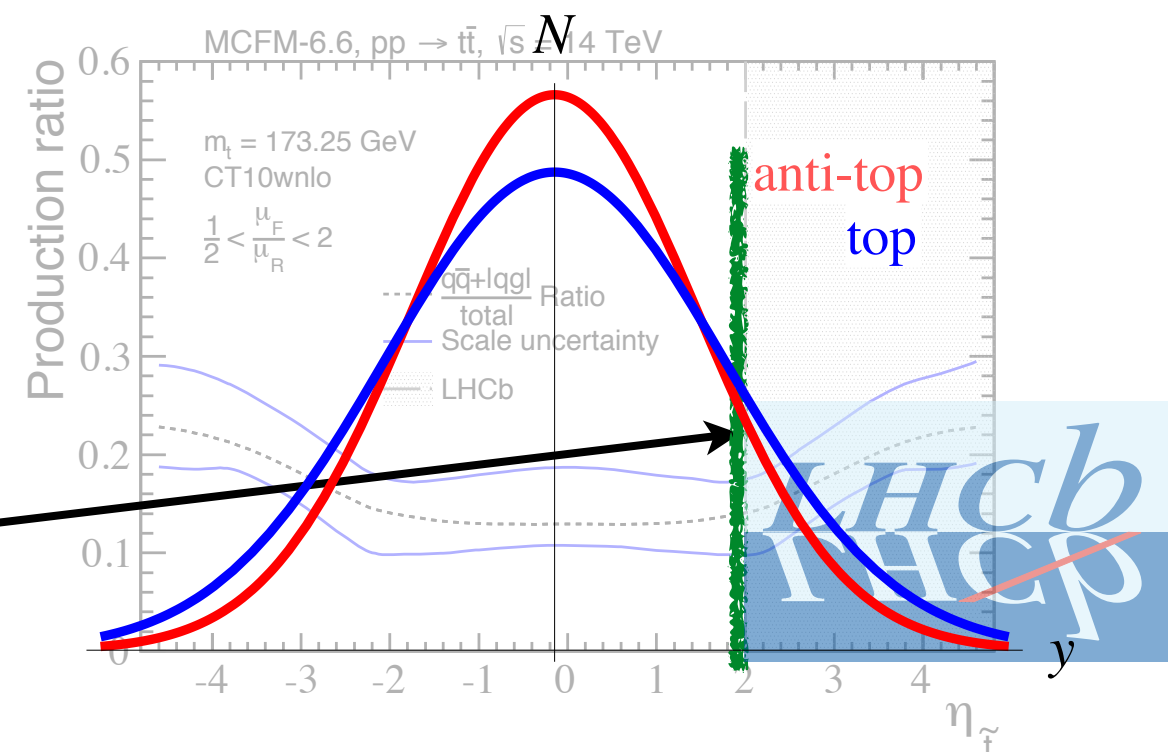
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# Asymmetry prediction for LHCb

Main contribution - interference of NLO amplitudes!

$$A = \frac{\alpha_s^3 \sigma_a^{s(1)} + \alpha_s^2 \alpha_{e/w} \sigma_a^{e/w(1)} + \alpha_{e/w}^2 \sigma_a^{e/w(0)} + \dots}{\alpha_s^2 \sigma_s^{s(0)} + \alpha_s^3 \sigma_s^{s(1)} + \dots},$$

$$= \alpha_s \frac{\sigma_a^{s(1)}}{\sigma_s^{s(0)}} + \alpha_{e/w} \frac{\sigma_a^{e/w(1)}}{\sigma_s^{s(0)}} + \frac{\alpha_{e/w}^2}{\alpha_s^2} \frac{\sigma_a^{e/w(0)}}{\sigma_s^{s(0)}} + \dots$$

$$\sigma_s^{s(0)} = \text{symmetric LO cross section (coupling stripped)}$$

$$\sigma_a^{x(1)} = \text{asymmetric NLO cross section (coupling stripped)}$$

arXiv:hep-ph/9802268, arXiv:hep-ph/9807420, arXiv:1109.6830, J.H.Kuhn, G. Rodrigo

arXiv:1107.2606, W. Hollik and D. Pagani,

arXiv:1205.6580, W. Bernreuther and Z.-G. Si

arXiv:1302.6995, B. Grinstein, C. W. Murphy

arXiv:1409.8631, RG

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$$= \boxed{\alpha_s \frac{\sigma_a^{s(1)}}{\sigma_s^{s(0)}}} + \boxed{\alpha_{e/w} \frac{\sigma_a^{e/w(1)}}{\sigma_s^{s(0)}}} + \boxed{\frac{\alpha_{e/w}^2}{\alpha_s^2} \frac{\sigma_a^{e/w(0)}}{\sigma_s^{s(0)}}} + \dots$$

1) Obtain QCD from MCFM, [arXiv:1204.1513](https://arxiv.org/abs/1204.1513) J. Campbell, R. K. Ellis

2) Apply rescaling of couplings and colour factors

$$R_{q\bar{q}}^X(\mu) = \frac{36 Q_q^X Q_t^X \alpha_e}{5 \alpha_s}, \quad R_{qg}^X(\mu) = \frac{24 Q_q^X Q_t^X \alpha_e}{5 \alpha_s}.$$

$$Q^w = (2\tau^3 - 4s_w^2 Q^e)/4s_w c_w$$

3) Its just LO...

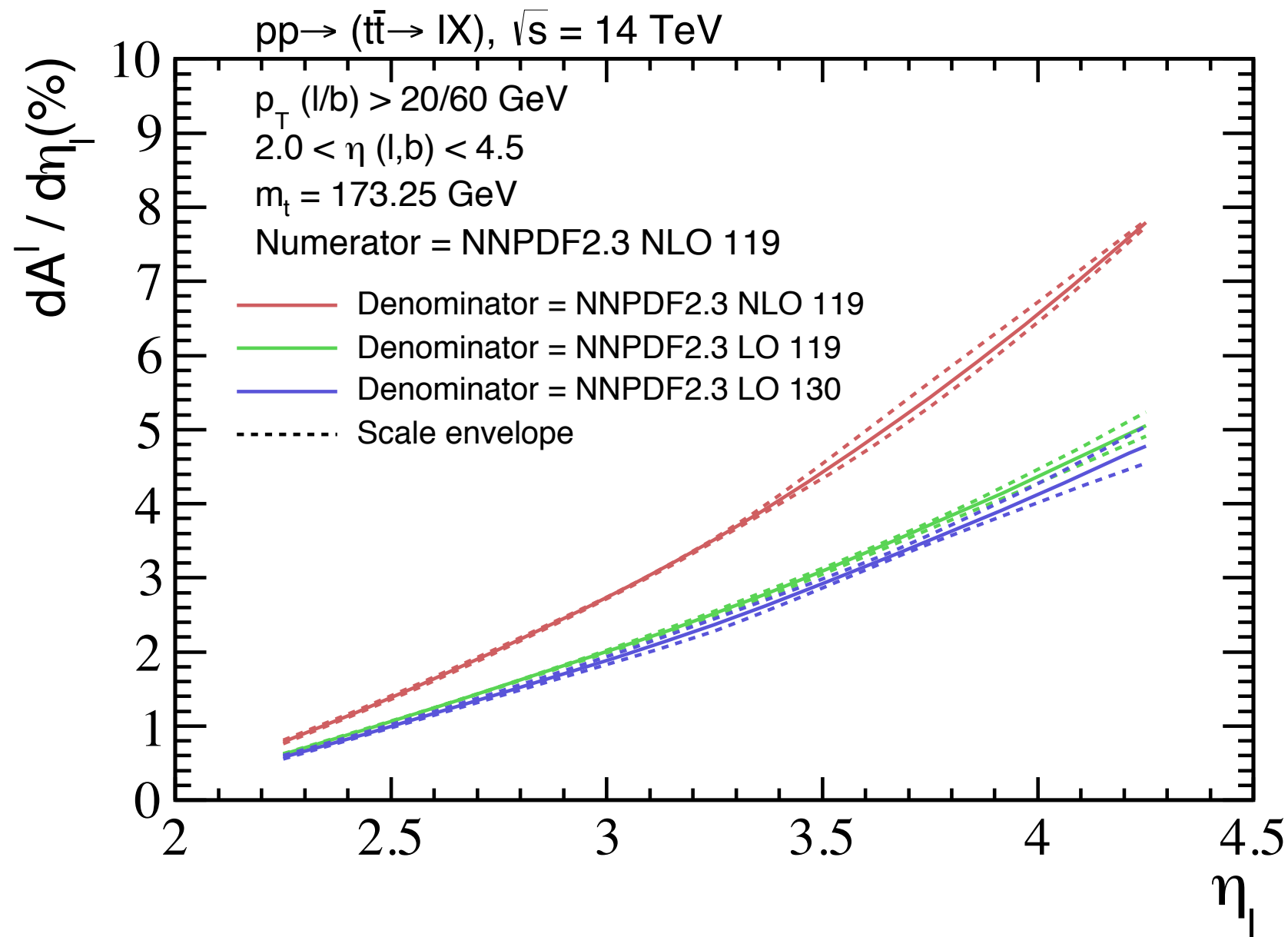
# Single-lepton asymmetry

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}/d\eta_l - d\sigma^{l^-b}/d\eta_l}{d\sigma^{l^+b}/d\eta_l + d\sigma^{l^-b}/d\eta_l} \right)$$

$$2.0 < \eta(l, b) < 4.5$$

$$p_T(l/b) > 20/60 \text{ GeV}$$

$$\Delta R(l^\pm, \text{jet}) \geq 0.5$$



$$A^l = (1.4 - 2.0)\%$$

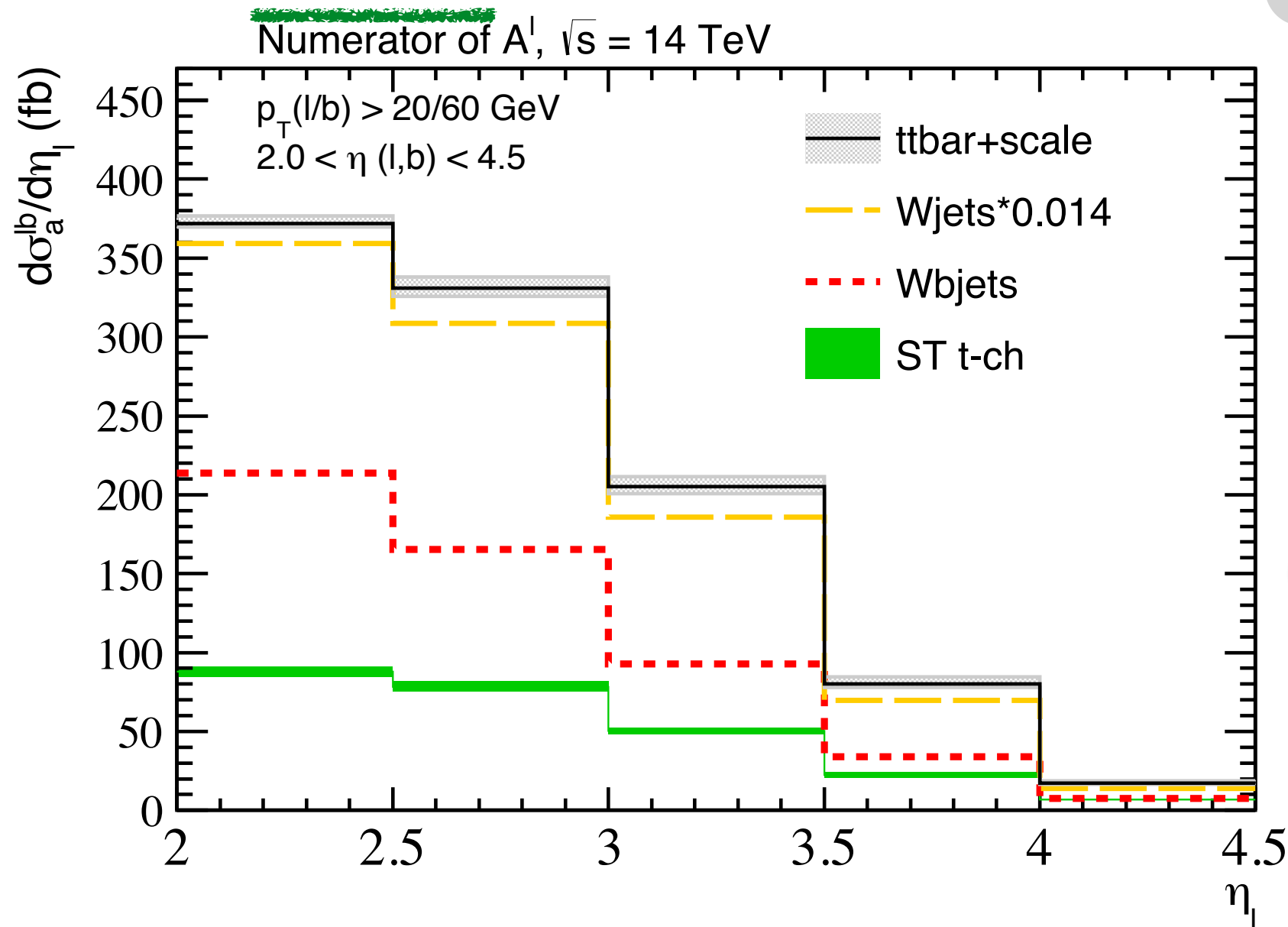
# Backgrounds

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}/d\eta_l - d\sigma^{l^-b}/d\eta_l}{d\sigma^{l^+b}/d\eta_l + d\sigma^{l^-b}/d\eta_l} \right)$$

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$$p_T(l/b) > 20/60 \text{ GeV}$$

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Fit backgrounds  
 experimentally:  
 $l^\pm j, l^\pm bj, l^\pm bb$   
 control channels

# Statistical feasibility

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}/d\eta_l - d\sigma^{l^-b}/d\eta_l}{d\sigma^{l^+b}/d\eta_l + d\sigma^{l^-b}/d\eta_l} \right)$$

$$\begin{aligned} 2.0 < \eta(l, b) < 4.5 \\ p_T(l/b) > 20/60 \text{ GeV} \\ \Delta R(l^\pm, \text{jet}) \geq 0.5 \end{aligned}$$

If backgrounds can be controlled!

$$\sigma^{\text{LO}} \simeq 4.7 \text{ pb}$$

$$\int \mathcal{L} dt = 50 \text{ fb}^{-1}$$

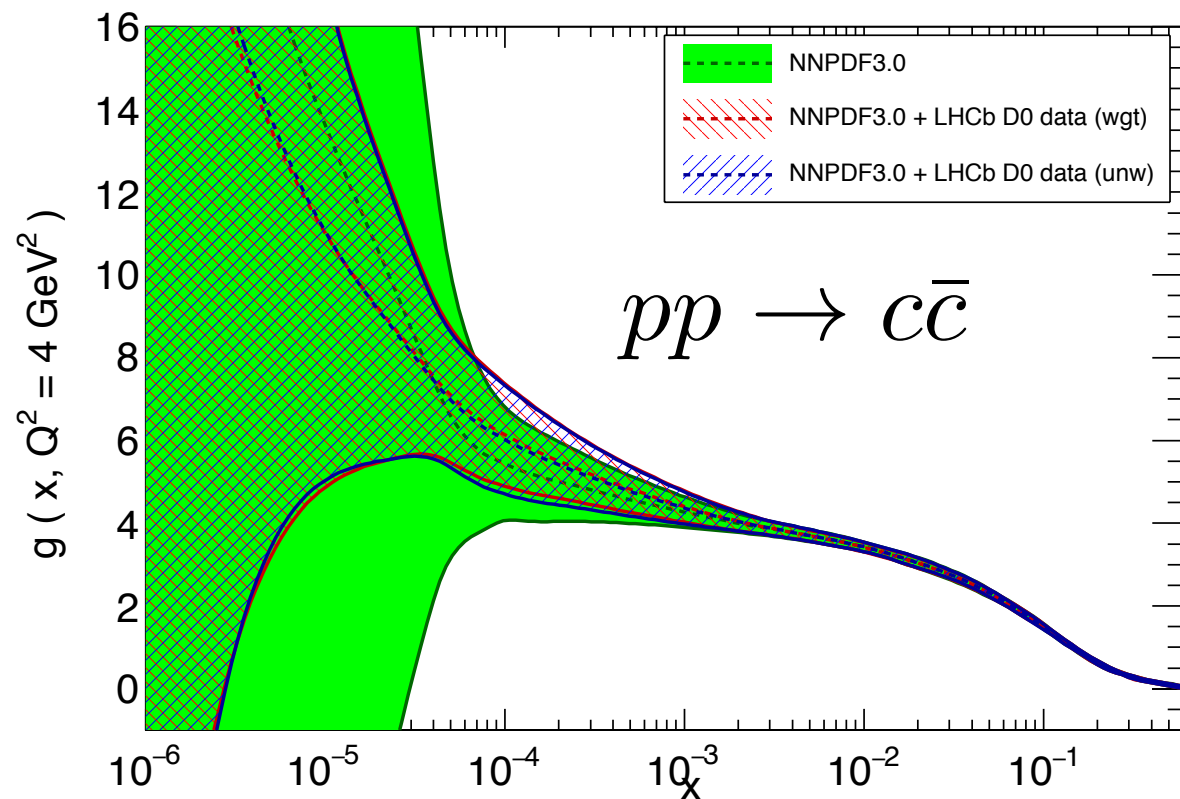


Apply b-tagging efficiency 0.7  
Apply lepton efficiency 0.75

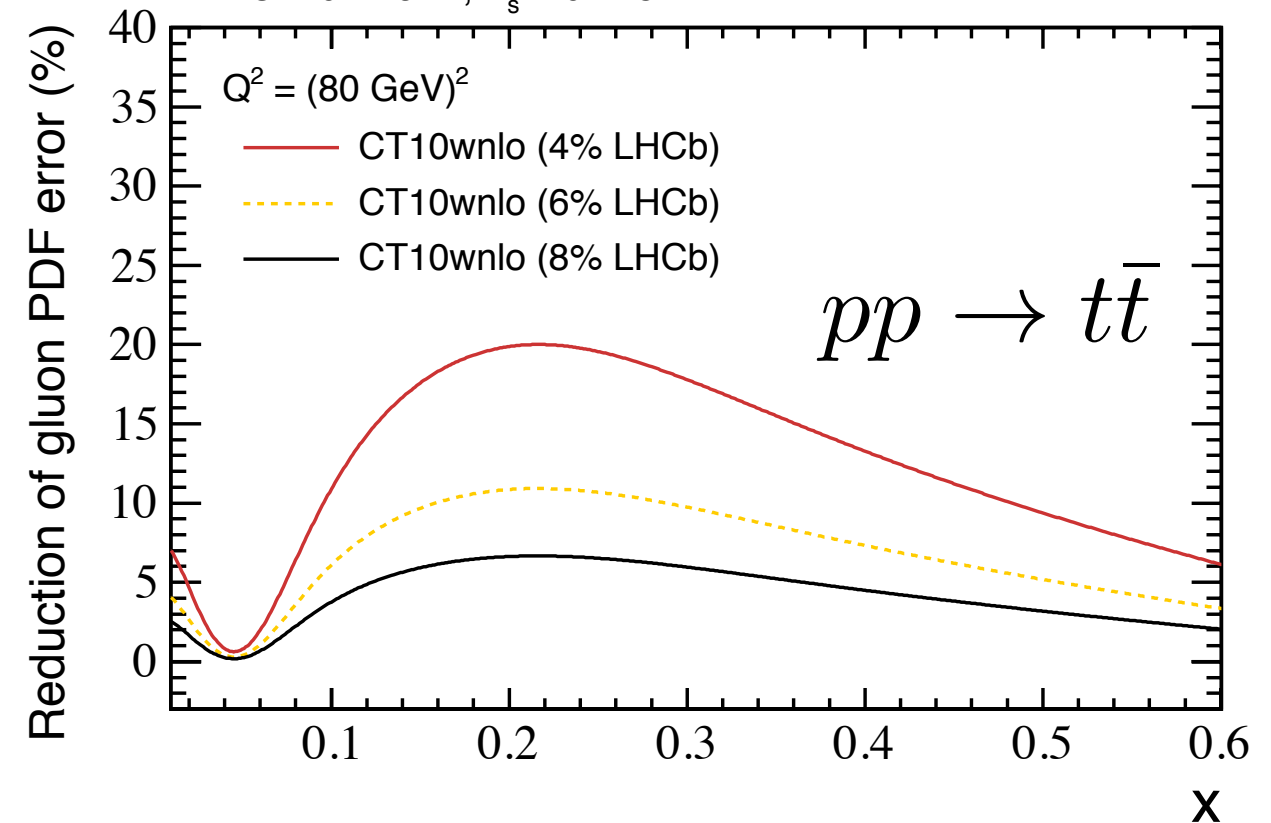
$$N_{\text{events}} \simeq 1.2e5$$

$$A^l = (1.4 - 2.0) \pm 0.3\%$$

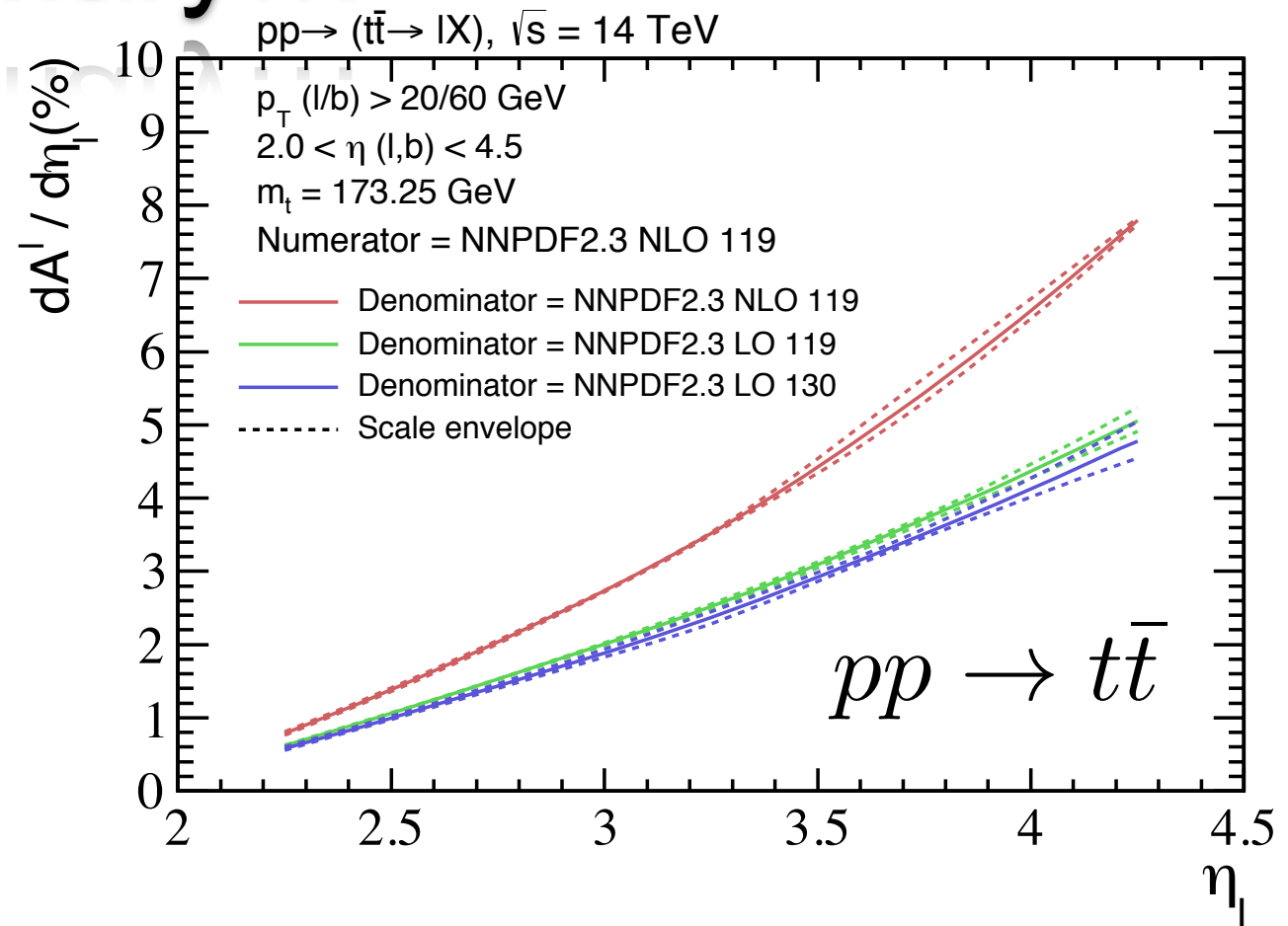
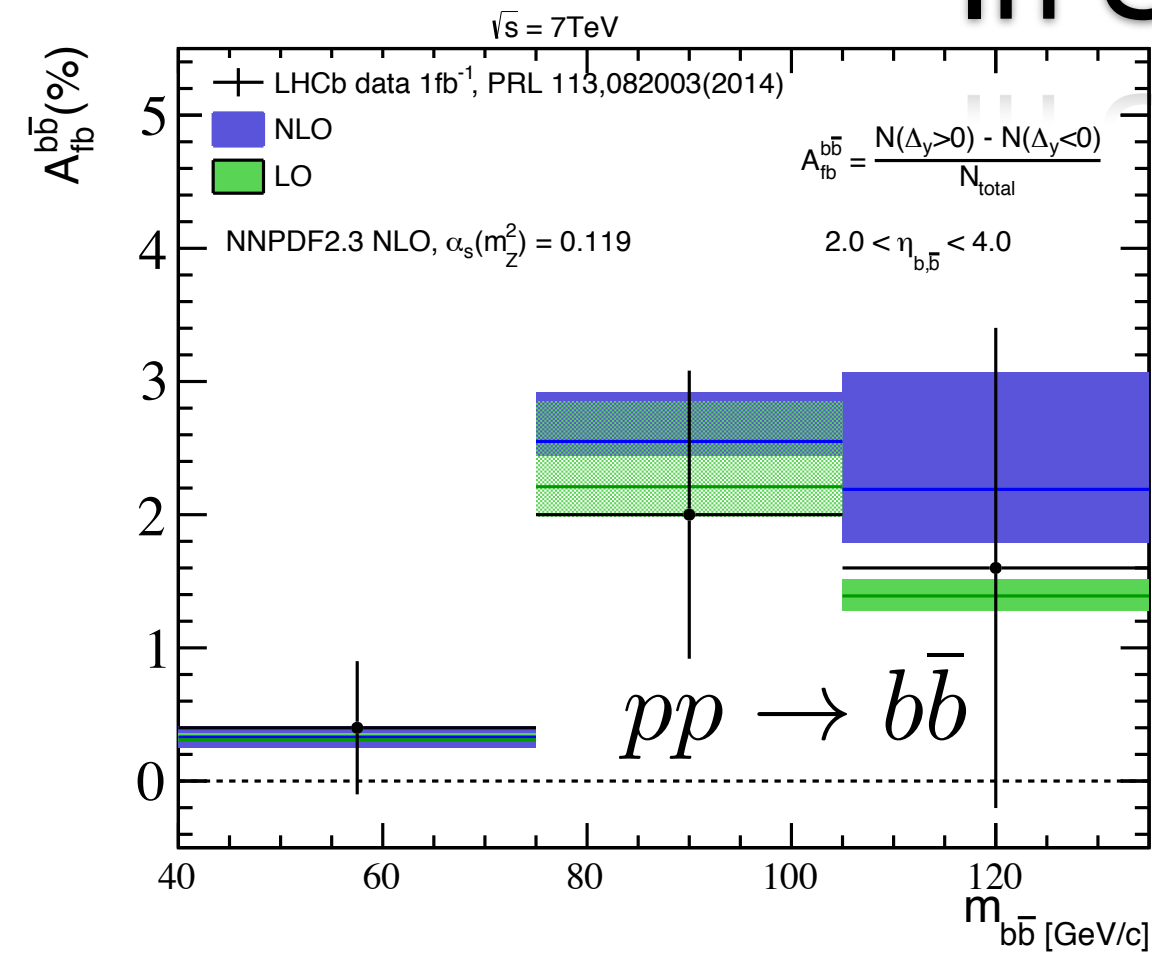
NNPDF3.0 NLO  $\alpha_s=0.118$



CT10wnlo  $1\sigma$ ,  $\alpha_s = 0.118$



## In Summary...



**Thanks for listening**



# D measurement (arXiv: 1302.2864)

LHCb data compared with:

**FONLL** - Fixed-Order + Resummation

Cacciari, Greco, Nason hep/ph:9803400

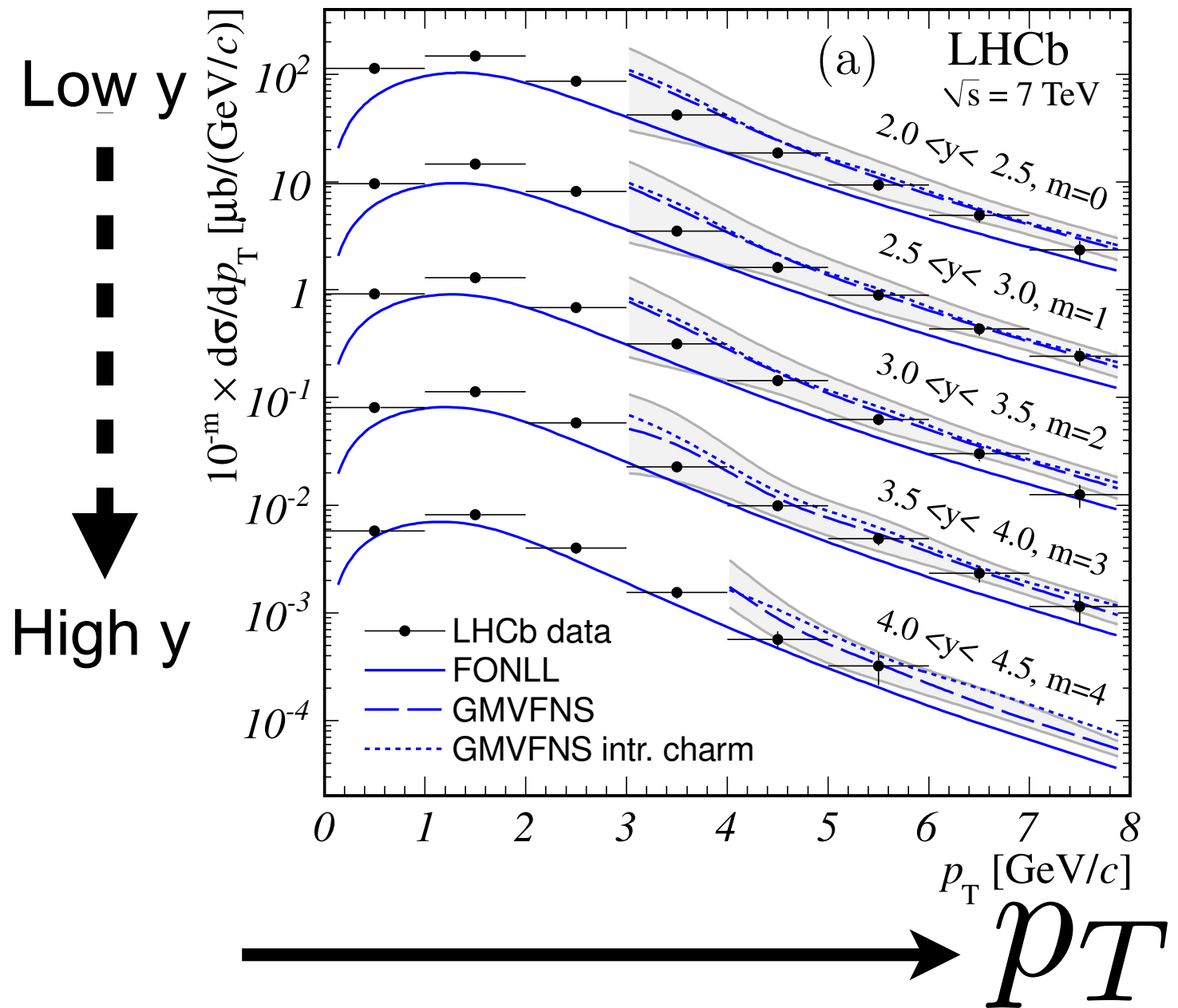
Web implementation:

<http://www.lpthe.jussieu.fr/~cacciari/fonll/fonllform.html>

Cacciari, Frixione, Houdeau, Mangano, Nason and Ridolfi hep-ph:1205.6344

**GMVFNS** - Generalised-Mass Variable-Flavour-Number-Scheme

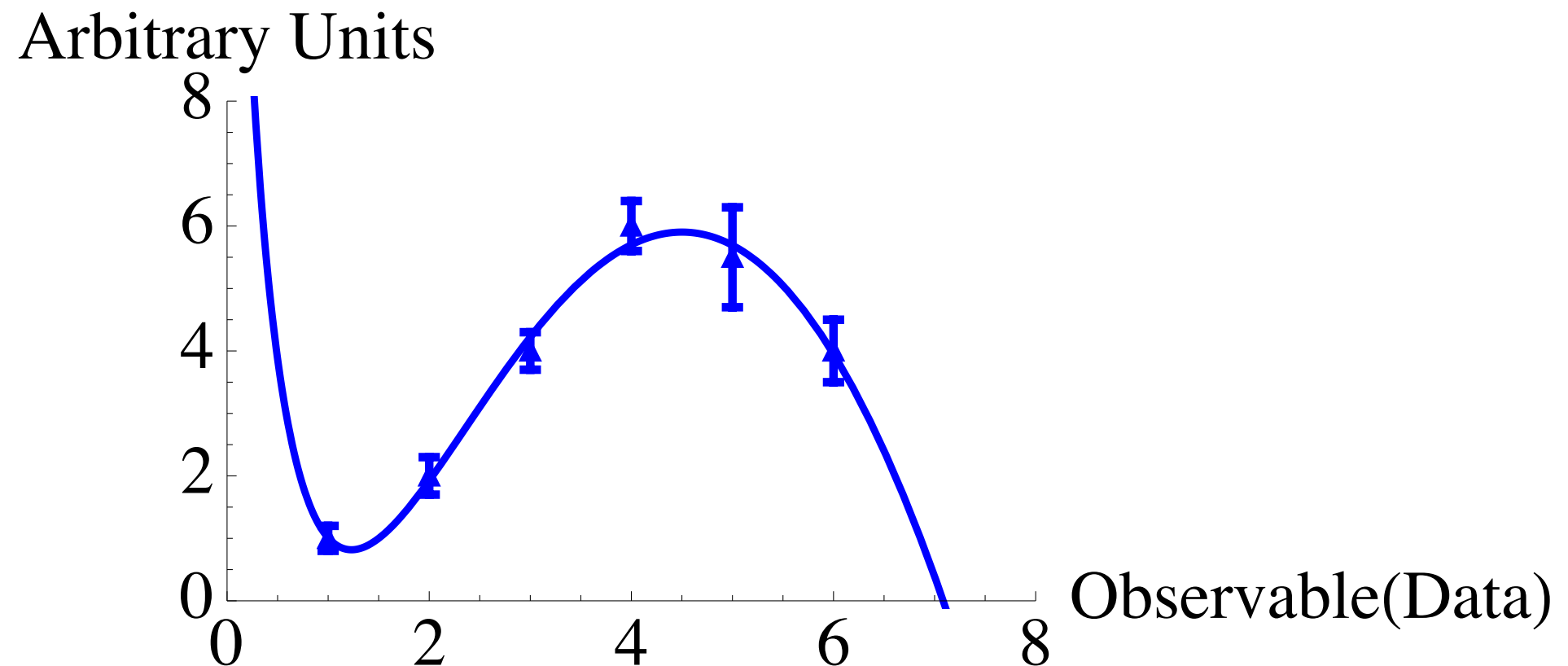
Kniehl, Kramer, Schienbein, Spiesberger hep-ph: arxiv:0901.4130 and refs. therein



$$d\hat{\sigma}_D = d\hat{\sigma}_Q \otimes \boxed{D_{Q \rightarrow D}^{\text{NP}}} \leftarrow \begin{array}{l} \text{Determined from} \\ e^+e^- \text{ data} \end{array}$$

# Wish to determine the impact of the data

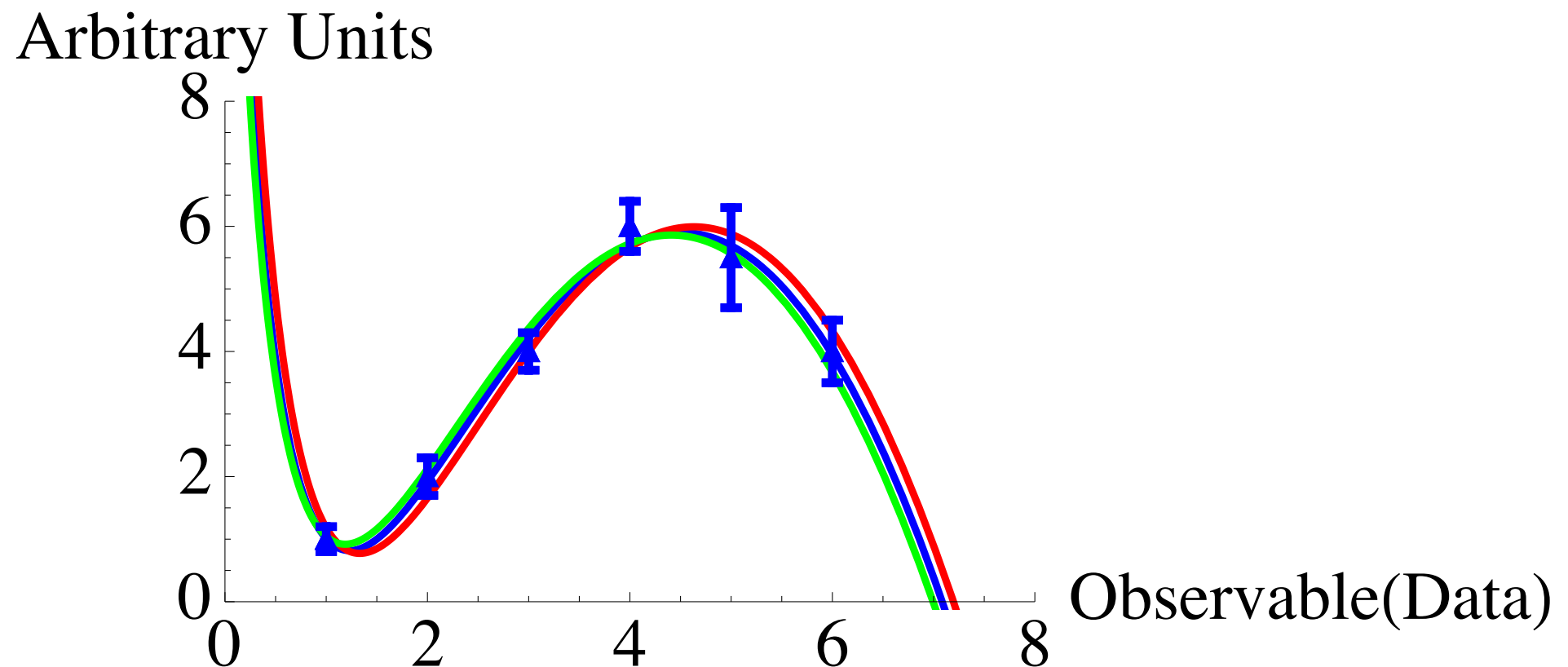
Use a reweighting technique of PDF replicas  
see - [arXiv:1012.0836](https://arxiv.org/abs/1012.0836), NNPDF collaboration  
(this is very qualitative)



1. NNPDF provide central member (from global fit)

# Wish to determine the impact of the data

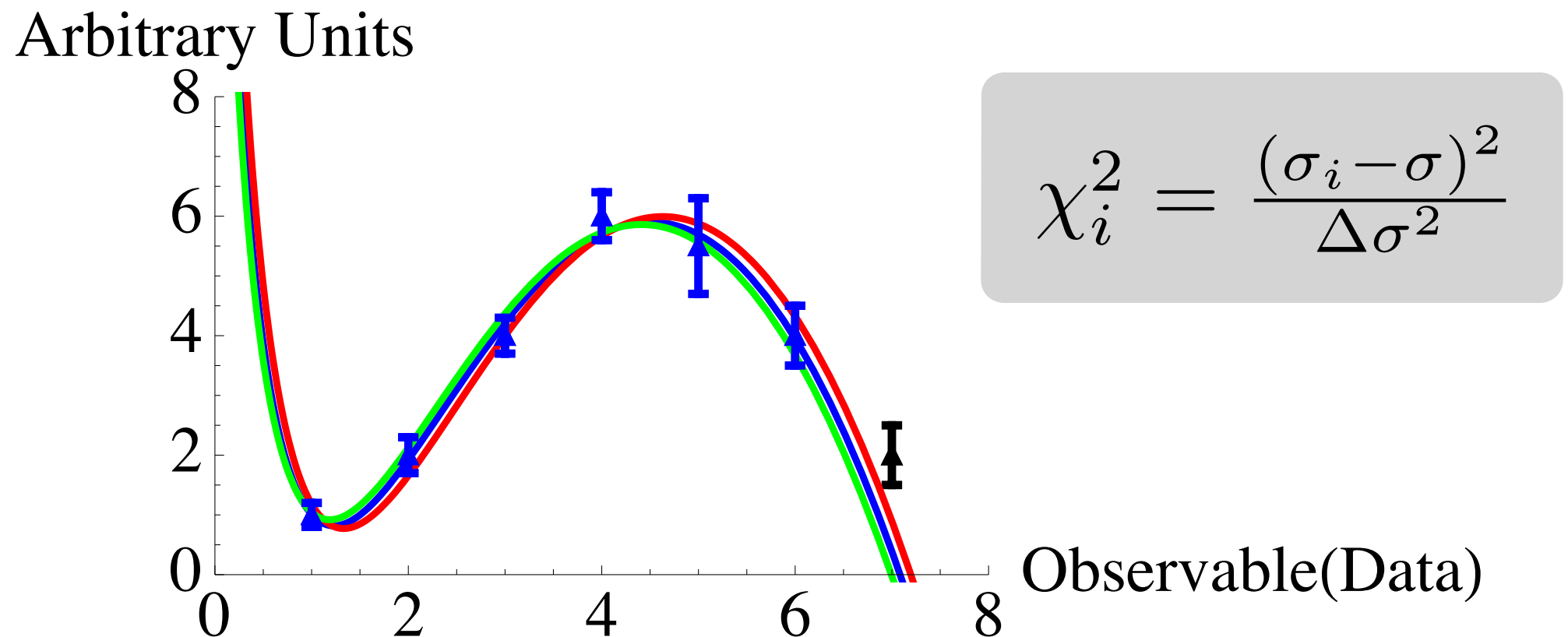
Use a reweighting technique of PDF replicas  
see - [arXiv:1012.0836](https://arxiv.org/abs/1012.0836), NNPDF collaboration  
(this is very qualitative)



1. NNPDF provide central member (from global fit)
2. NNPDF provide replica members (gives uncertainty)

# Wish to determine the impact of the data

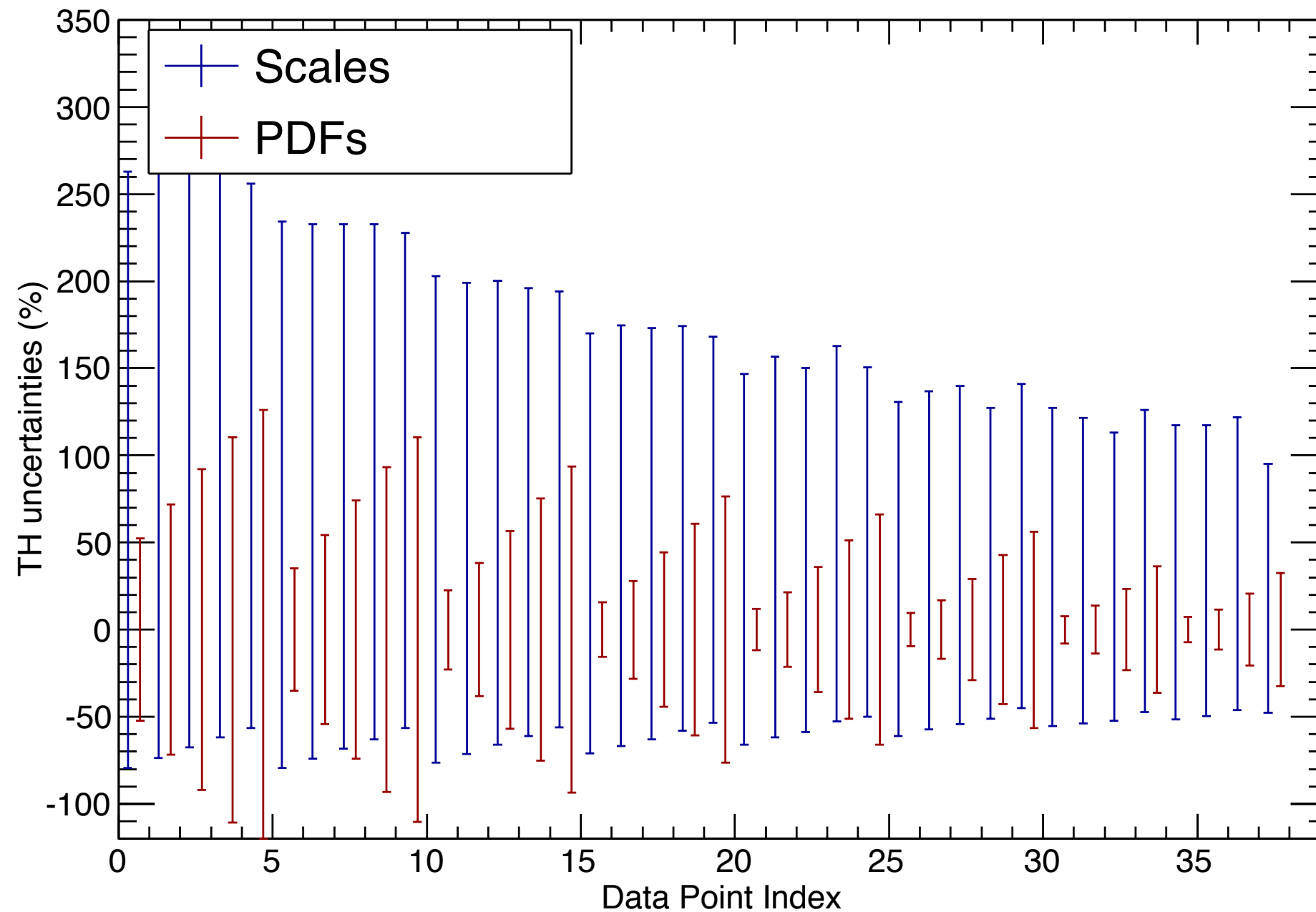
Use a reweighting technique of PDF replicas  
see - [arXiv:1012.0836](https://arxiv.org/abs/1012.0836), NNPDF collaboration  
(this is very qualitative)



1. NNPDF provide central member (from global fit)
2. NNPDF provide 100 replica members (gives uncertainty)
3. Look at the impact of a new measurement (cross section)

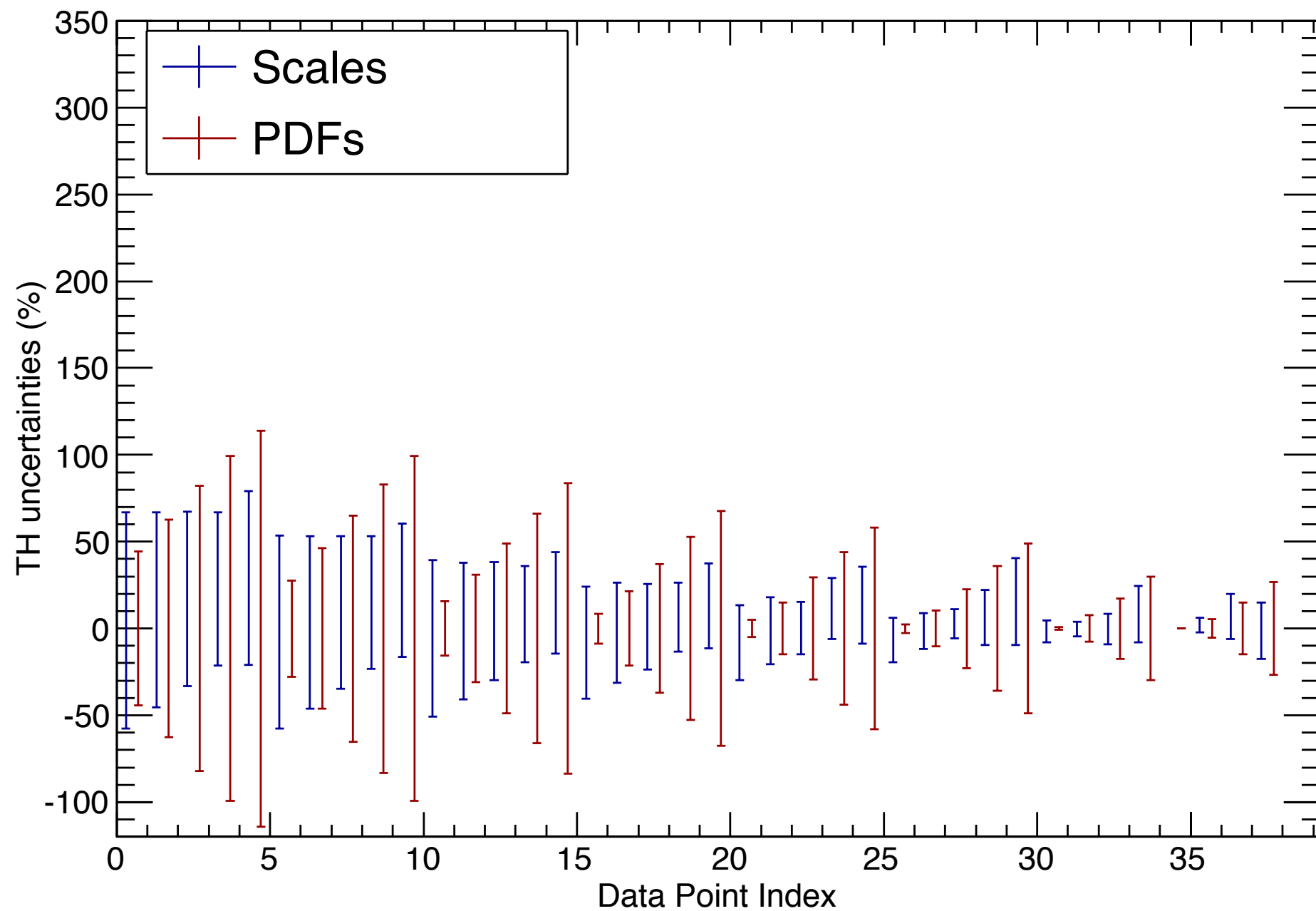
# Wish to determine the impact of the data

LHCb forward charm production, 7 TeV, D0 mesons, POWHEG



# Wish to determine the impact of the data

LHCb forward charm production, 7 TeV, D0 mesons, POWHEG

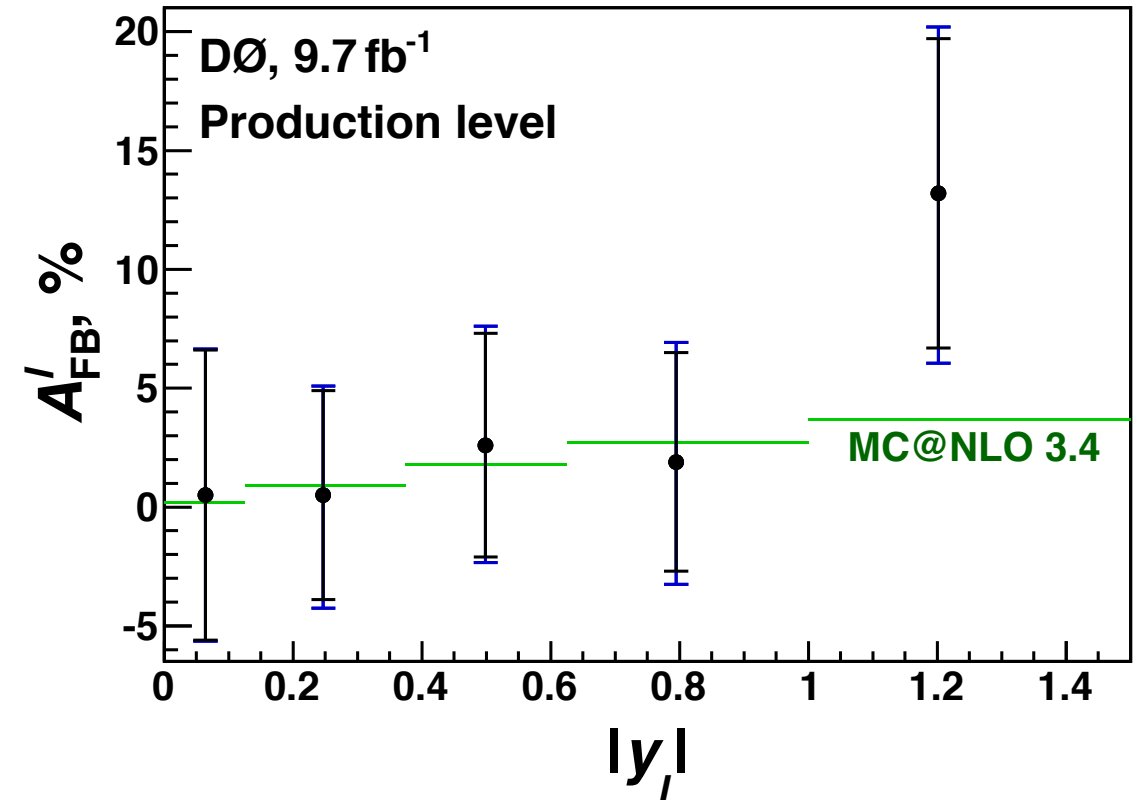
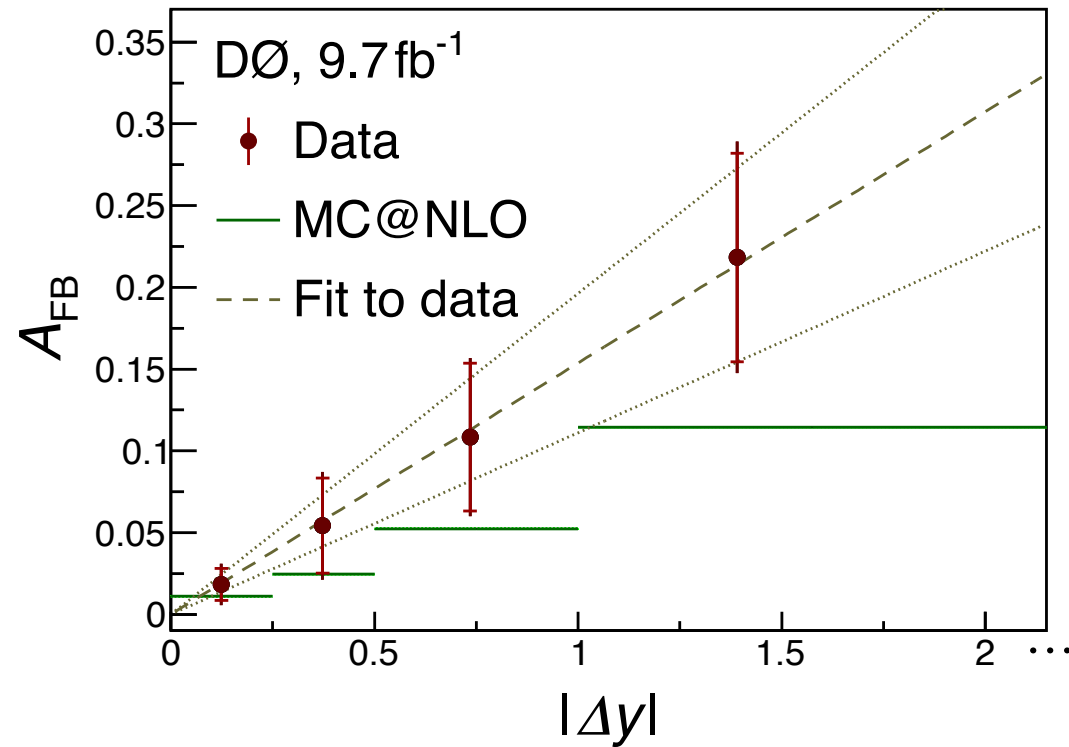


# TeVatron results differentially

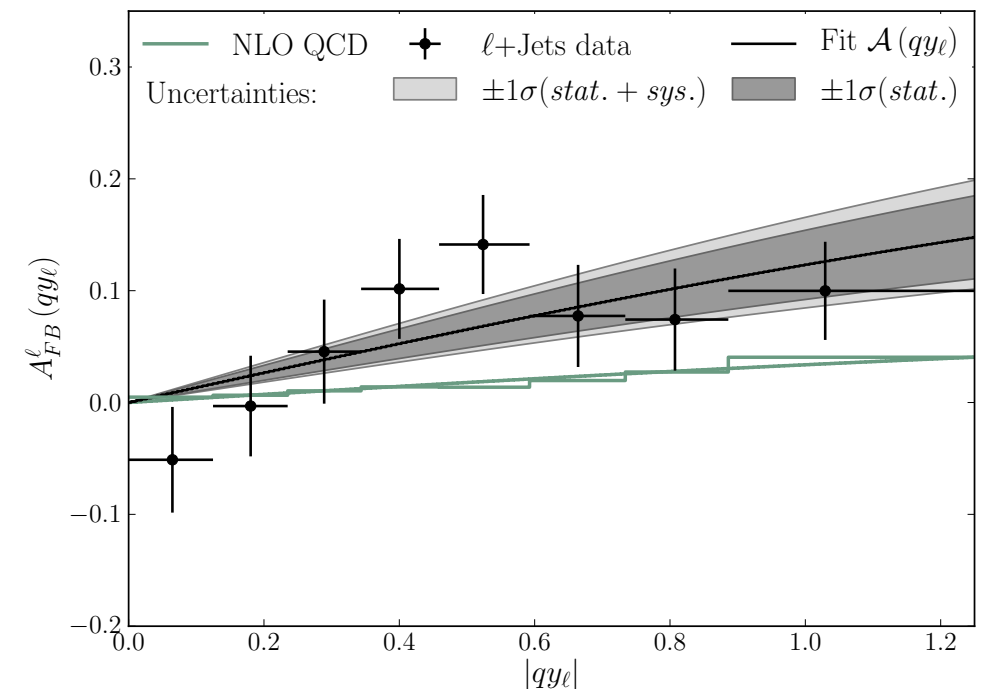
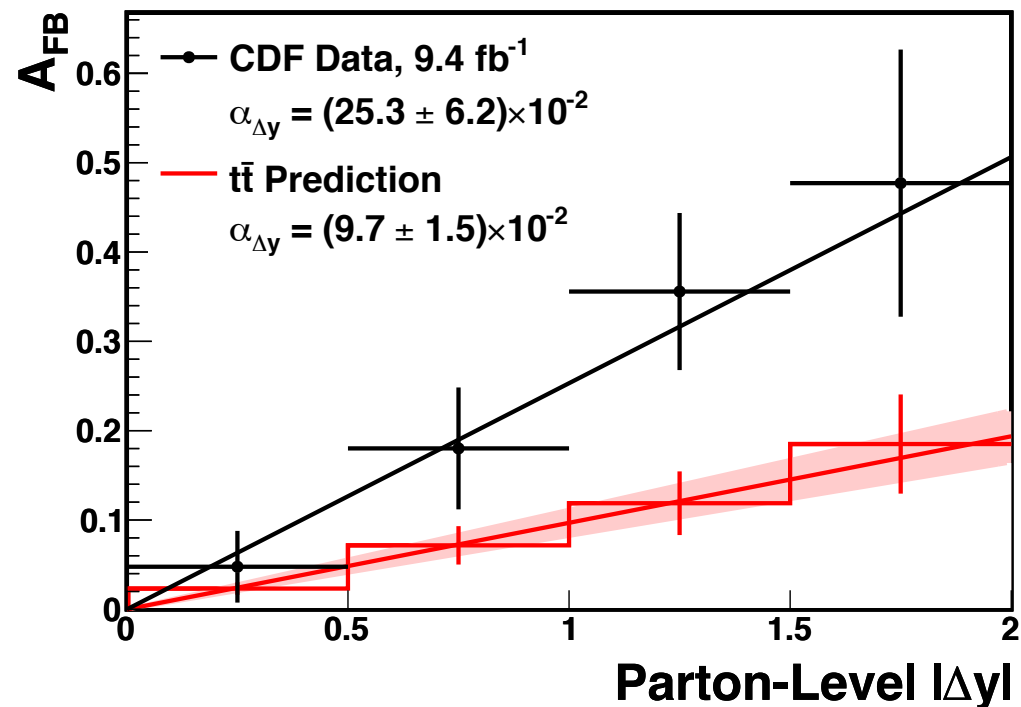
Parton level

Lepton level

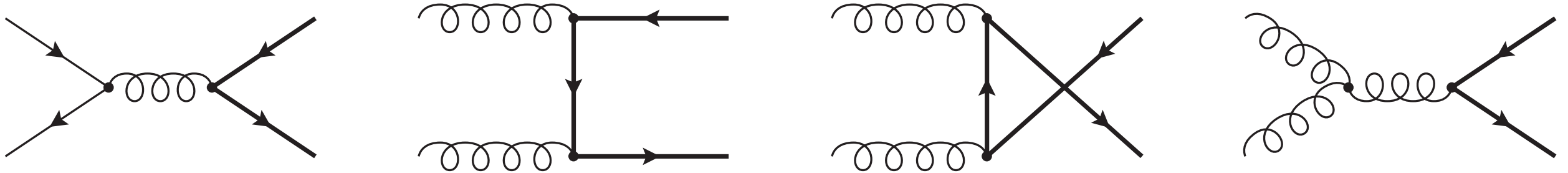
D0



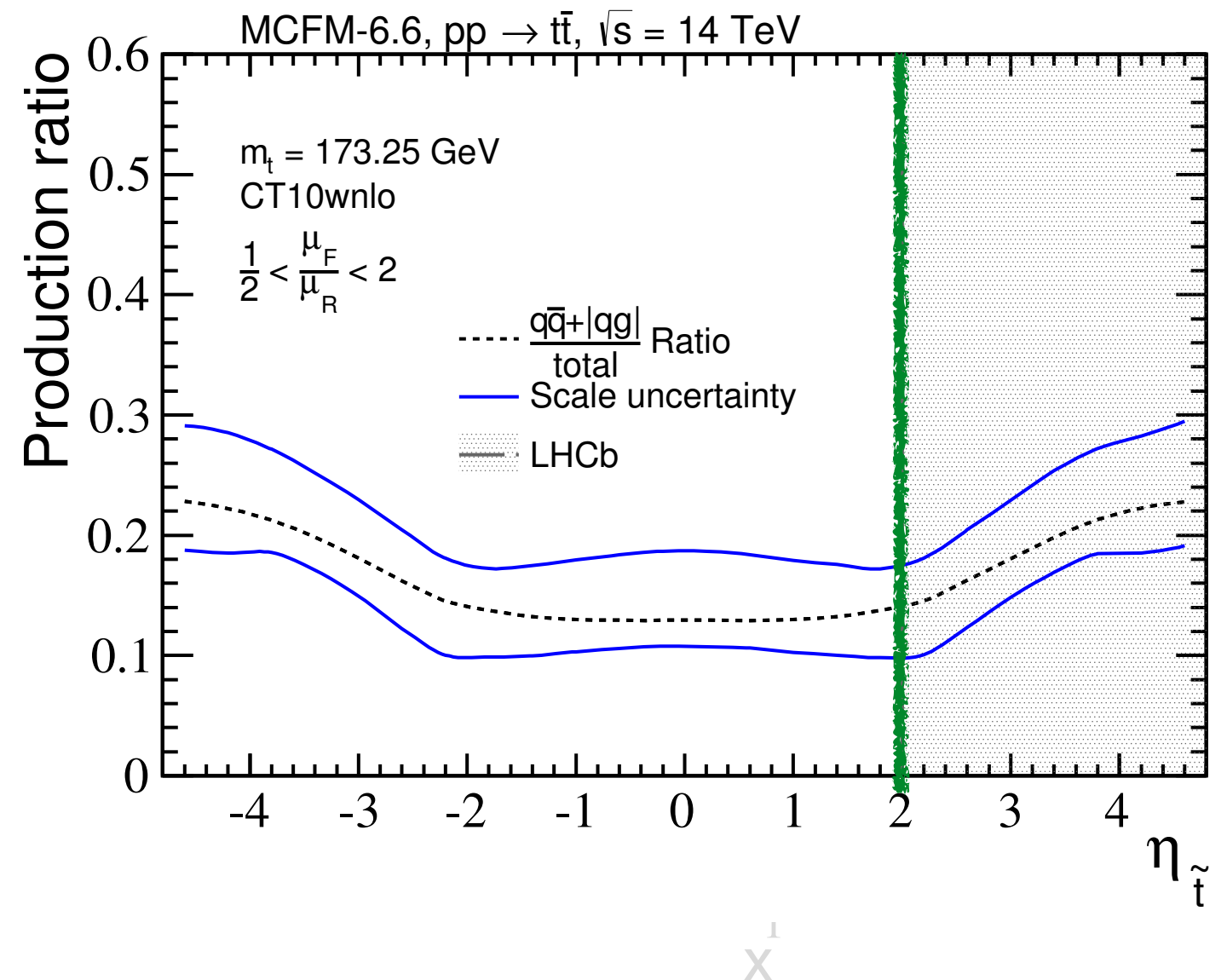
CDF



# Enriched $qX \rightarrow t+Y$ sample at LHCb



less gg-dilution  
in LHCb acceptance





# Single-lepton backups

$N^l$ (fb)		$\mu = m_t/2$	$\mu = m_t$	$\mu = 2m_t$	
$\mathcal{O}(\alpha_s^3)$	$u\bar{u}$	55.62	40.84	31.56	
	$d\bar{d}$	23.15	16.99	13.05	
	$ug$	1.79	1.02	0.65	
	$dg$	0.72	0.45	0.26	
$\mathcal{O}(\alpha_s^2\alpha_e)$		9.37	7.65	6.47	
$\approx \mathcal{O}(\alpha_s^2\alpha_w)$		0.35	0.25	0.19	
$\mathcal{O}(\alpha_{e/w}^2)$		0.81	0.78	0.77	
Total		91.80	67.96	52.95	
		$D^l$ (fb), 14 TeV			
PDF		$\mu = m_t/2$	$\mu = m_t$	$\mu = 2m_t$	$A^l$ (%)
NLO 119		4626	3512	2742	1.95 (3)
LO 119		6225	4663	3586	1.47 (1)
LO 130		6761	4961	3752	1.38 (3)

# Backgrounds

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}/d\eta_l - d\sigma^{l^-b}/d\eta_l}{d\sigma^{l^+b}/d\eta_l + d\sigma^{l^-b}/d\eta_l} \right)$$

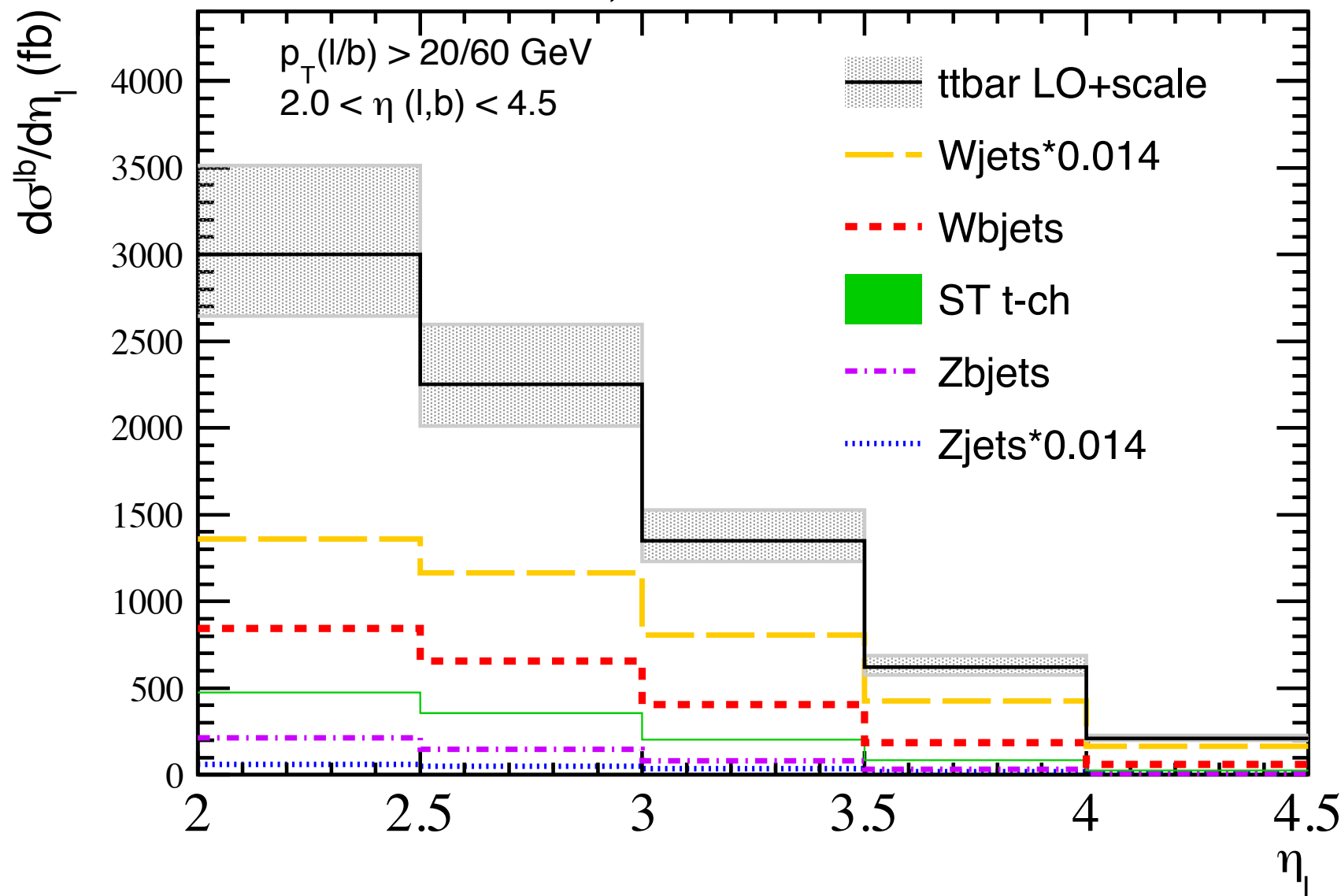
$$2.0 < \eta(l, b) < 4.5$$

$$p_T(l/b) > 20/60 \text{ GeV}$$

$$\Delta R(l^\pm, \text{jet}) \geq 0.5$$

Denominator of  $A^l$ ,  $\sqrt{s} = 14 \text{ TeV}$

$p_T(l/b) > 20/60 \text{ GeV}$   
 $2.0 < \eta(l, b) < 4.5$



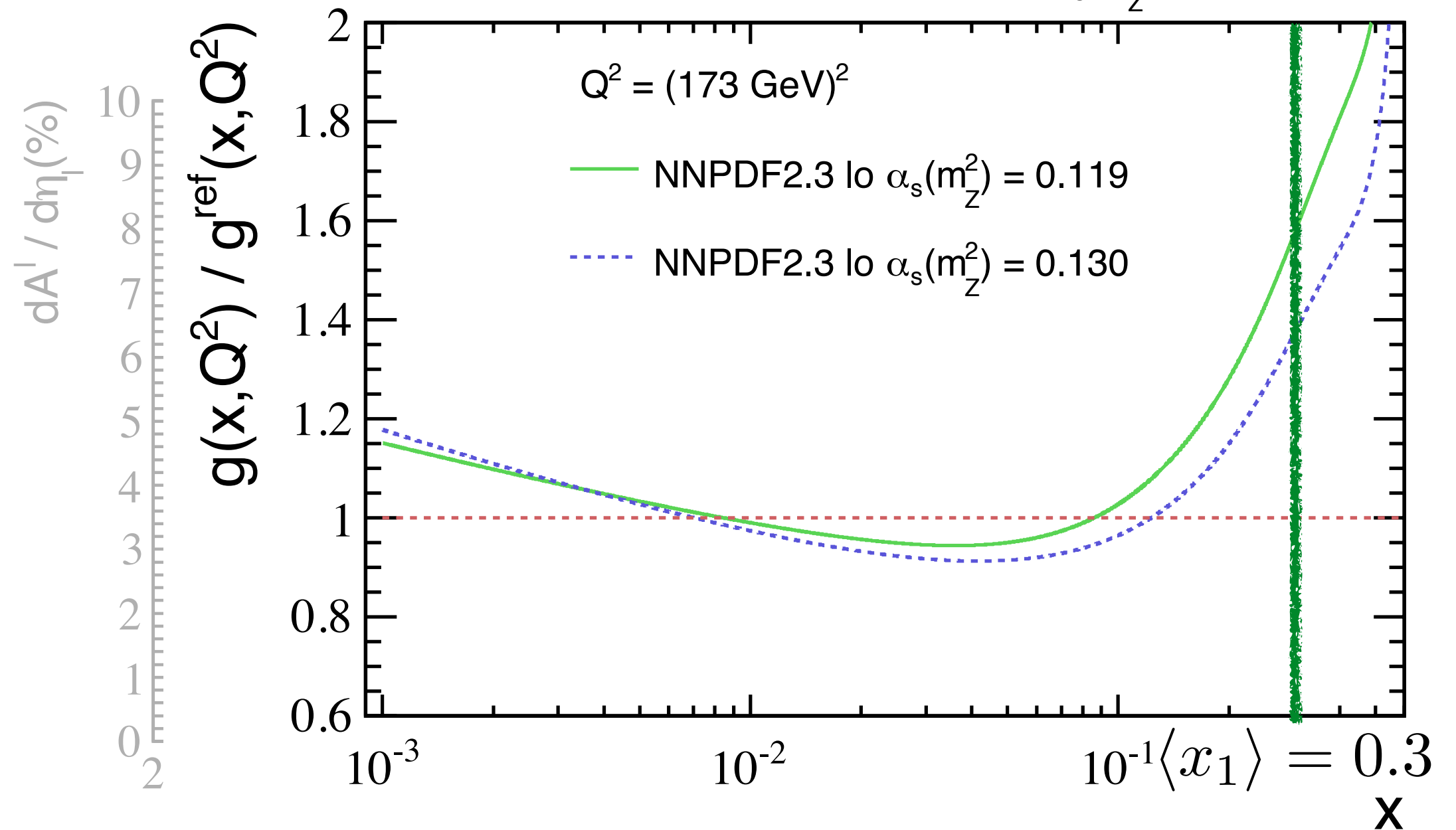
Fit backgrounds  
 experimentally:

$l^\pm j, l^\pm bj, l^\pm bb$   
 control channels

# Single-lepton asymmetry

$$A^l = \int_{2.0}^{4.5} d\eta_l \left( \frac{d\sigma^{l^+b}/d\eta_l - d\sigma^{l^-b}/d\eta_l}{d\sigma^{l^+b}/d\eta_l + d\sigma^{l^-b}/d\eta_l} \right) \quad \begin{array}{l} 2.0 < \eta(l, b) < 4.5 \\ p_T(l/b) > 20/60 \text{ GeV} \end{array}$$

gluon PDF ratio,  $g^{\text{ref}} = \text{NNPDF2.3 nlo } \alpha_s(m_Z^2) = 0.119$



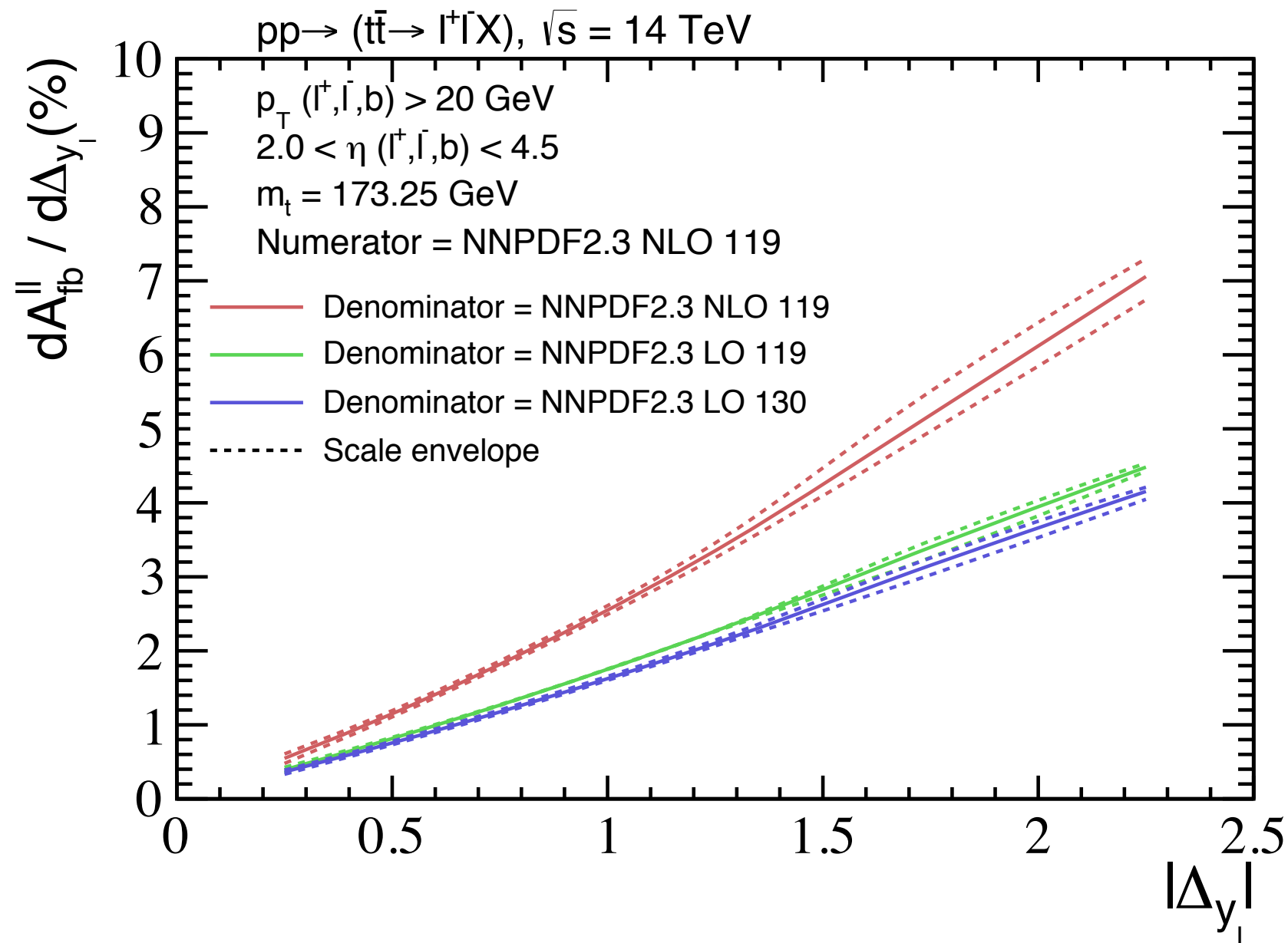
# Differential di-lepton asymmetry

$$A_{fb}^{ll} = \int d\Delta_y \frac{(d\sigma^{\mu eb}(\Delta_y > 0) - d\sigma^{\mu eb}(\Delta_y < 0)) / d\Delta_y}{d\sigma^{\mu eb} / d\Delta_y}$$

$$2.0 < \eta(e, \mu, b) < 4.5$$

$$p_T(e, \mu, b) > 20 \text{ GeV}$$

$$\Delta R(l^\pm, \text{jet}) \geq 0.5$$

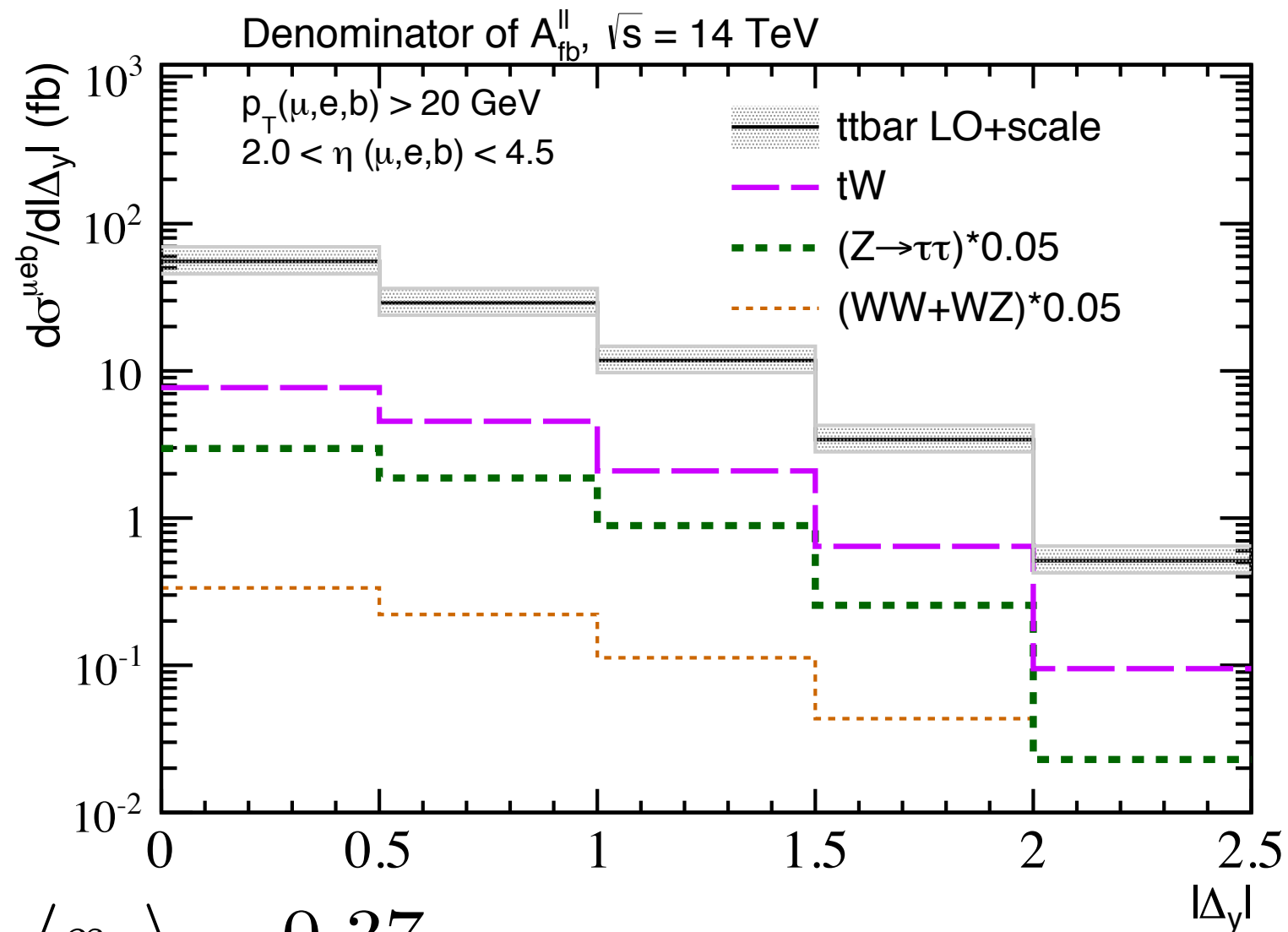


$$A_{fb}^{ll} = (0.9 - 1.4)\%$$

# Integrated di-lepton asymmetry

$N_{fb}^{ll}$ (fb)		$\mu = m_t/2$	$\mu = m_t$	$\mu = 2m_t$	
$\mathcal{O}(\alpha_s^3)$	$u\bar{u}$	0.977	0.709	0.536	
	$d\bar{d}$	0.344	0.239	0.181	
	$ug$	0.095	0.070	0.045	
	$dg$	0.031	0.021	0.013	
$\mathcal{O}(\alpha_s^2\alpha_e)$		0.179	0.146	0.120	
$\approx \mathcal{O}(\alpha_s^2\alpha_w)$		0.009	0.007	0.006	
$\mathcal{O}(\alpha_{e/w}^2)$		0.006	0.005	0.005	
Total		1.642	1.198	0.907	
		$D_{fb}^{ll}$ (fb), 14 TeV			
PDF		$\mu = m_t/2$	$\mu = m_t$	$\mu = 2m_t$	$A_{fb}^{ll}$ (%)
NLO 119		110.4	85.0	67.4	1.41 (8)
LO 119		160.7	120.7	93.3	0.99 (3)
LO 130		176.6	130.0	98.8	0.92 (1)

# Dilepton + b-jet



$$\delta\sigma_{\text{stat}}(1\text{year}) = 6\%$$

$$t\bar{t} \rightarrow \mu^{\pm} e^{\mp} b X$$

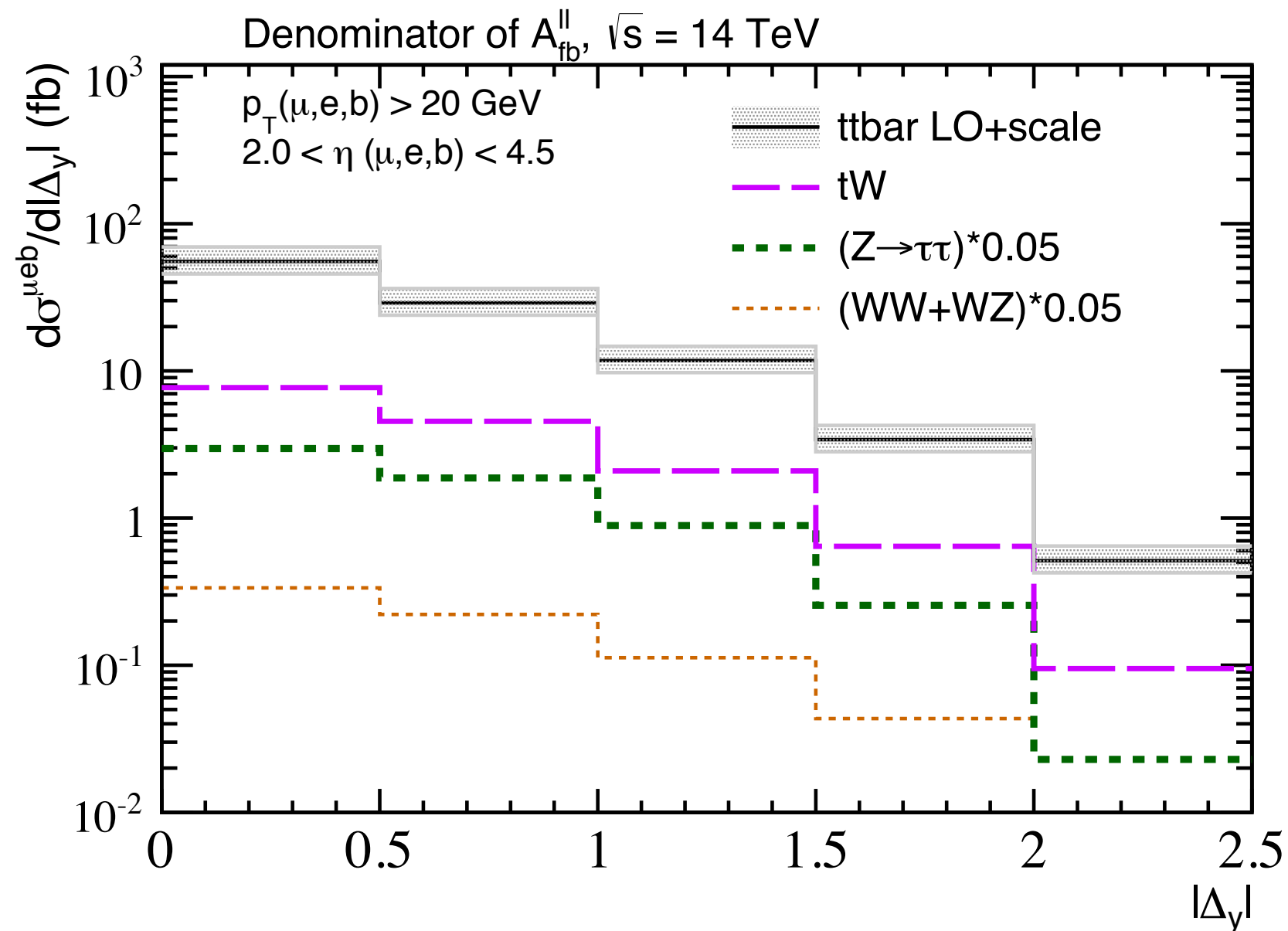
14 TeV

$$2.0 < \eta(l, b) < 4.5$$

$$p_T(l, b) > 20 \text{ GeV}$$

$$\Delta R(l^{\pm}, \text{jet}) \geq 0.5$$

# Di-lepton asymmetry



$$A_{fb}^{ll} = (0.9 - 1.4) \pm 1.6\%$$

stat. 50 fb<sup>-1</sup>

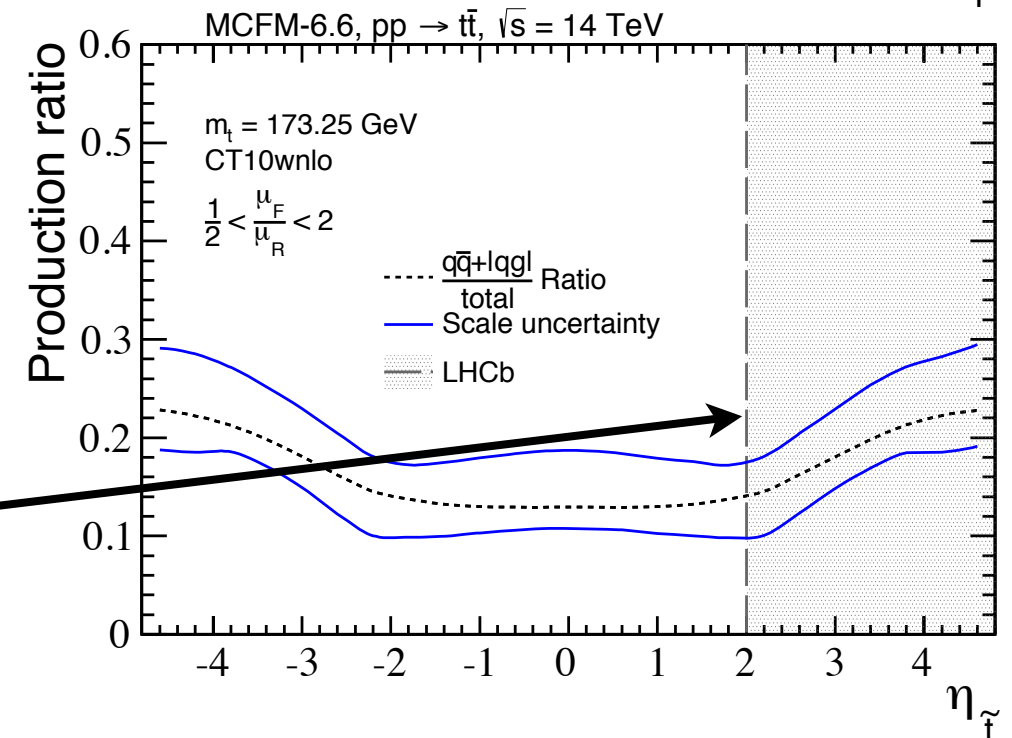
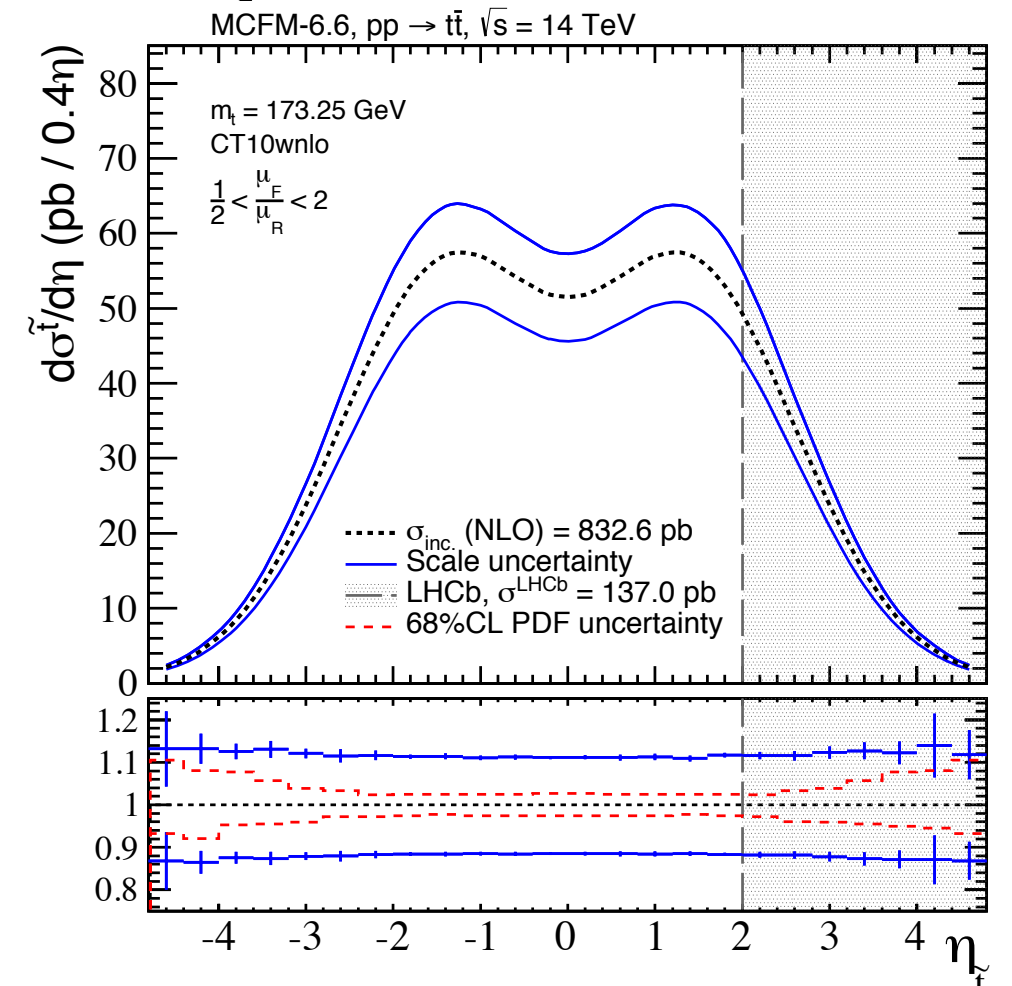
# Parton level theoretical systematics

$$\frac{d\sigma^{\tilde{t}}}{dX} = \frac{1}{2} \left( \frac{d\sigma^t}{dX} + \frac{d\sigma^{\bar{t}}}{dX} \right)$$

Production mechanism ratio:

$$\frac{q\bar{q} + |qg|}{total}$$

LHCb probes unique region





# Theoretical systematics for forward ttbar?

$$\sigma = \sum_{i,j} \int dx_i dx_j f_i(x_i, \mu_F^2) f_j(x_j, \mu_F^2) \frac{d\hat{\sigma}(m, \mu_F^2, \alpha_s(\mu_R), \mu_R^2)}{d\eta} d\eta$$

$$\frac{d\hat{\sigma}^{\text{LHCb}}}{d\eta} = \frac{1}{2} \left[ \frac{d\hat{\sigma}}{d\eta_t} + \frac{d\hat{\sigma}}{d\eta_{\bar{t}}} \right]_{\eta \in [2,5]}$$

$$\frac{1}{2} < \frac{\mu_F}{\mu_R} < 2$$

$$\delta\text{PDF} = 1\sigma\text{CL}$$

$$\alpha_s(M_Z) = 0.1184 \pm 0.0007$$

$$\delta m_t = 1.5 \text{ GeV}$$

# Strong coupling

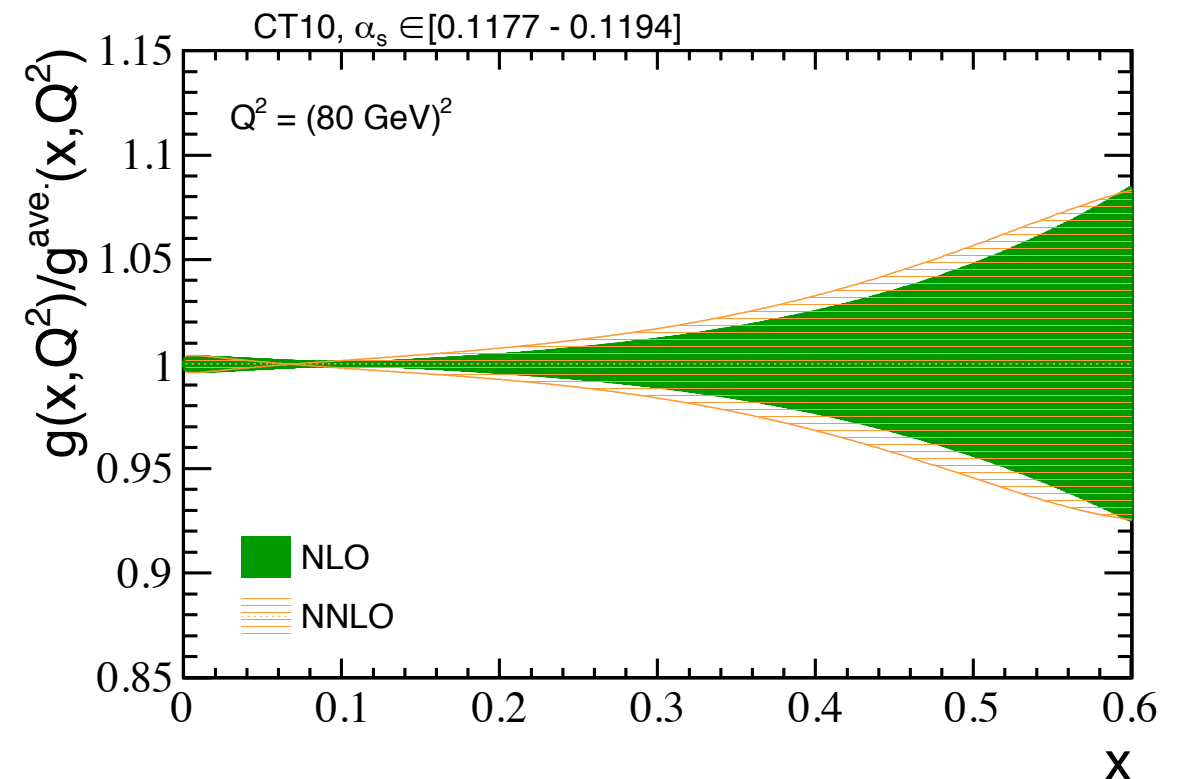
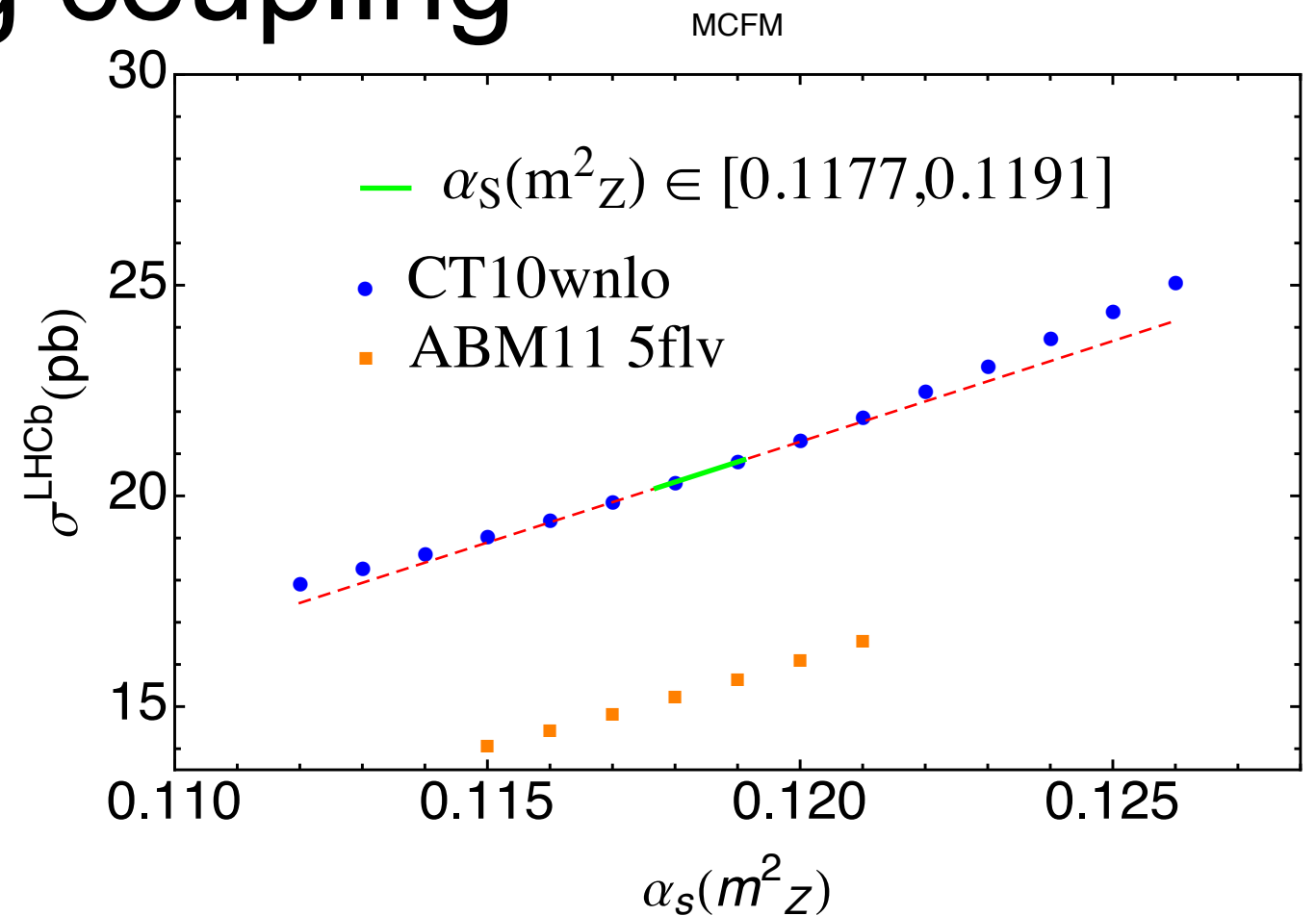
$\sigma^{LHCb}$  vs.  $\alpha_s(M_Z)$

Current PDG value

$$\alpha_s(M_Z) = 0.1184 \pm 0.0007$$

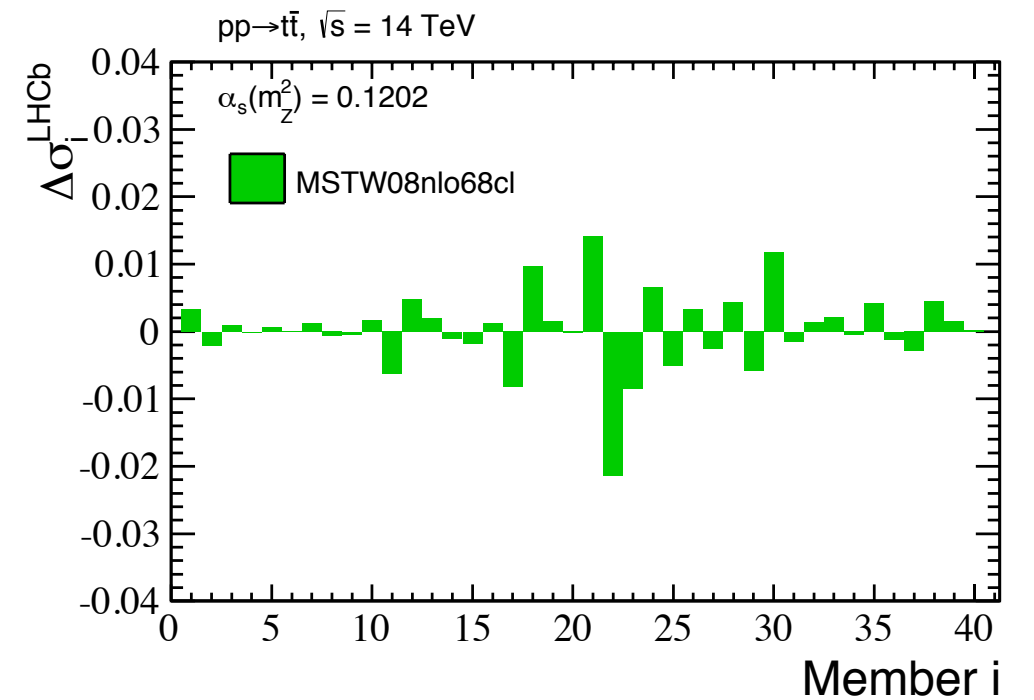
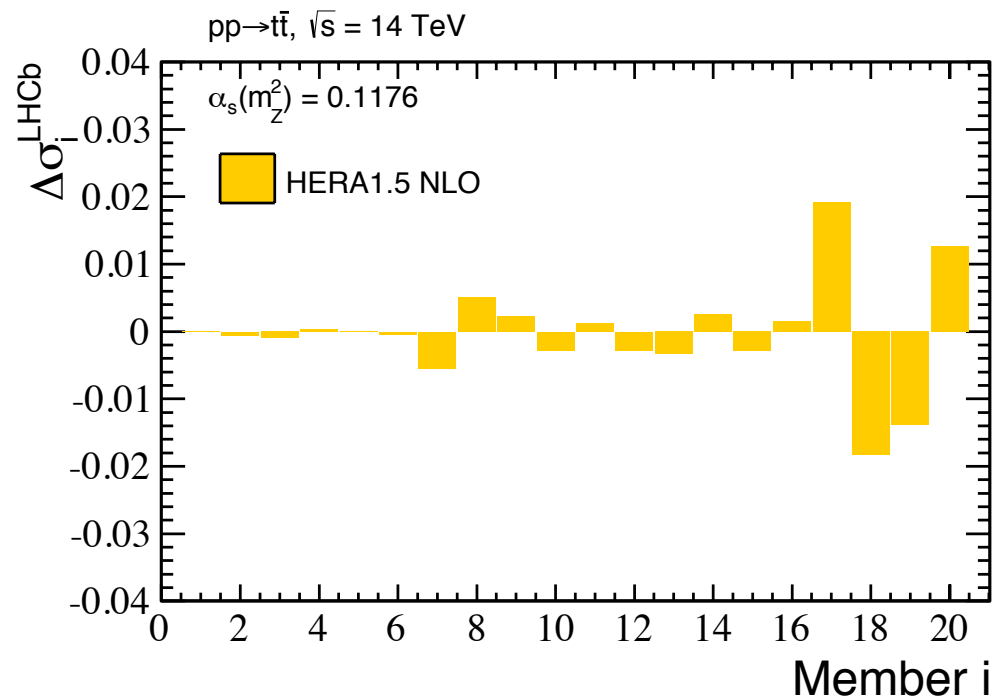
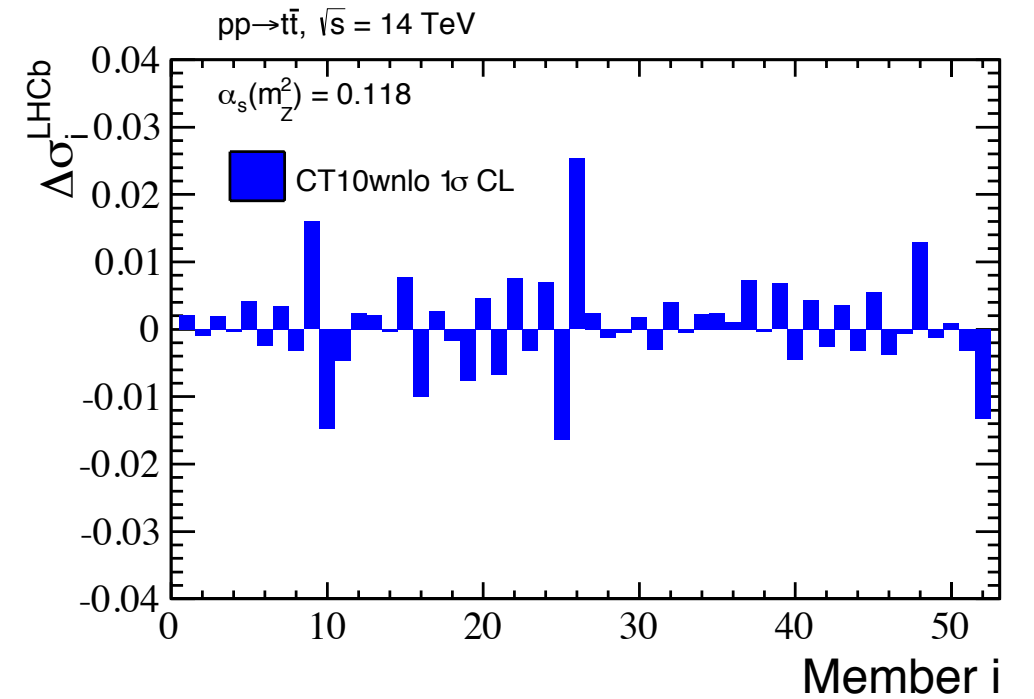
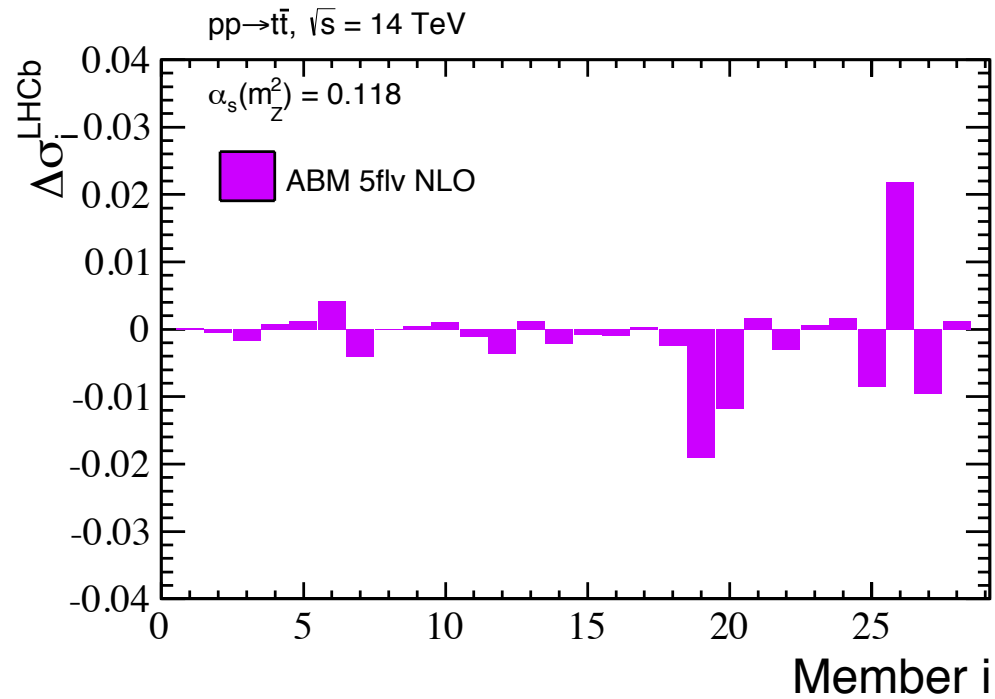
gluon PDF uncertainty  
for  $\delta\alpha_s$

$$\delta\alpha_s \rightarrow \delta\sigma^{LHCb} = 1.3\%$$



Order	PDF	$\sigma(\text{pb})$	$\delta_{\text{scale}} \text{ (pb)}$	$\delta_{\text{PDF}} \text{ (pb)}$	$\delta_{\alpha_s} \text{ (pb)}$	$\delta_{m_t} \text{ (pb)}$	$\delta_{\text{total}} \text{ (pb)}$
NNLO* (inc.)	ABM	832.0	+18.7 (+2.2%) -27.4 (-3.3%)	+25.1 (+3.0%) -25.1 (-3.0%)	+0.0 (+0.0%) -0.0 (-0.0%)	+34.9 (+4.2%) -33.7 (-4.1%)	+61.7 (+7.4%) -69.7 (-8.4%)
NLO(inc.)		771.9	+91.0 (+11.8%) -92.4 (-12.0%)	+9.4 (+1.2%) -9.4 (-1.2%)	+0.0 (+0.0%) -0.0 (-0.0%)	+32.3 (+4.2%) -31.9 (-4.1%)	+124.7 (+16.1%) -125.7 (-16.3%)
NLO(LHCb)		117.2	+14.5 (+12.3%) -14.1 (-12.0%)	+2.0 (+1.7%) -2.0 (-1.7%)	+0.0 (+0.0%) -0.0 (-0.0%)	+5.2 (+4.4%) -5.1 (-4.3%)	+20.0 (+17.1%) -19.5 (-16.7%)
NNLO* (inc.)	CT10	952.8	+23.3 (+2.4%) -34.5 (-3.6%)	+22.4 (+2.3%) -19.9 (-2.1%)	+14.0 (+1.5%) -14.0 (-1.5%)	+39.2 (+4.1%) -37.8 (-4.0%)	+70.6 (+7.4%) -79.5 (-8.3%)
NLO(inc.)		832.6	+97.0 (+11.7%) -96.7 (-11.6%)	+19.6 (+2.4%) -20.2 (-2.4%)	+9.2 (+1.1%) -9.2 (-1.1%)	+34.0 (+4.1%) -33.3 (-4.0%)	+137.4 (+16.5%) -136.6 (-16.4%)
NLO(LHCb)		137.0	+16.7 (+12.2%) -16.4 (-12.0%)	+5.0 (+3.6%) -4.6 (-3.4%)	+1.8 (+1.3%) -1.8 (-1.3%)	+5.9 (+4.3%) -5.8 (-4.2%)	+24.7 (+18.0%) -24.0 (-17.5%)
NNLO* (inc.)	HERA	970.5	+22.1 (+2.3%) -22.0 (-2.3%)	+15.7 (+1.6%) -25.7 (-2.6%)	+12.8 (+1.3%) -12.8 (-1.3%)	+39.6 (+4.1%) -38.4 (-4.0%)	+66.6 (+6.9%) -70.0 (-7.2%)
NLO(inc.)		804.2	+91.9 (+11.4%) -87.6 (-10.9%)	+16.1 (+2.0%) -21.9 (-2.7%)	+5.3 (+0.7%) -5.3 (-0.7%)	+33.4 (+4.1%) -32.4 (-4.0%)	+129.3 (+16.1%) -127.1 (-15.8%)
NLO(LHCb)		124.7	+14.8 (+11.8%) -13.7 (-11.0%)	+3.0 (+2.4%) -3.0 (-2.4%)	+1.1 (+0.9%) -1.1 (-0.9%)	+5.5 (+4.4%) -5.3 (-4.3%)	+21.1 (+16.9%) -19.9 (-15.9%)
NNLO* (inc.)	MSTW	953.6	+22.7 (+2.4%) -33.9 (-3.6%)	+16.2 (+1.7%) -17.8 (-1.9%)	+12.8 (+1.3%) -12.8 (-1.3%)	+39.1 (+4.1%) -37.9 (-4.0%)	+66.9 (+7.0%) -77.7 (-8.1%)
NLO(inc.)		885.6	+107.2 (+12.1%) -105.7 (-11.9%)	+16.0 (+1.8%) -19.4 (-2.2%)	+10.1 (+1.1%) -10.1 (-1.1%)	+36.2 (+4.1%) -35.3 (-4.0%)	+148.1 (+16.7%) -147.3 (-16.6%)
NLO(LHCb)		144.4	+18.6 (+12.8%) -17.8 (-12.3%)	+3.5 (+2.4%) -3.9 (-2.7%)	+1.9 (+1.3%) -1.9 (-1.3%)	+6.2 (+4.3%) -6.1 (-4.2%)	+25.9 (+18.0%) -25.2 (-17.5%)
NNLO* (inc.)	NNPDF	977.5	+23.6 (+2.4%) -35.4 (-3.6%)	+16.4 (+1.7%) -16.4 (-1.7%)	+12.2 (+1.3%) -12.2 (-1.3%)	+40.4 (+4.1%) -39.1 (-4.0%)	+68.9 (+7.0%) -80.0 (-8.1%)
NLO(inc.)		894.5	+107.6 (+12.0%) -101.0 (-11.3%)	+12.8 (+1.4%) -12.8 (-1.4%)	+9.9 (+1.1%) -9.9 (-1.1%)	+36.6 (+4.1%) -35.8 (-4.0%)	+147.6 (+16.5%) -140.3 (-15.7%)
NLO(LHCb)		142.5	+18.1 (+12.7%) -16.6 (-11.7%)	+3.0 (+2.1%) -3.0 (-2.1%)	+2.0 (+1.4%) -2.0 (-1.4%)	+6.2 (+4.4%) -6.1 (-4.3%)	+25.2 (+17.7%) -23.7 (-16.6%)

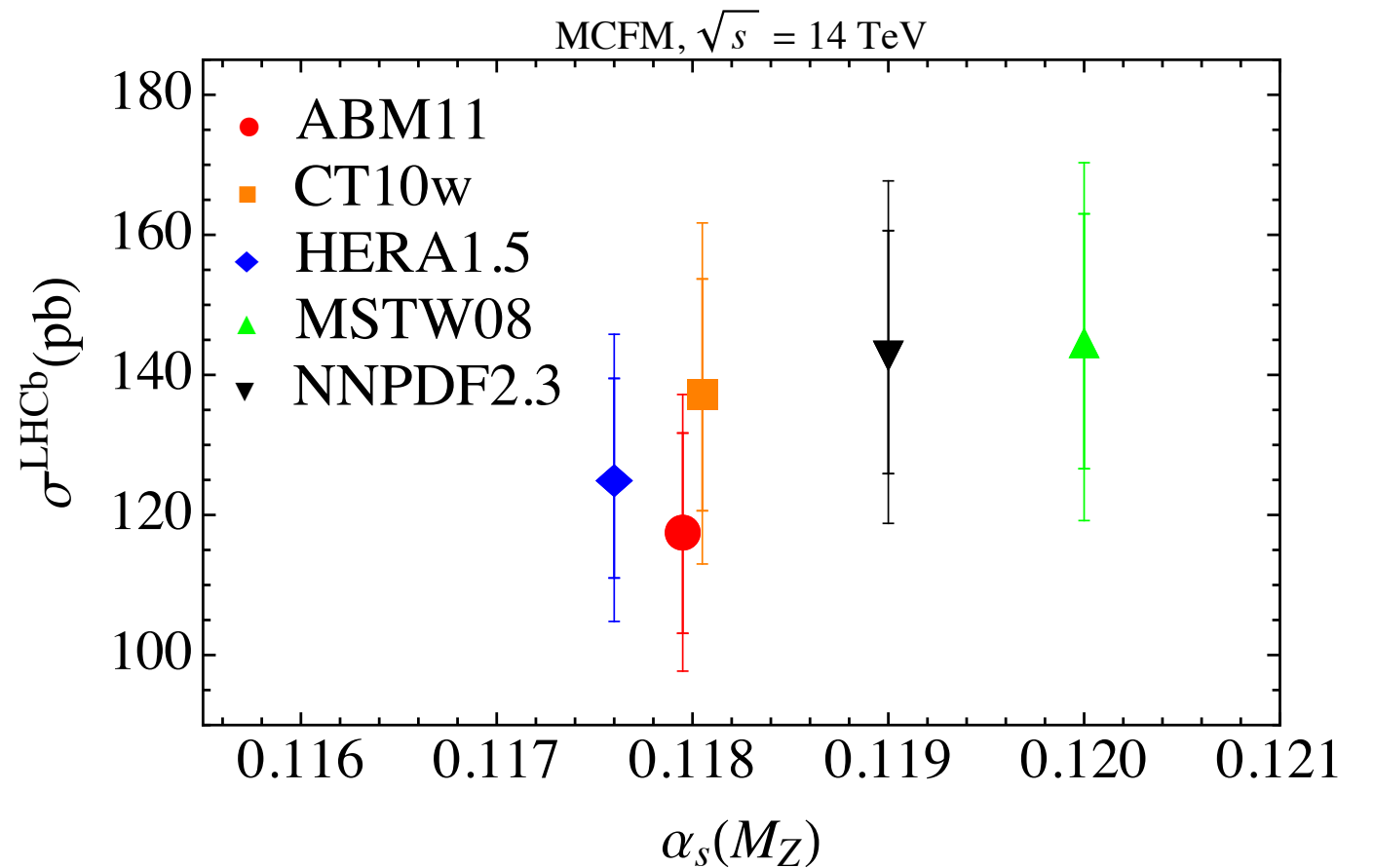
# Summary of eigenvector sensitivity



$$\Delta X_j^\pm = \frac{X(\mathcal{S}_j^\pm) - X(\mathcal{S}_0)}{X(\mathcal{S}_0)}$$

# Summary of theory systematics (NLO)

$$\delta_{\text{total}} = \delta_{\text{scale}} + (\delta_{\text{PDF}}^2 + \delta_{\alpha_s}^2 + \delta_{m_t}^2)^{\frac{1}{2}}$$

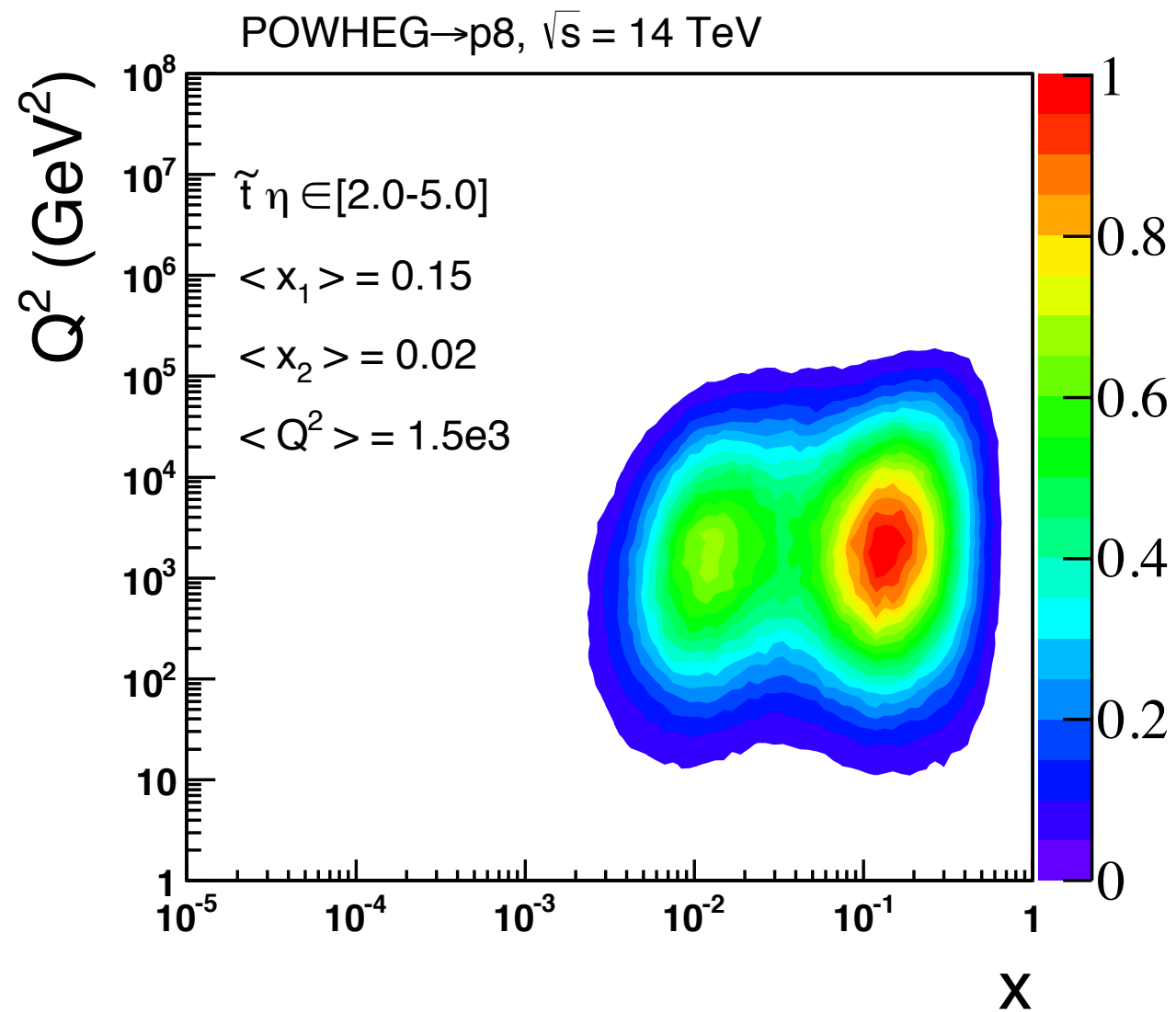


$$\delta_X^{\text{ratio}} = \frac{\delta_X^{\text{LHCb}}}{\delta_X^{\text{NLO}}} \left\{ \begin{array}{l} \text{ABM} \\ \text{CT10} \\ \text{HERA} \\ \text{MSTW} \\ \text{NNPDF} \end{array} \right.$$

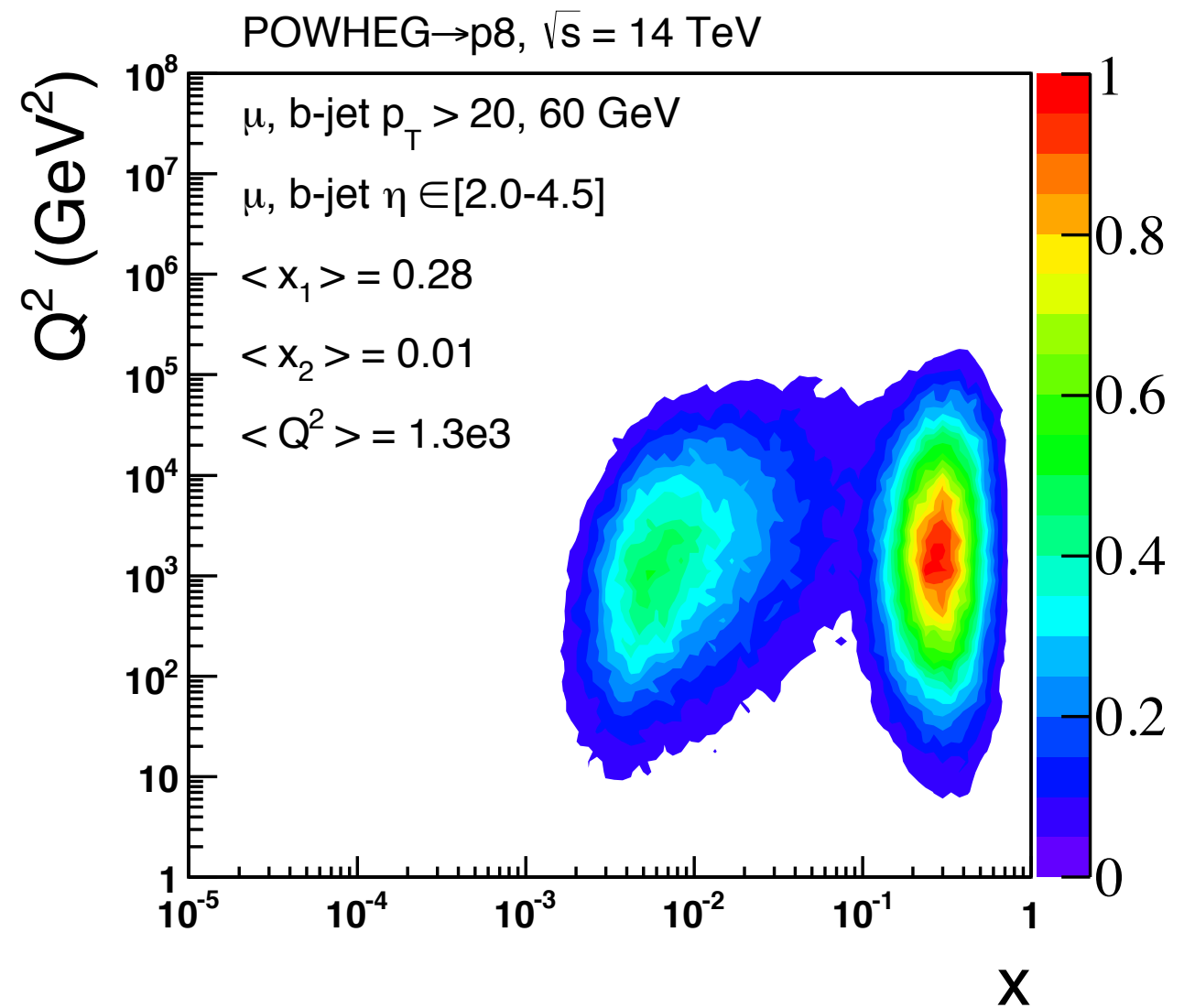
PDF	$\delta_{\text{scale}}^{\text{ratio}}$	$\delta_{\text{PDF}}^{\text{ratio}}$	$\delta_{\alpha_s}^{\text{ratio}}$	$\delta_{m_t}^{\text{ratio}}$	$\delta_{\text{total}}^{\text{ratio}}$
ABM	+1.05 -1.00	+1.40 -1.40	+0.00 -0.00	+1.05 -1.05	+1.06 -1.02
CT10	+1.05 -1.03	+1.55 -1.40	+1.20 -1.20	+1.06 -1.05	+1.09 -1.07
HERA	+1.04 -1.01	+1.19 -0.90	+1.33 -1.33	+1.07 -1.06	+1.05 -1.01
MSTW	+1.06 -1.03	+1.35 -1.23	+1.13 -1.13	+1.05 -1.06	+1.07 -1.05
NNPDF	+1.05 -1.03	+1.45 -1.45	+1.27 -1.27	+1.07 -1.07	+1.07 -1.06

# Impact of acceptance cuts (NLO)

parton level



kinematic cuts



# Constraining the gluon PDF

Perform a bayesian reweighting based on statistical inference.

[arXiv:1012.0836](#) NNPDF collaboration

[arXiv:1205.4024](#) G. Watt, R. S. Thorne, applied technique to MSTW hessian set

I apply the technique to CT10w and NNPDF2.3 NLO sets

## Recipe for Hessian reweighting

1) Calculate observables from eigenvector set

$$\{X_0(\mathcal{S}_0), X_1^-(\mathcal{S}_1^-), X_1^+(\mathcal{S}_1^+), \dots, X_N^-(\mathcal{S}_N^-), X_N^+(\mathcal{S}_N^+)\}$$

2) Generate random observables from these (storing random numbers)

$$X(\mathcal{S}_k) = X(\mathcal{S}_0) + \sum_{j=1}^N [X(\mathcal{S}_j^\pm) - X(\mathcal{S}_0)] |R_{kj}|$$

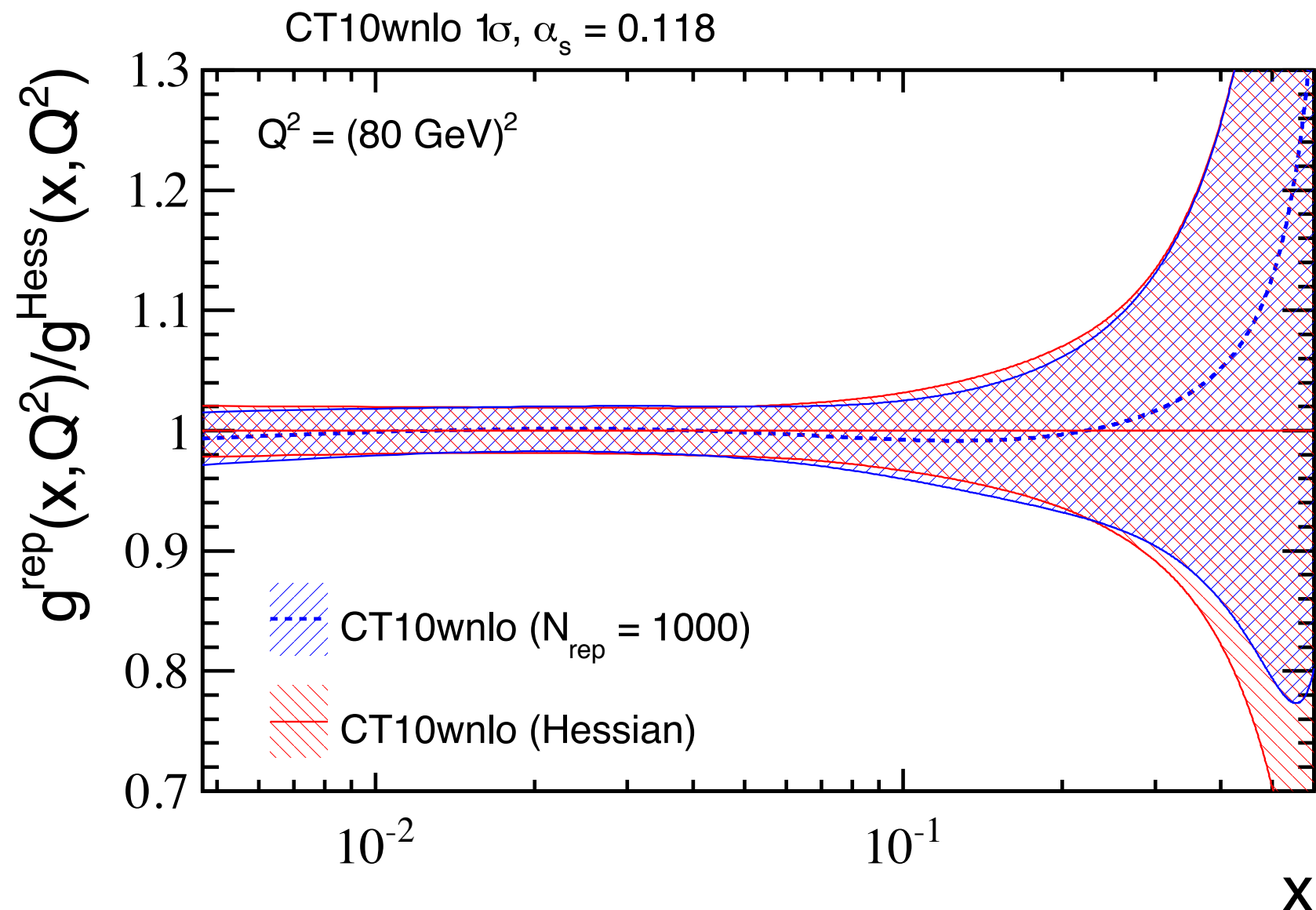
3) Apply a reweighting based on a ‘measured’ observable (e.g. cross-section)

$$W_k(\chi_k^2) = (\chi_k^2)^{\frac{1}{2}(N_{pts.} - 1)} \exp\left(-\frac{1}{2}\chi_k^2\right)$$

4) Apply these weights to the other observables (gluon PDF, ttbar asymmetry etc.)

# Follow the recipe - steps 1, 2

- 1) Choose observable as evolved gluon PDF,  $g^{\text{Hess}}(x, [Q = 80 \text{ GeV}]^2)$
- 2) Generate 1000 Replicas and compare,  $g^{\text{rep}}(x, [Q = 80 \text{ GeV}]^2)$

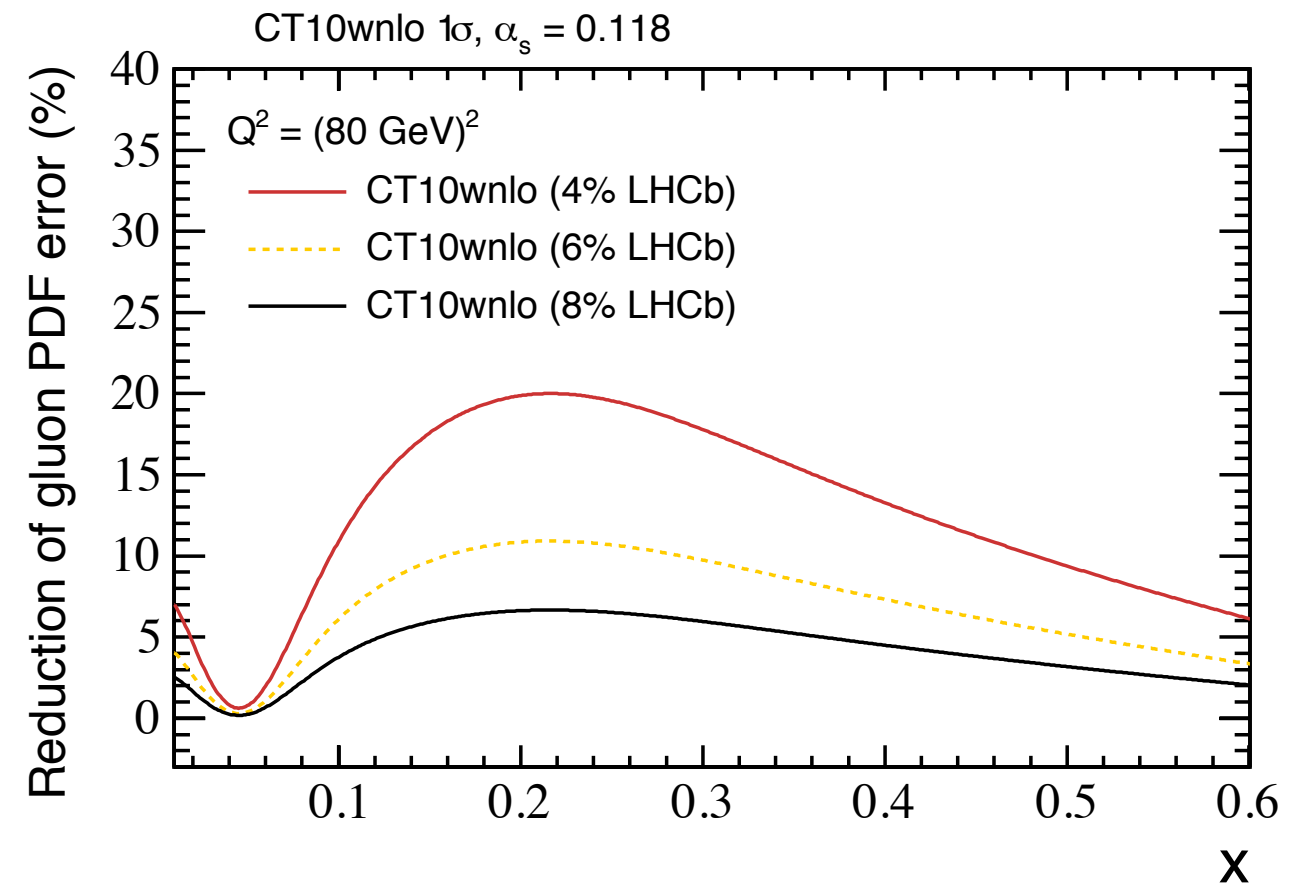
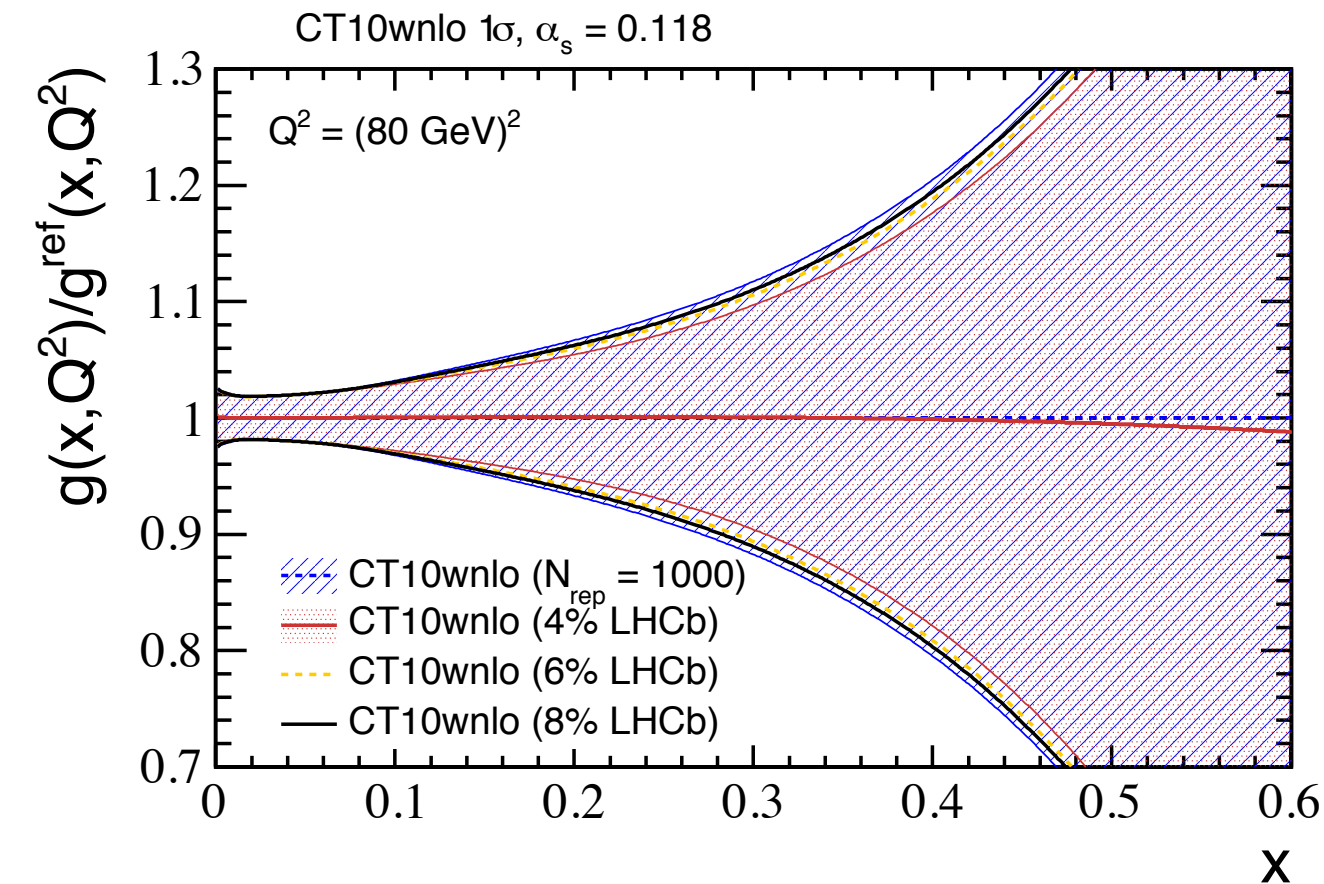




# Follow the recipe - steps 3, 4

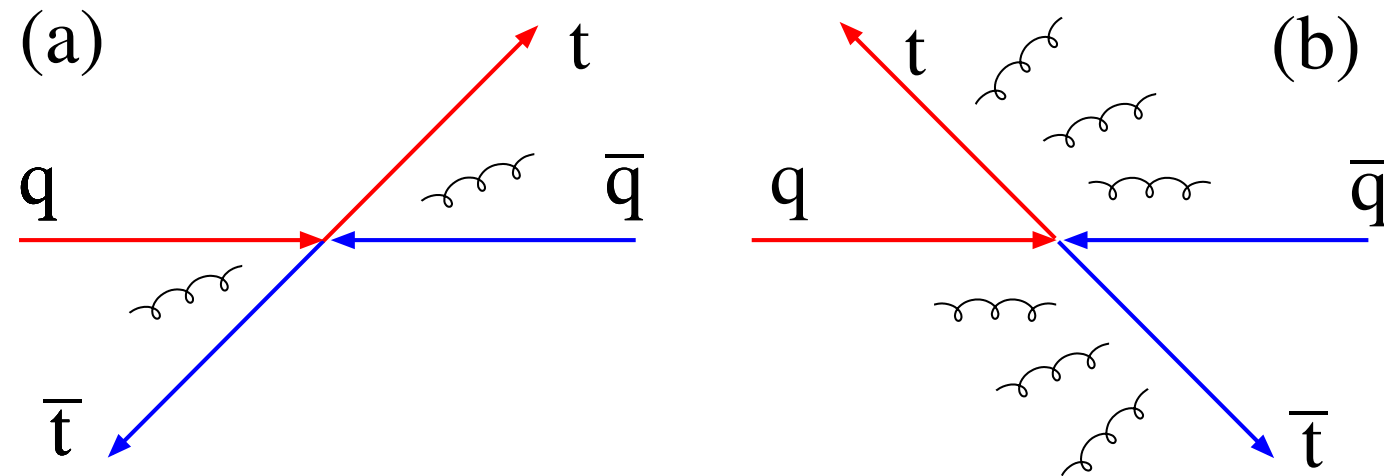
3) Pick some pseudo LHCb cross-section data,  $\bar{X}_0 = \frac{1}{N_{\text{rep}}} \sum_{k=1}^{N_{\text{rep}}} X_0(\mathcal{S}_0)[1 + R_{k0}]$

4) Apply weights found using pseudodata to reweight evolved gluon PDF



# Asymmetry when interfaced to PS?

[arXiv:1205.1466](https://arxiv.org/abs/1205.1466) P.Z.Skands, B. R. Webber, J. Winter, QCD Coherence



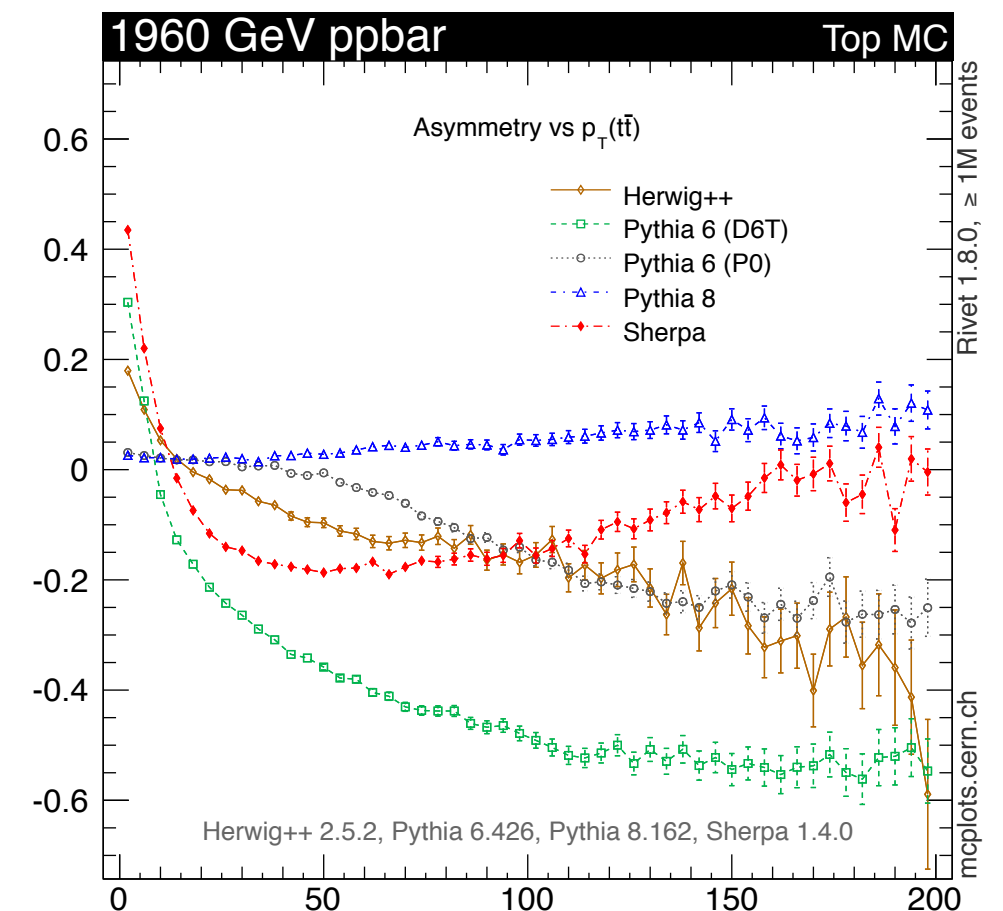
**Figure 2:** Colour flow and QCD radiation in (a) forward and (b) backward  $t\bar{t}$  production.

Symmetric LO matrix elements

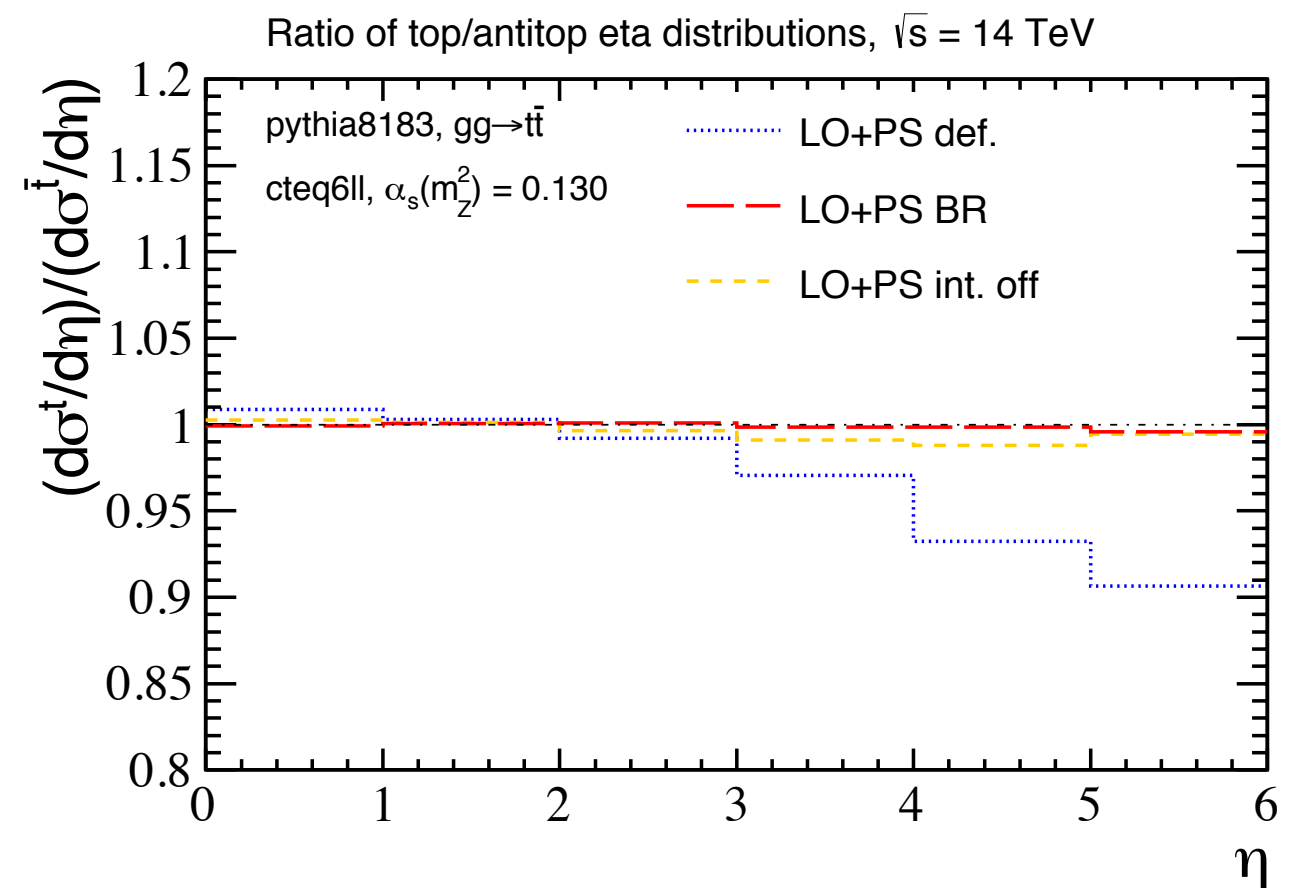
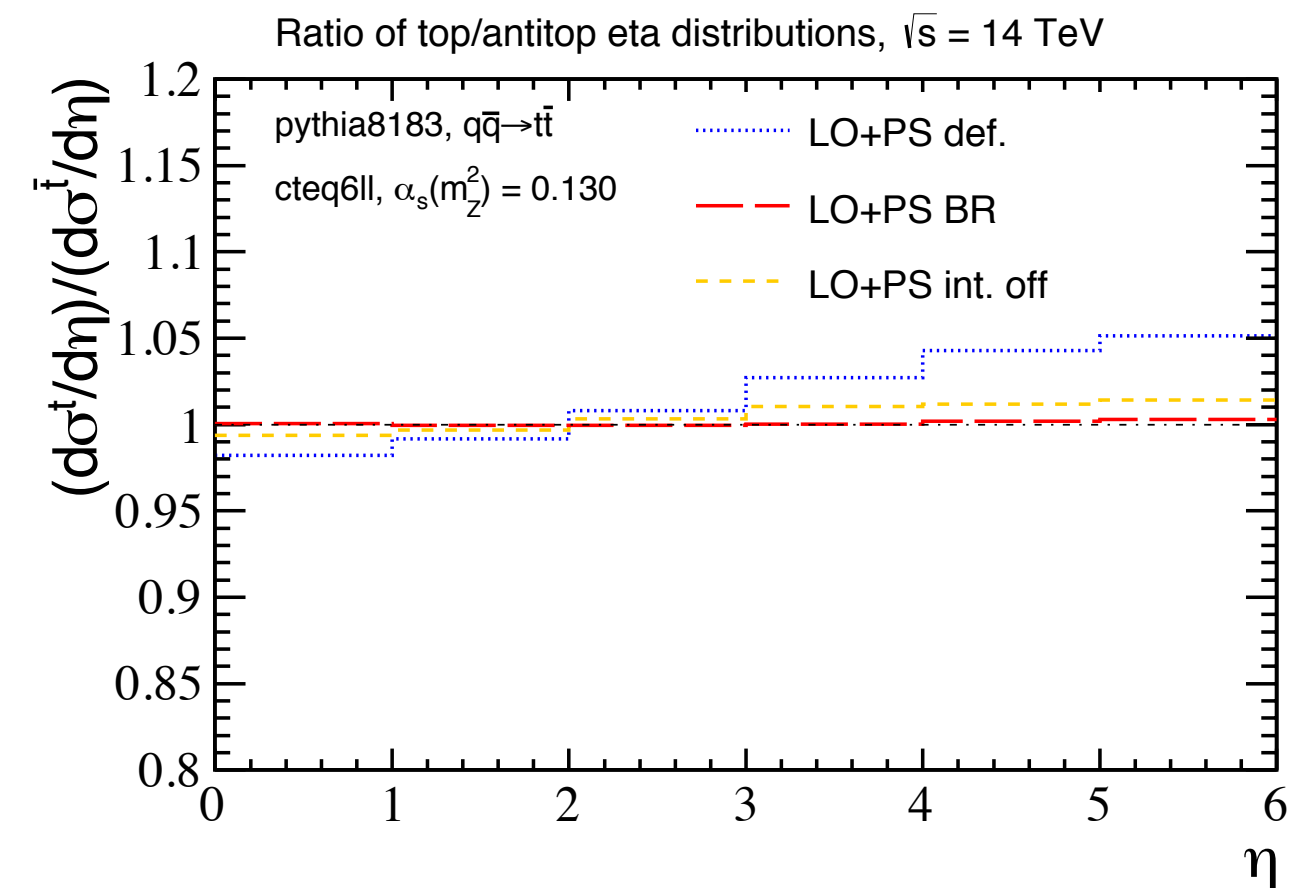
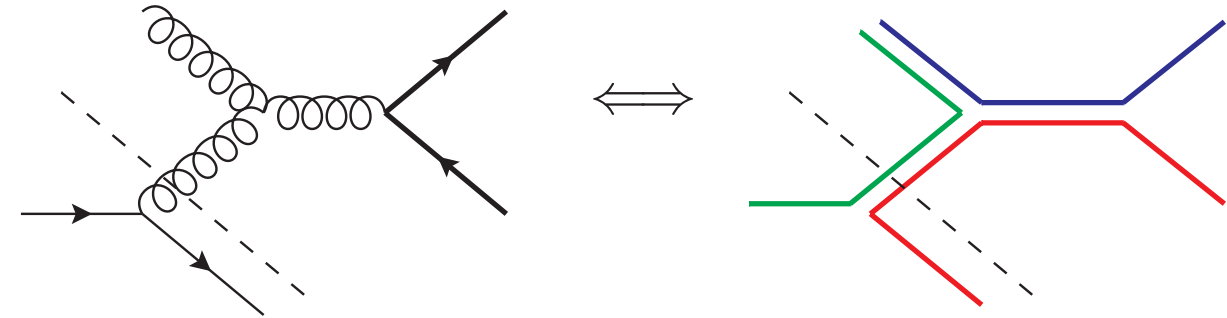
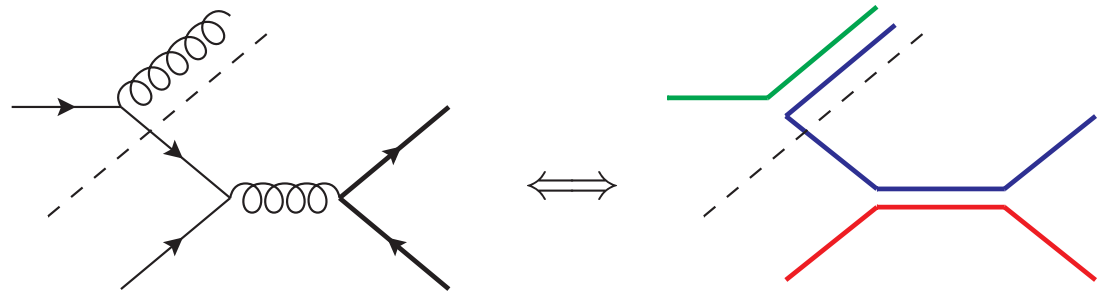
Different behaviour observed in Parton Shower (PS)

Though this was observed in qqbar (TeVatron)

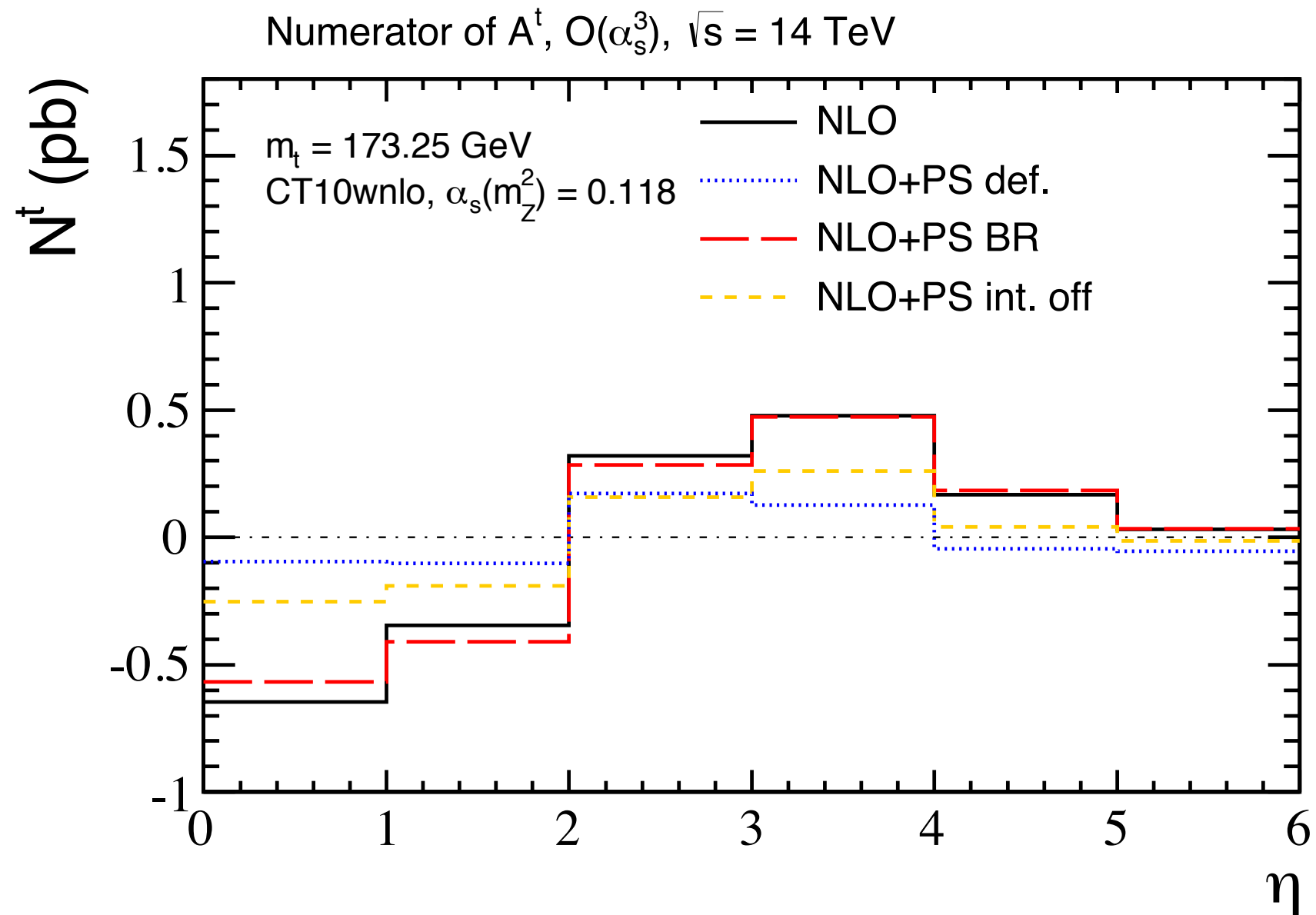
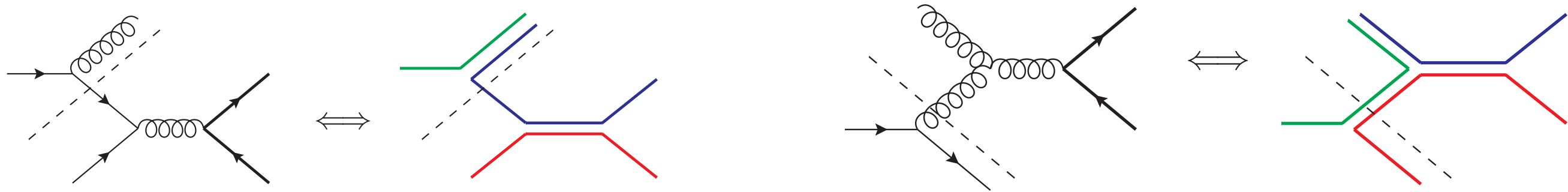
What about the LHC, gg dominated



# Asymmetry when interfaced to PS?



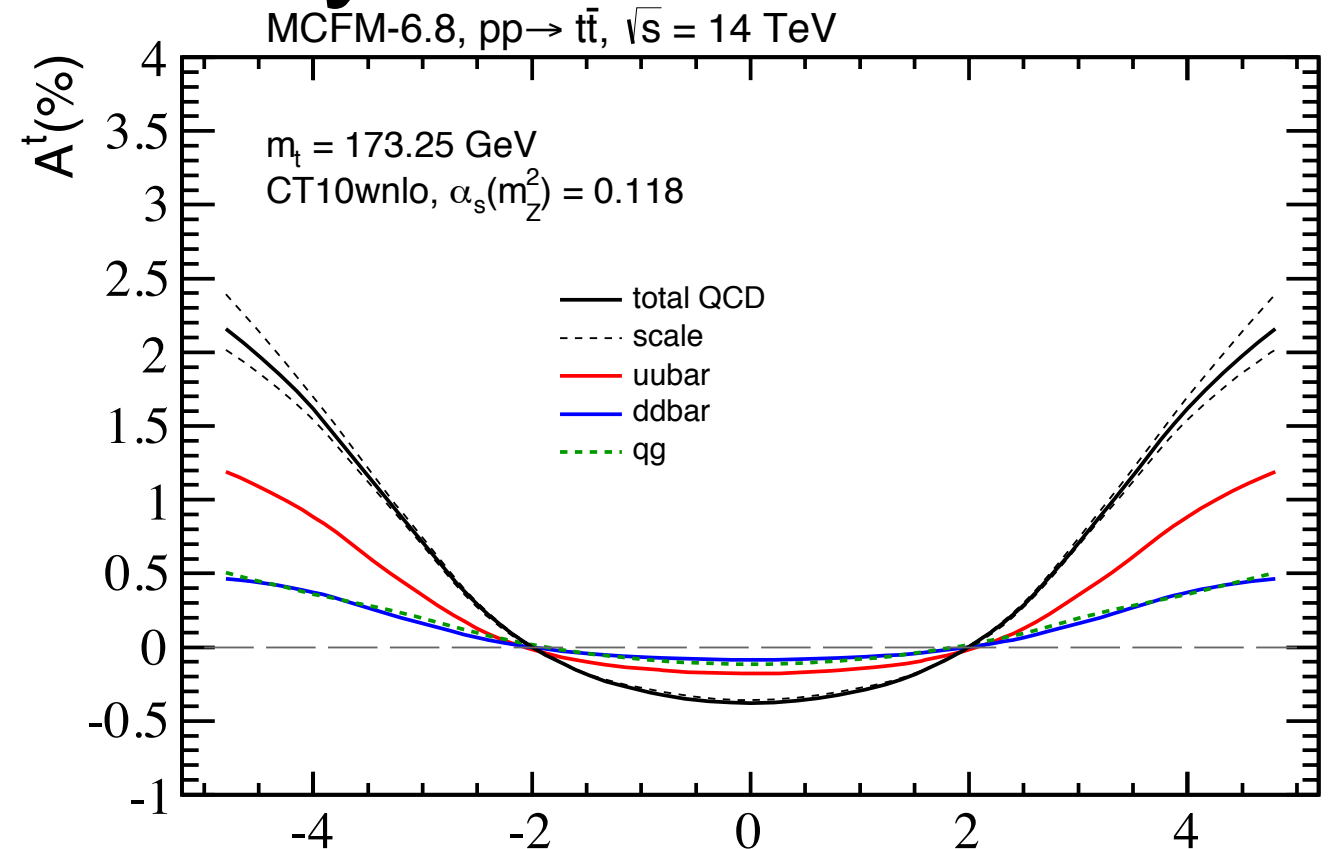
# Asymmetry when interfaced to PS?



# Stable top quark asymmetries

Parton level asymmetry

qqbar and qg separated



Parton level asymmetry

QCD / WEAK separated

