



A Higgs Near 125 GeV Beyond the MSSM

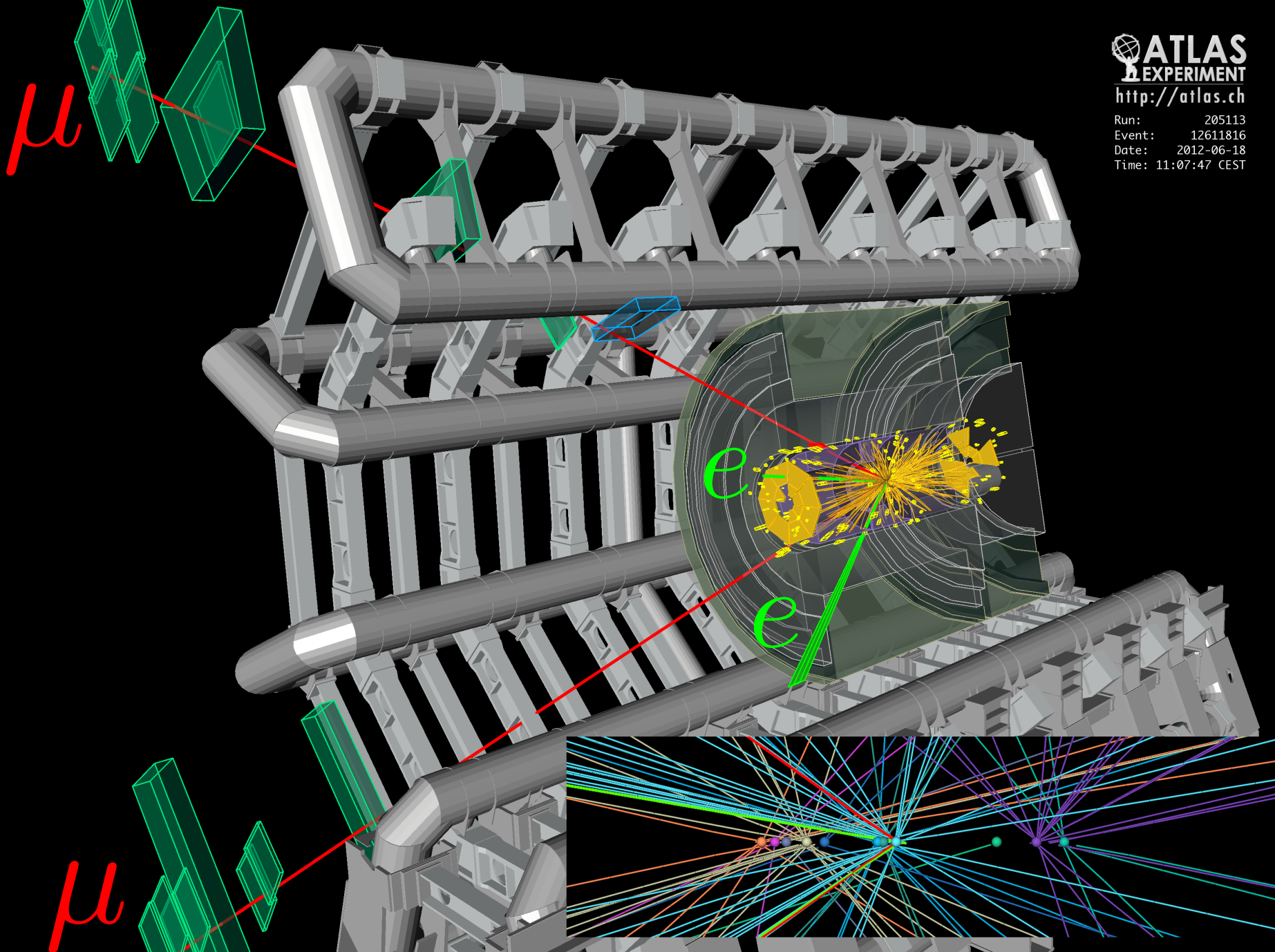
Part 1 Higgs in SM and NMSSM

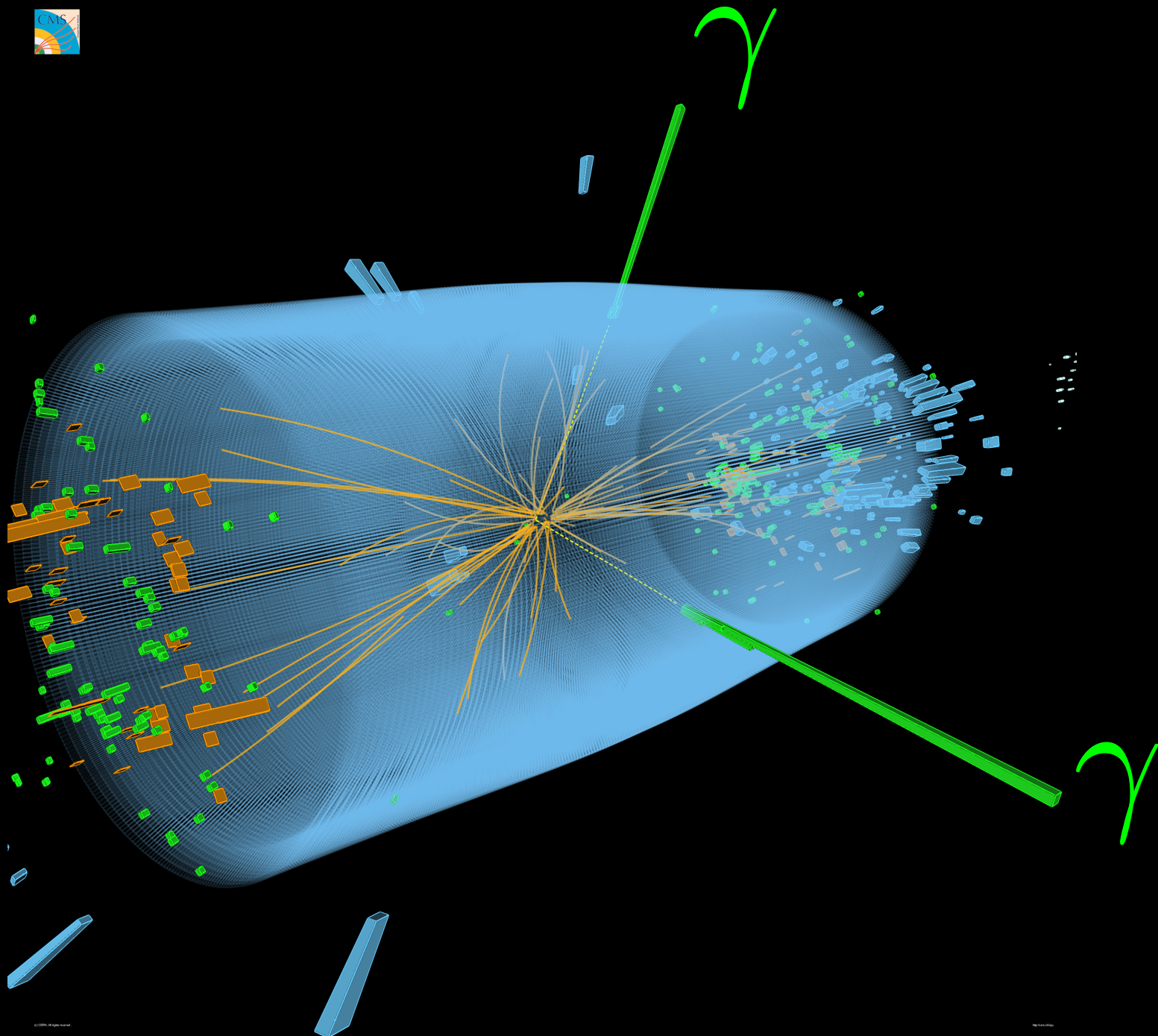
Part 2 Higgs and Gluinos in E6SSM

Steve King

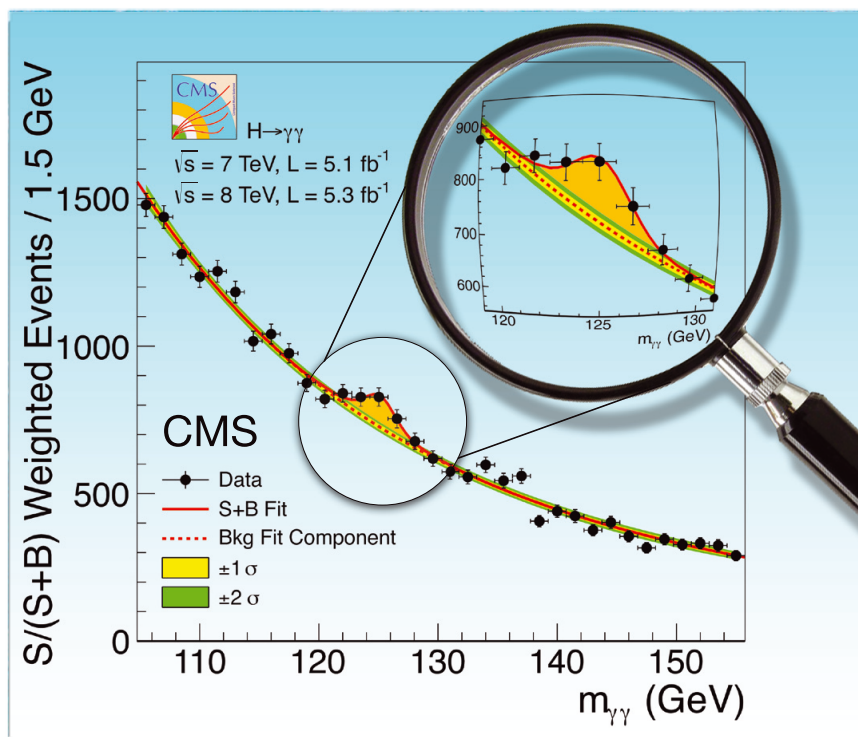
Sussex, Mon 22nd Oct 2012

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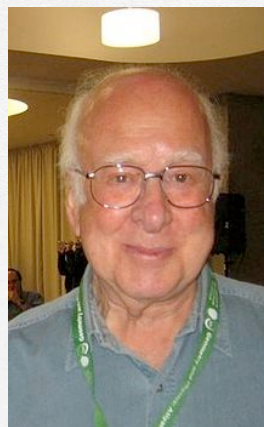




LHC has discovered a new particle



Congratulations to both
Atlas and CMS Collaborations
and to the builders of the LHC
on a magnificent achievement!

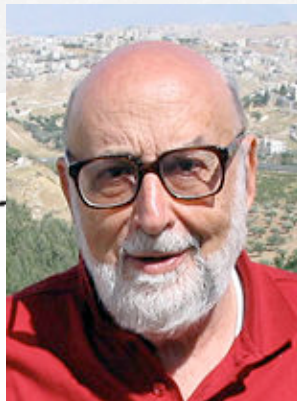


Peter Higgs
30 August 2012

"... The decay to two photons indicates that the new particle is a boson with spin different from one. The results presented here are consistent, ... with expectations for a standard model Higgs boson."

Not only does the discovery yield the missing link to the present Standard Model theory of elementary particles, but a detailed analysis of the decays, in particular of the decay of the Scalar to two photons which is sensitive to loops of intermediated charged particles, will possibly yield information about the spectrum beyond the Standard Model.

Prof. François Englert

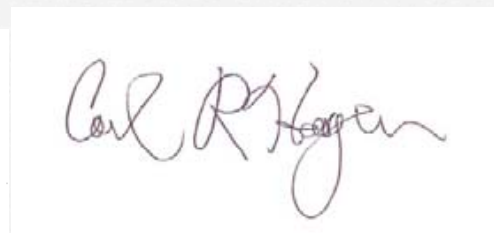


It is great to know that the famous boson almost certainly exists, and we are eagerly waiting for detailed measurement of its properties.

Prof. Tom Kibble



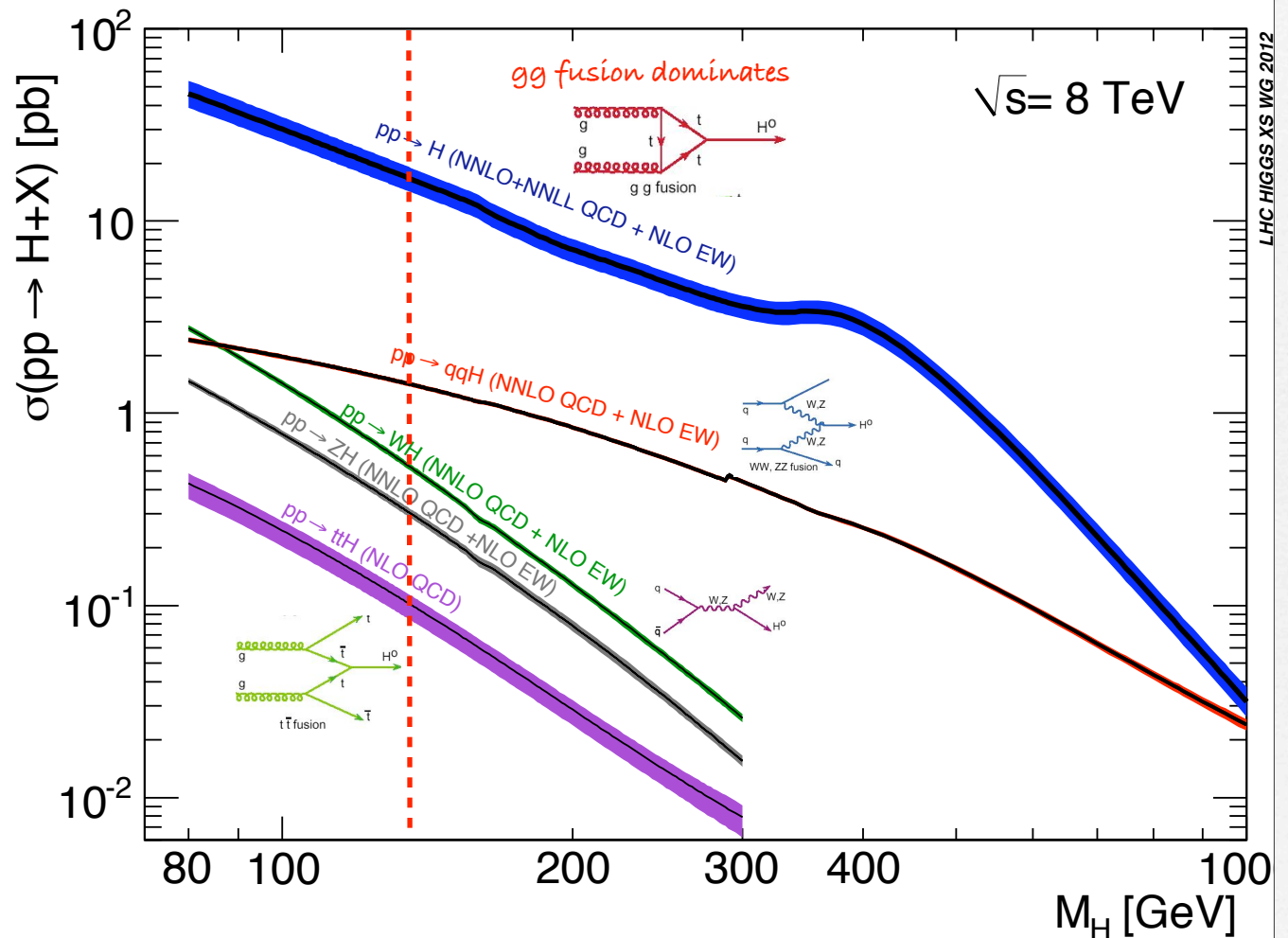
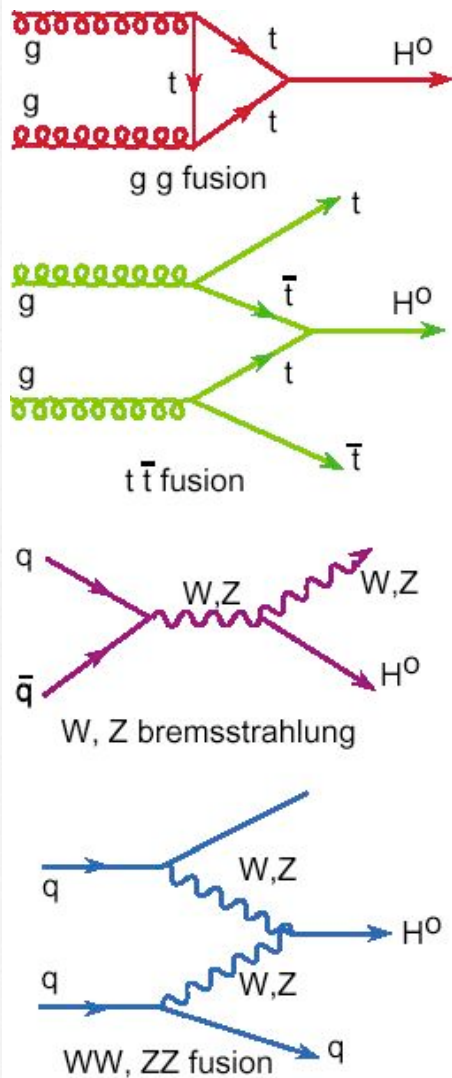
Prof. Carl R. Hagen



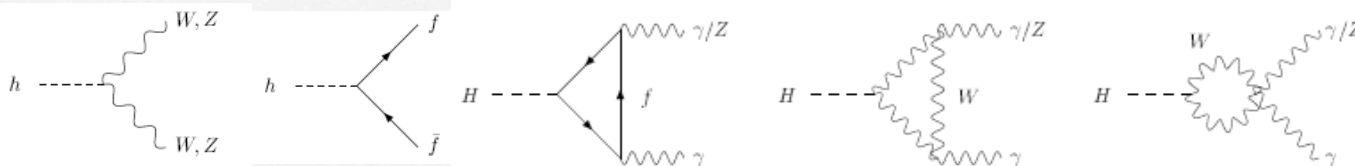
Prof. Gerald Guralnik



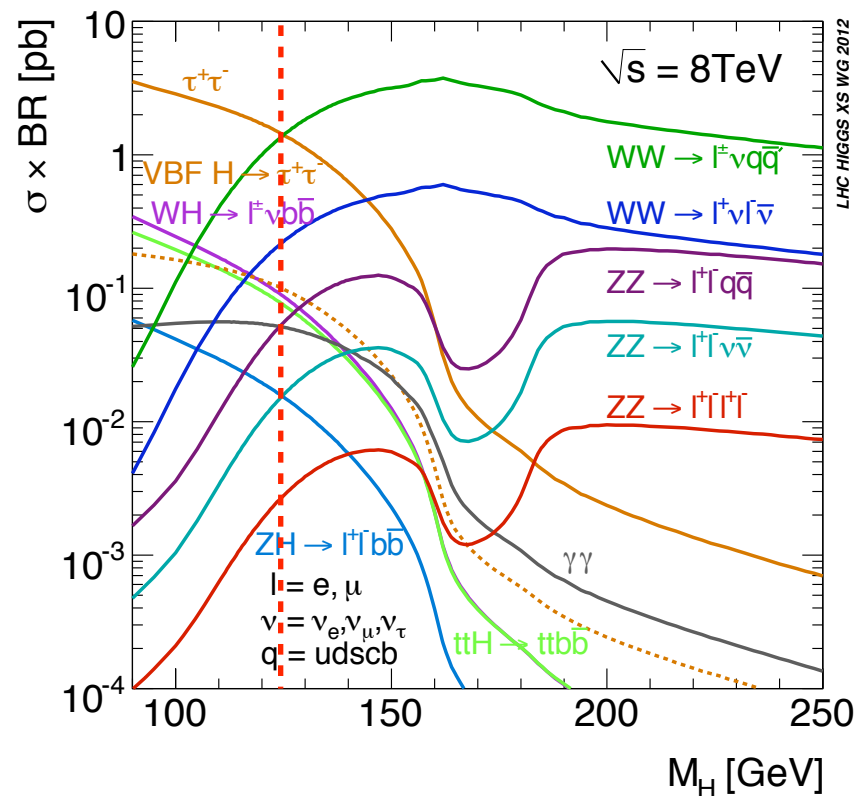
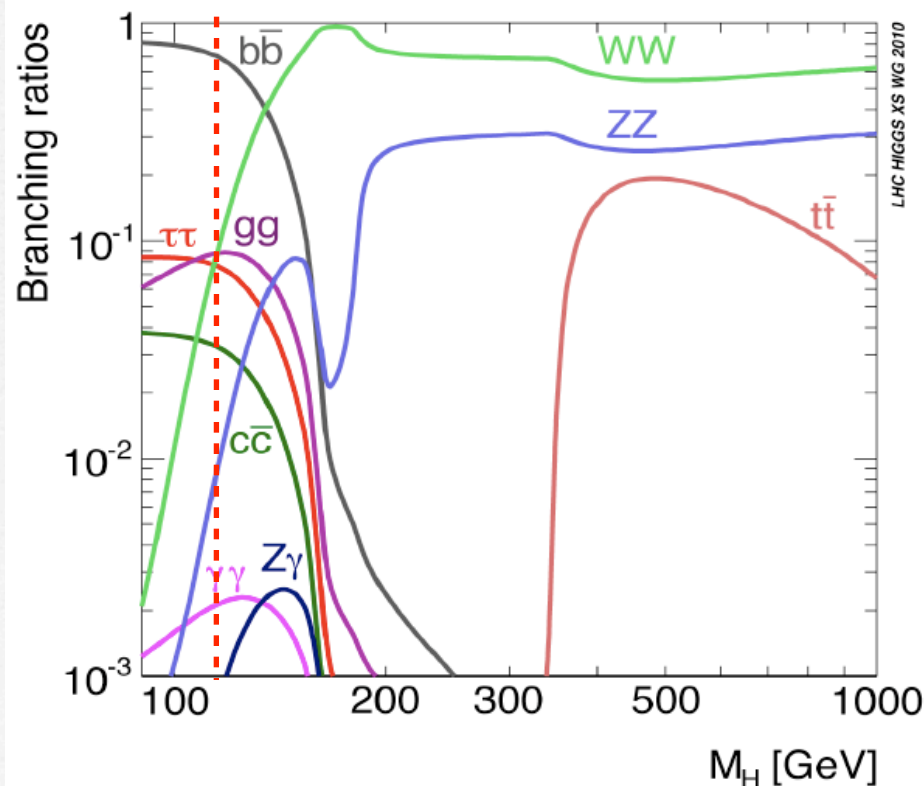
• Higgs production mechanisms and cross sections



Higgs Decays

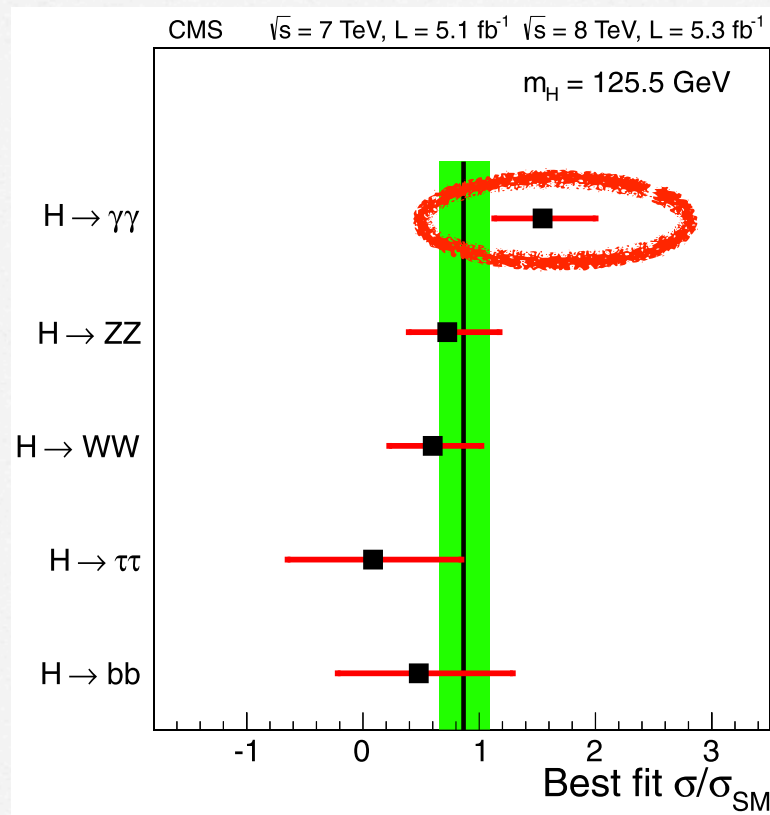
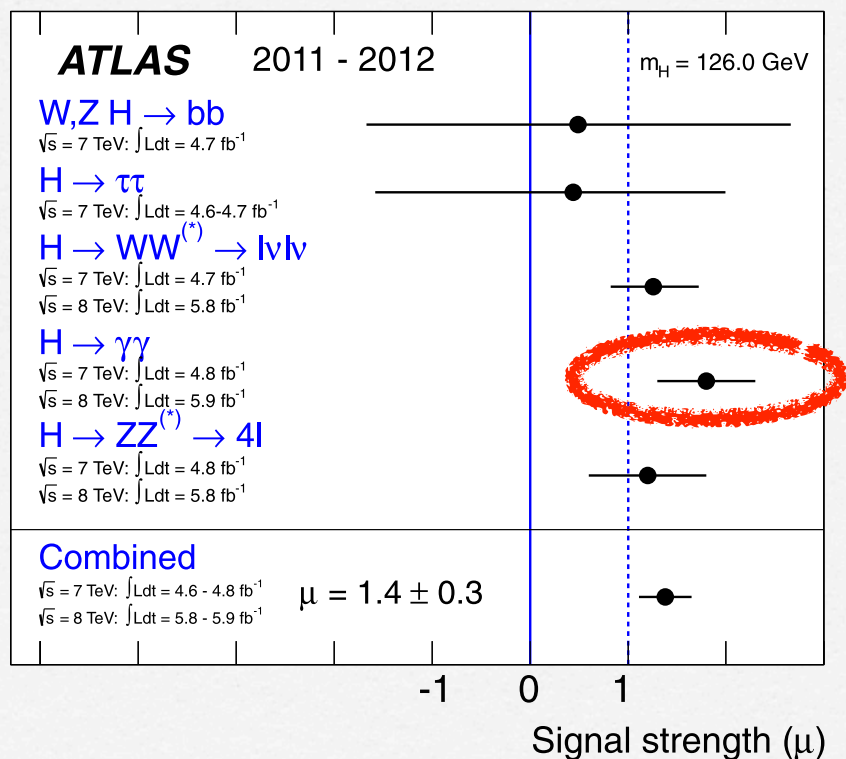


LHC search channels

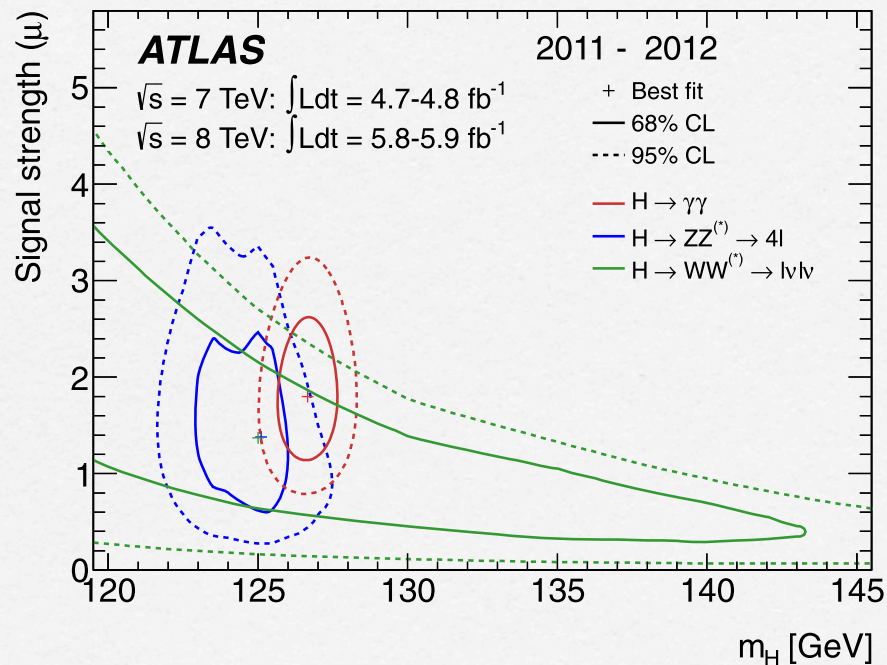


Higgs decay LHC signal strengths

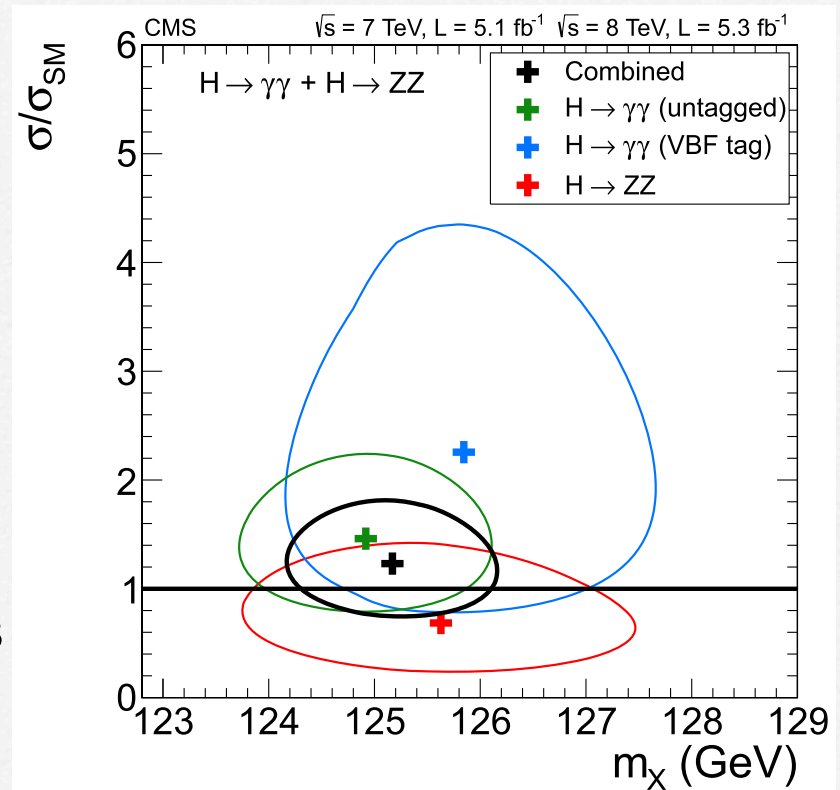
Two photon rate too high in both experiments



Higgs mass 124-127 GeV



$126.0 \pm 0.4 \text{ (stat)} \pm 0.4 \text{ (sys)} \text{ GeV}$

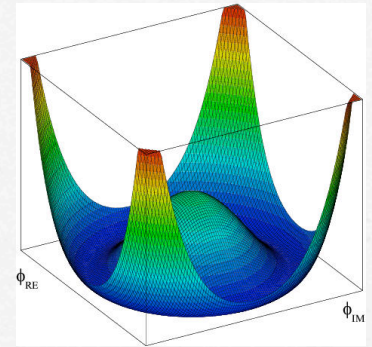


$125.3 \pm 0.4 \text{ (stat.)} \pm 0.5 \text{ (syst.)} \text{ GeV.}$

Higgs Theory in SM

Higgs potential

$$V = m_H^2 |H|^2 + \frac{1}{2} \lambda |H|^4$$

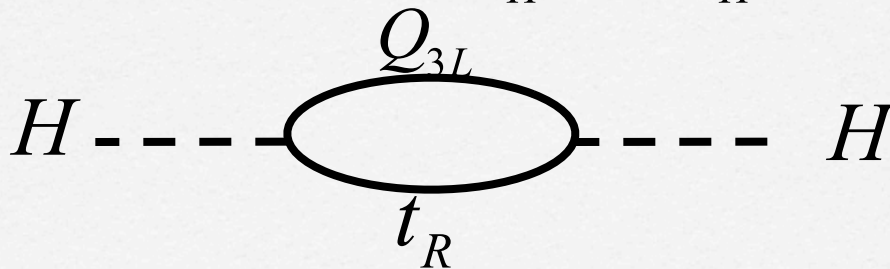


Tree-level min cond

$$m_H^2 = -\lambda v^2 = -\lambda (246 \text{ GeV})^2$$

Including rad corr

$$m_H^2 + \delta m_H^2 = -\lambda (246 \text{ GeV})^2$$



$$\delta m_H^2(\text{top loop}) = -\frac{3}{\sqrt{2}\pi^2} G_F m_t^2 \Lambda^2 = -(100 \text{ GeV})^2 \left(\frac{\Lambda}{1 \text{ TeV}} \right)^2$$

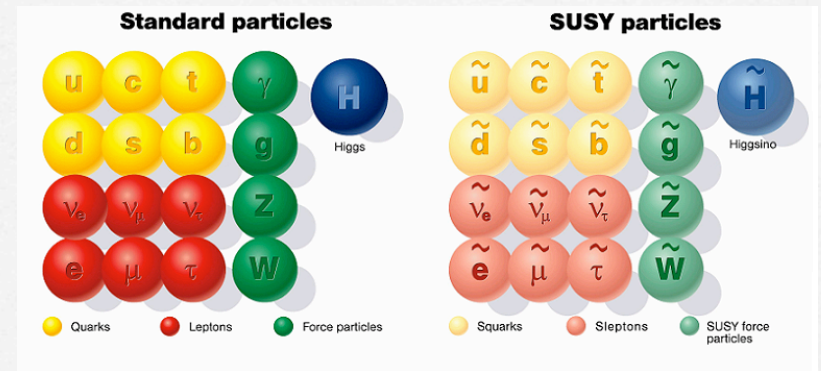
Fine-tuning is required if the cut-off $\Lambda \gg 1 \text{ TeV}$

Motivates new physics at TeV scale e.g. SUSY

Minimal SUSY SM (MSSM)

Table 1: The MSSM Particle Spectrum

Superfield	Bosons	Fermions
<u>Gauge</u>		
\widehat{G}	g	\widetilde{g}
\widehat{V}^a	W^a	\widetilde{W}^a
\widehat{V}'	B	\widetilde{B}
<u>Matter</u>		
\widehat{L} \widehat{E}^c	leptons $\left\{ \begin{array}{l} \widetilde{L} = (\widetilde{\nu}, \widetilde{e}^-)_L \\ \widetilde{E} = \widetilde{e}_R^+ \end{array} \right.$	$(\nu, e^-)_L$ e_L^c
\widehat{Q} \widehat{U}^c \widehat{D}^c	quarks $\left\{ \begin{array}{l} \widetilde{Q} = (\widetilde{u}_L, \widetilde{d}_L) \\ \widetilde{U}^c = \widetilde{u}_R^* \\ \widetilde{D}^c = \widetilde{d}_R^* \end{array} \right.$	$(u, d)_L$ u_L^c d_L^c
\widehat{H}_d \widehat{H}_u	Higgs $\left\{ \begin{array}{l} H_d^i \\ H_u^i \end{array} \right.$	$(\widetilde{H}_d^0, \widetilde{H}_d^-)_L$ $(\widetilde{H}_u^+, \widetilde{H}_u^0)_L$



Higgs/Higgsino mass parameter

$$\mu \tilde{H}_u \tilde{H}_d$$

$$|\mu| \lesssim 200 \text{ GeV.}$$

to avoid tree-level tuning since

$$m_H^2 = \mu^2 + m_0^2$$

Higgs Theory in MSSM $\mathcal{W} = \mu \hat{H}_u \hat{H}_d$

Higgs
doublets

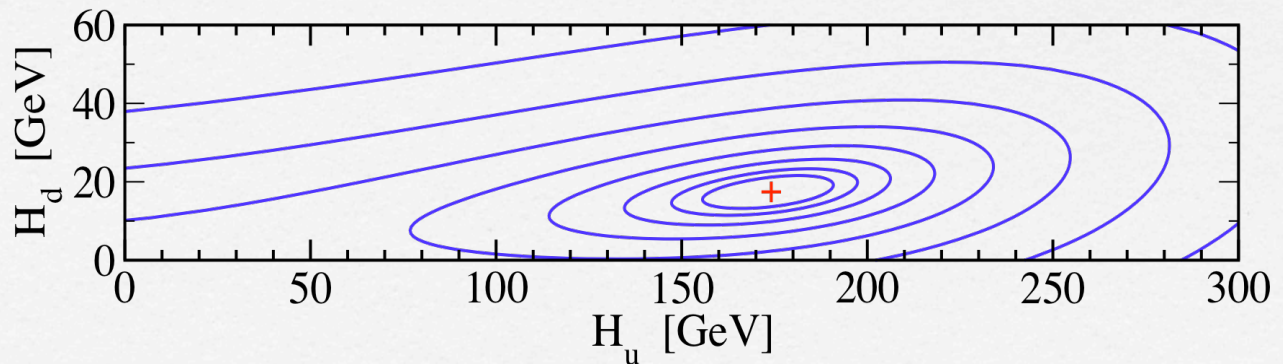
$$H_u = (H_u^+, H_u^0)$$

$$H_d = (H_d^0, H_d^-)$$

Higgs
potential

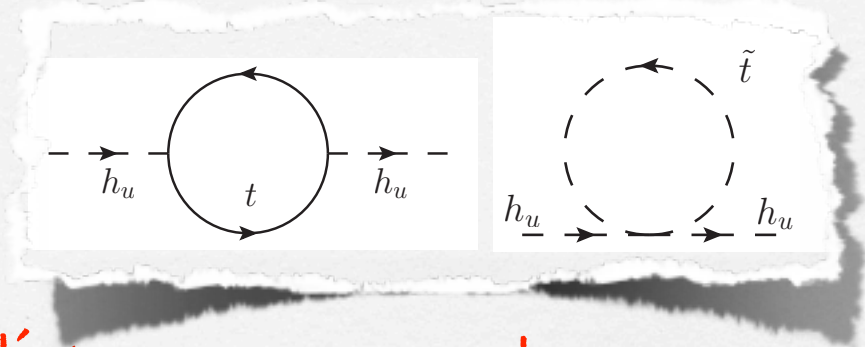
$$V = (|\mu|^2 + m_{H_u}^2)|H_u^0|^2 + (|\mu|^2 + m_{H_d}^2)|H_d^0|^2 - (b H_u^0 H_d^0 + \text{c.c.}) + \frac{1}{8}(g^2 + g'^2)(|H_u^0|^2 - |H_d^0|^2)^2.$$

$$\tan \beta = \frac{v_u}{v_d}$$



In SUSY, stop loops dominate Higgs mass parameter correction

$$\delta m_H^2 (\text{stop loop})$$



Leading quadratic divergence cancels

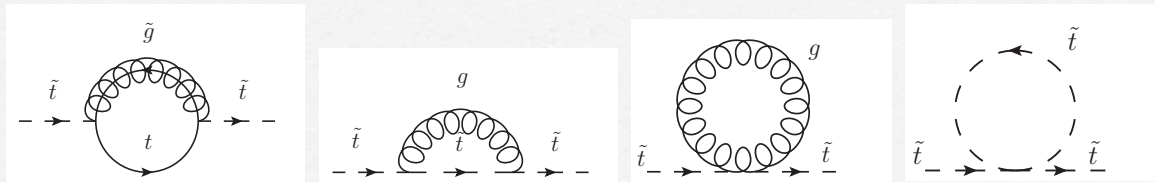
$$\delta m_{h_u}^2 = -\frac{3y_t^2}{4\pi^2} m_{\tilde{t}}^2 \ln \left(\frac{\Lambda_{UV}}{m_{\tilde{t}}} \right)$$

To avoid
tuning need

$$m_{\tilde{t}} \lesssim 400 \text{ GeV. } 500 \text{ GeV OK}$$

LHC should find stops SOON

Gluino corrections to stop



$$\delta m_{\tilde{t}}^2 = \frac{2g_s^2}{3\pi^2} m_{\tilde{g}}^2 \ln \frac{\Lambda_{UV}}{m_{\tilde{g}}}.$$

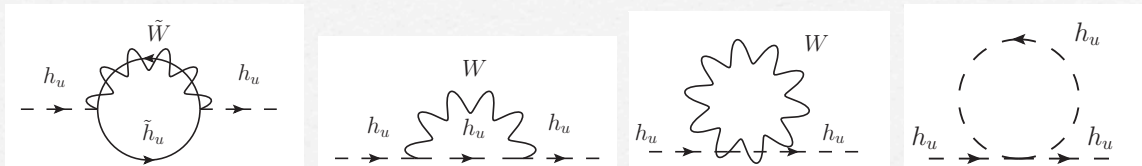
To avoid
tuning need

$$m_{\tilde{g}} \lesssim 2m_{\tilde{t}}.$$

1 TeV OK

LHC should find gluinos SOON

Other important loops



$$\delta m_{h_u}^2 = \frac{3g^2}{8\pi^2} (m_{\tilde{W}}^2 + m_{\tilde{h}}^2) \ln \frac{\Lambda_{UV}}{m_{\tilde{W}}}.$$

To avoid
tuning need

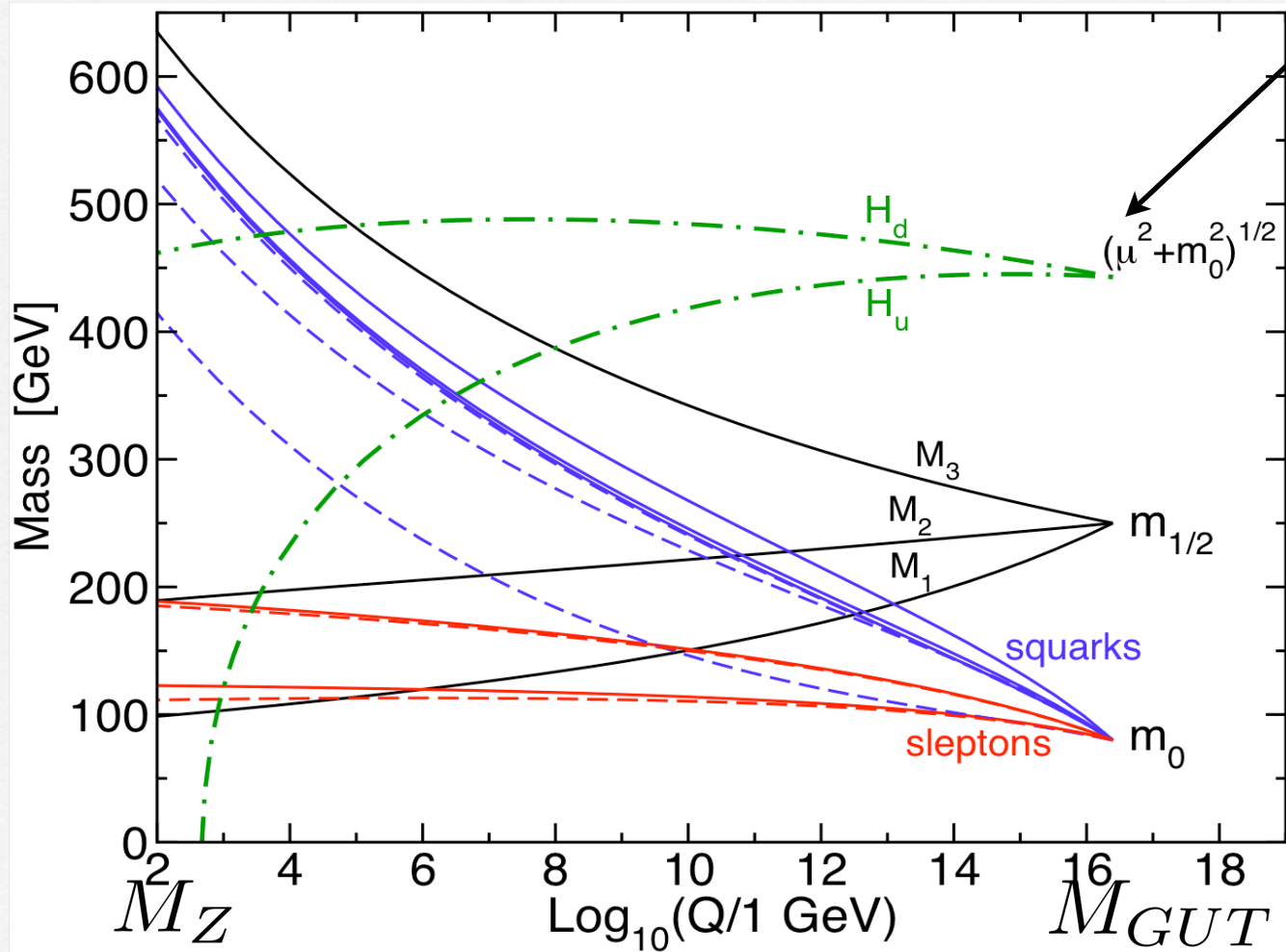
$$m_{\tilde{W}} \lesssim \text{TeV}.$$

1 TeV OK

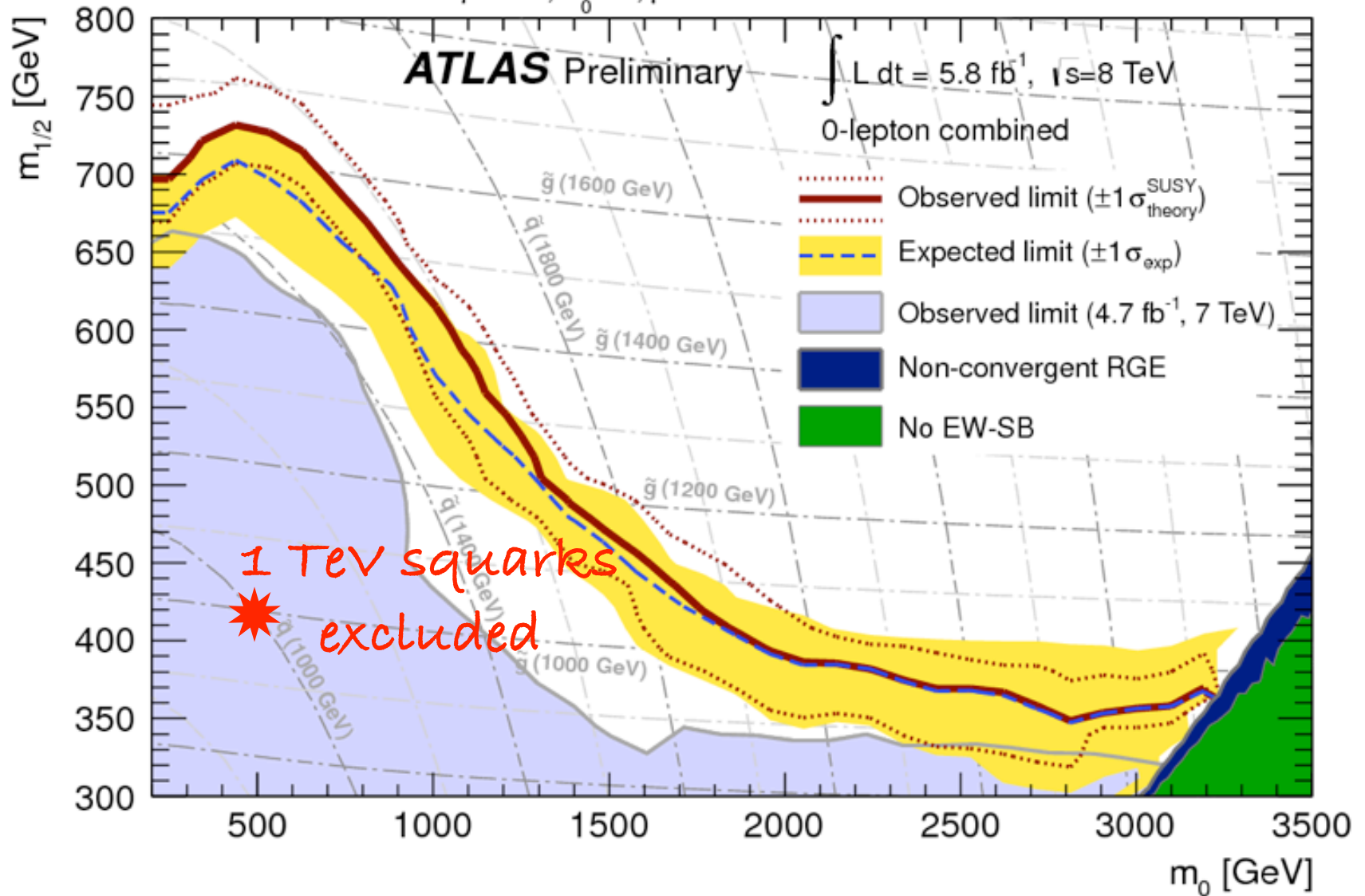
Difficult to find colour singlets at LHC

Constrained MSSM

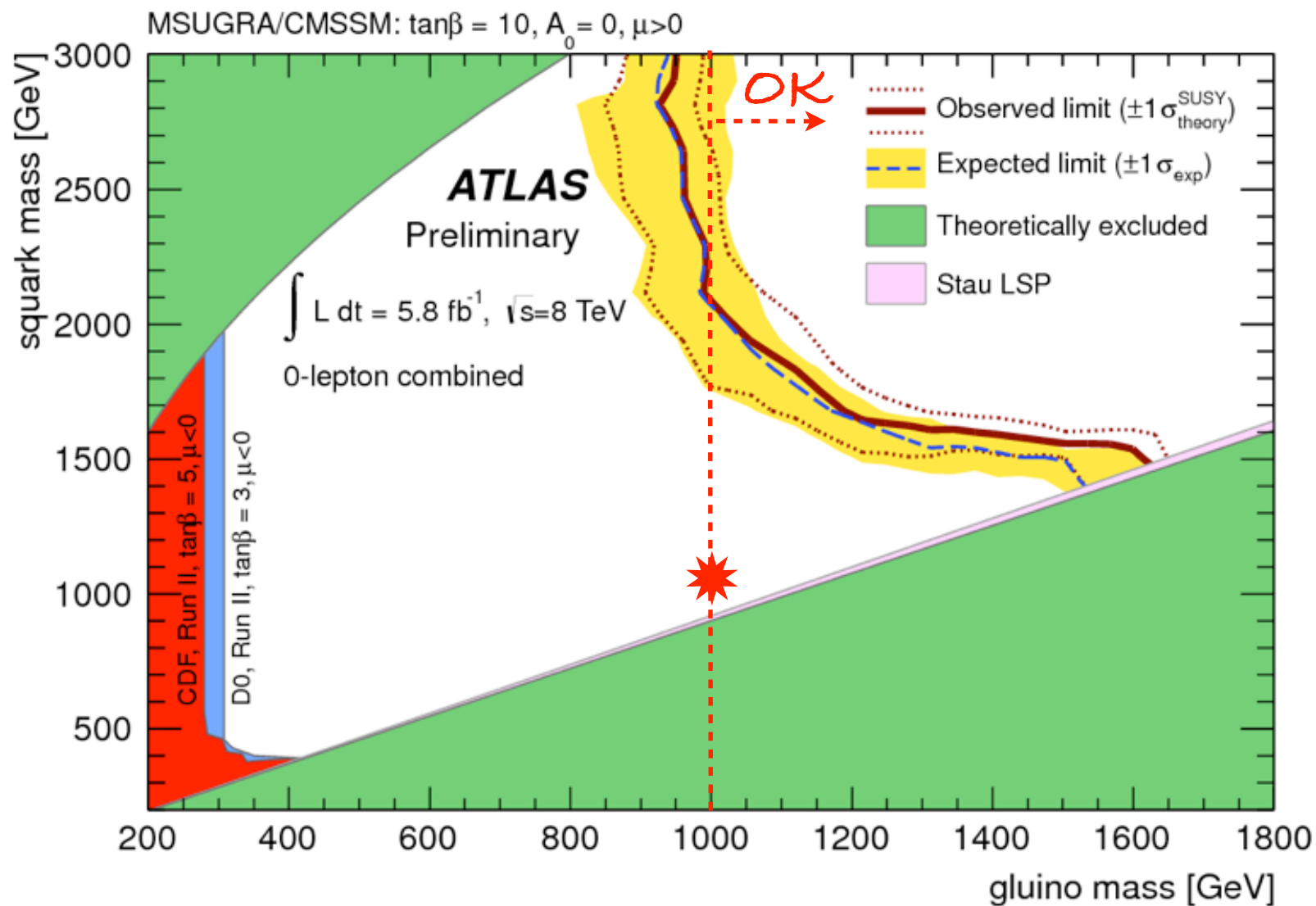
$$m_H^2 = \mu^2 + m_0^2$$



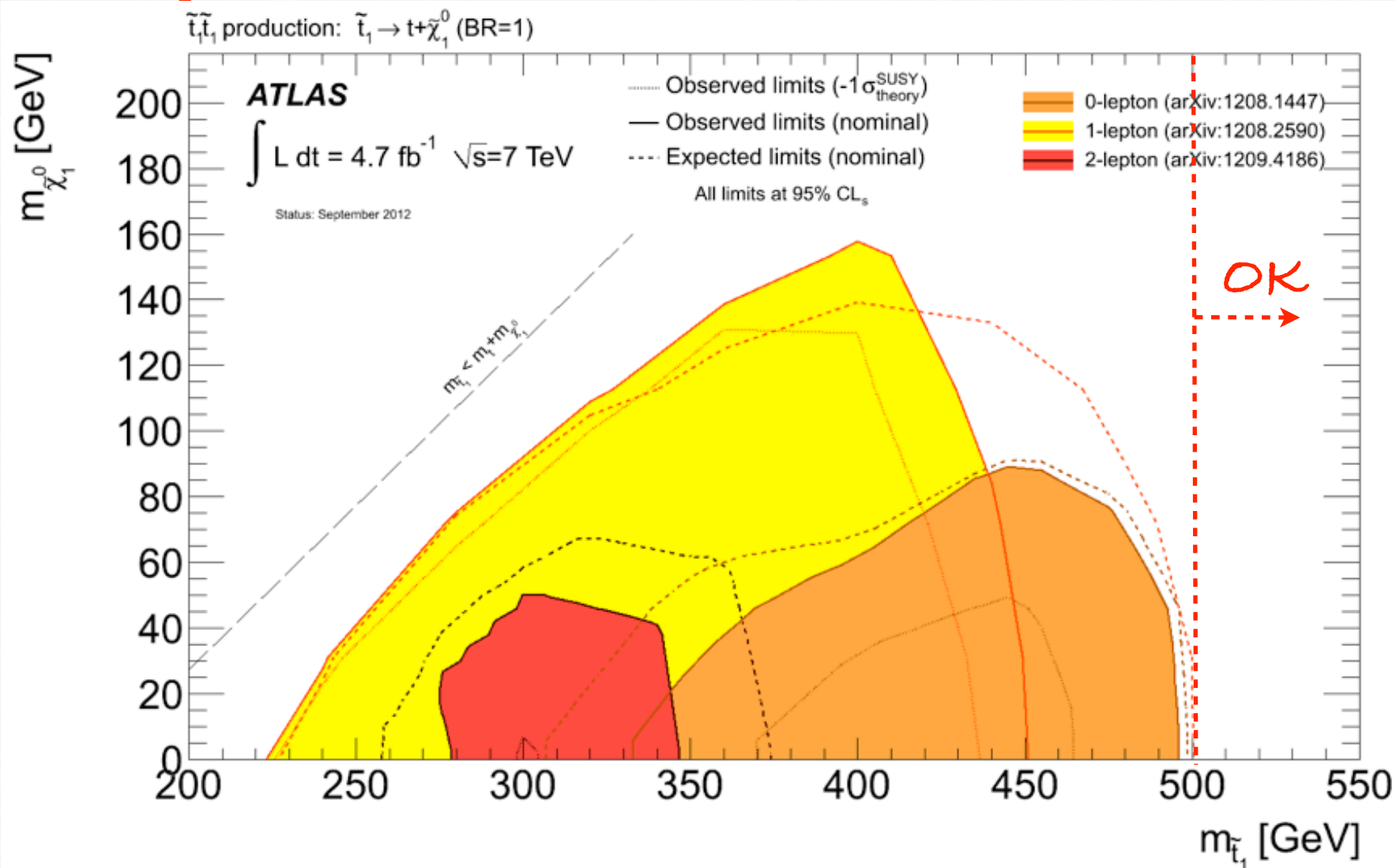
MSUGRA/CMSSM: $\tan\beta = 10$, $A_0 = 0$, $\mu > 0$



Gluinos at 1 TeV not excluded



Stops at 500 GeV not excluded



Mass Spectrum in MSSM

LHC Higgs

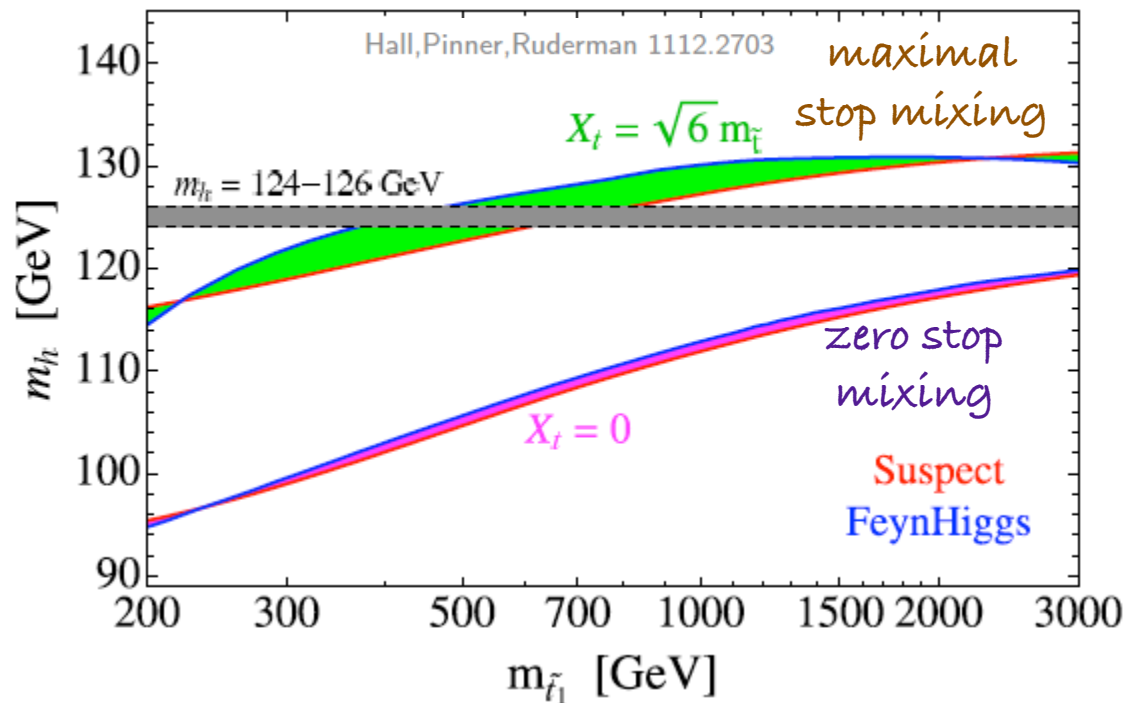
Names	Spin	P_R	Gauge Eigenstates	Mass Eigenstates
Higgs bosons	0	+1	$H_u^0 \ H_d^0 \ H_u^+ \ H_d^-$	$h^0 \ H^0 \ A^0 \ H^\pm$
squarks	0	-1	$\tilde{u}_L \ \tilde{u}_R \ \tilde{d}_L \ \tilde{d}_R$	(same)
			$\tilde{s}_L \ \tilde{s}_R \ \tilde{c}_L \ \tilde{c}_R$	(same)
			$\tilde{t}_L \ \tilde{t}_R \ \tilde{b}_L \ \tilde{b}_R$	$\tilde{t}_1 \ \tilde{t}_2 \ \tilde{b}_1 \ \tilde{b}_2$
sleptons	0	-1	$\tilde{e}_L \ \tilde{e}_R \ \tilde{\nu}_e$	(same)
			$\tilde{\mu}_L \ \tilde{\mu}_R \ \tilde{\nu}_\mu$	(same)
			$\tilde{\tau}_L \ \tilde{\tau}_R \ \tilde{\nu}_\tau$	$\tilde{\tau}_1 \ \tilde{\tau}_2 \ \tilde{\nu}_\tau$
neutralinos	1/2	-1	$\tilde{B}^0 \ \tilde{W}^0 \ \tilde{H}_u^0 \ \tilde{H}_d^0$	$\tilde{N}_1 \ \tilde{N}_2 \ \tilde{N}_3 \ \tilde{N}_4$
charginos	1/2	-1	$\tilde{W}^\pm \ \tilde{H}_u^\pm \ \tilde{H}_d^\pm$	$\tilde{C}_1^\pm \ \tilde{C}_2^\pm$
gluino	1/2	-1	\tilde{g}	(same)
goldstino (gravitino)	1/2 (3/2)	-1	\tilde{G}	(same)

Higgs h Mass in MSSM

$$\mathcal{W} = \mu \hat{H}_u \hat{H}_d$$

$$m_h^2 \approx M_Z^2 \cos^2 2\beta + \Delta m_h^2$$

MSSM Higgs Mass



$$\Delta m_h^2 \approx \frac{3}{(4\pi)^2} \frac{m_t^4}{v^2} \left[\ln \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

$$m_{\tilde{t}}^2 = m_{\tilde{Q}_3} m_{\tilde{t}_R} \quad X_t = A_t - \mu \cot \beta.$$

Must have at least one
stop mass heavier
than 500 GeV -->
Fine Tuning!

Next-to-Minimal SUSY SM (NMSSM)

Model gives dynamical origin of μ term via complex singlet S :

$$S H_u H_d \quad \text{where singlet } \langle S \rangle \sim \mu \sim \text{TeV}$$

Danger from weak scale axion due to global $U(1)$ symmetry

Need to avoid axion somehow

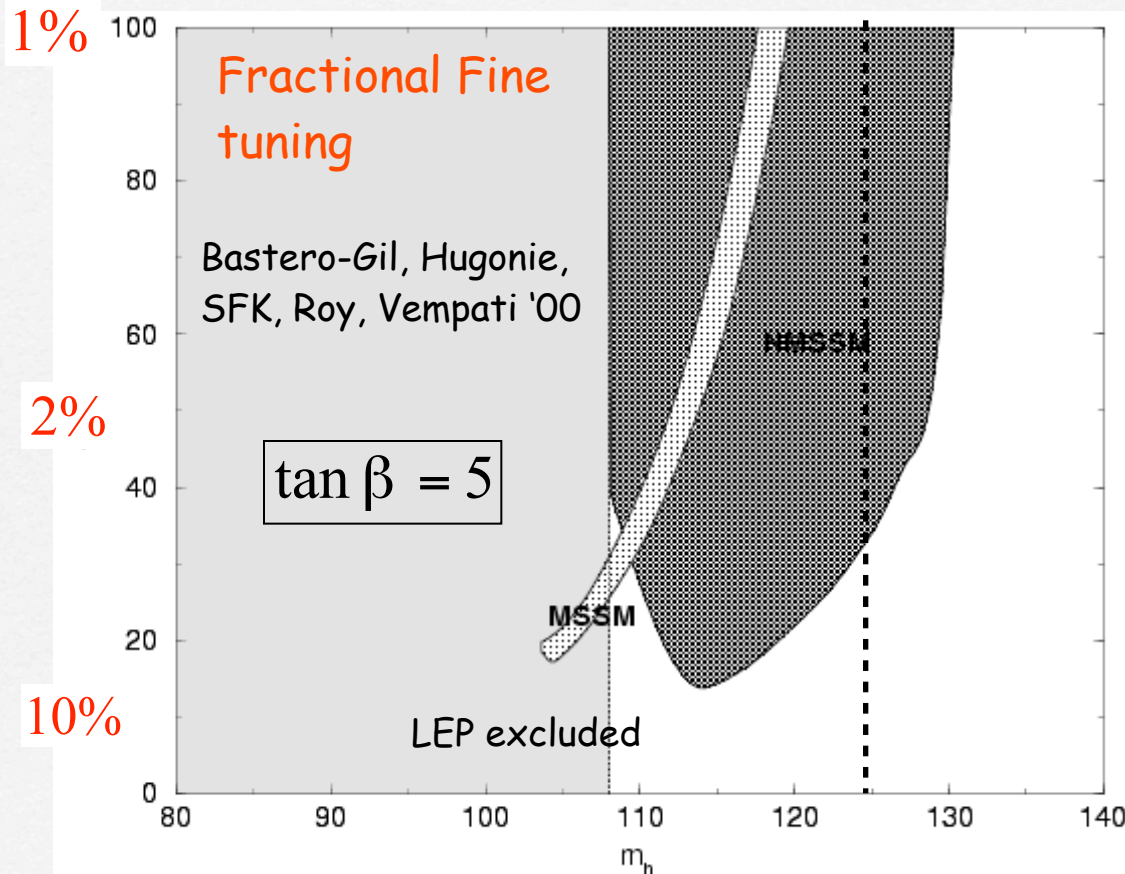
In **NMSSM** we add S^3 to break $U(1)$ to Z_3

$$\mathcal{W} = \lambda \hat{S} \hat{H}_u \hat{H}_d + \frac{\kappa}{3} \hat{S}^3$$

$$m_h^2 \approx M_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta + \Delta m_h^2$$

Extra tree-level
contribution to
Higgs mass reduces
fine-tuning

Fine Tuning vs. Higgs Mass



For 125 GeV
Higgs the
MSSM fine
tuning is
much worse
than in
NMSSM

LEP favours NMSSM over MSSM (12 years ago)
LHC with Higgs @ 125 GeV strengthens conclusion

NMSSM Higgs Theory

Spectrum has an extra CP even S plus extra CP odd A
(both singlets) compared to MSSM

CP even mass
eigenstates

$$H_1 = S_{1,d} H_d + S_{1,u} H_u + S_{1,s} S ,$$

$$H_2 = S_{2,d} H_d + S_{2,u} H_u + S_{2,s} S ,$$

$$H_3 = S_{3,d} H_d + S_{3,u} H_u + S_{3,s} S .$$

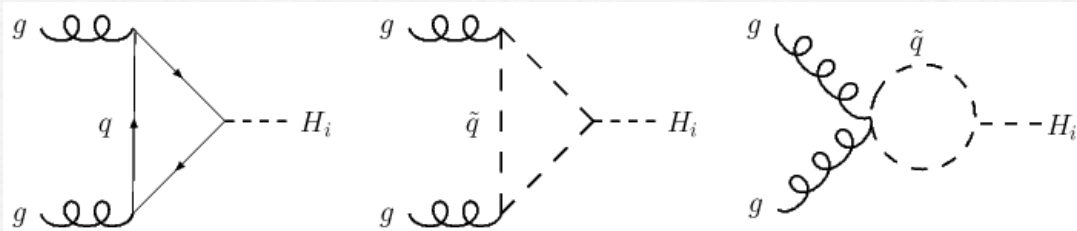
H_1 or H_2 have reduced couplings due to the singlet component

$h^{125 \text{ GeV}}$ can be H_1, H_2

NMSSM Higgs Phenomenology

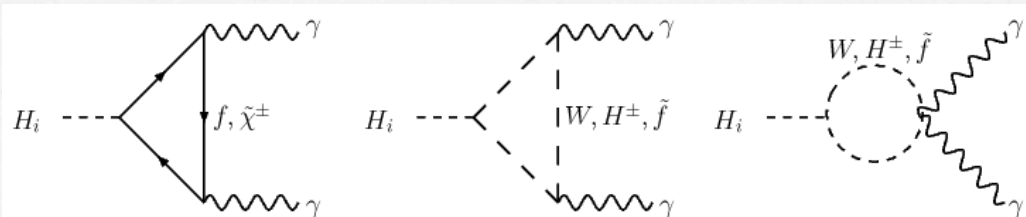
Enhanced gluon fusion production

Stop and sbottom loop contributions in $gg \rightarrow H_i$



$$BR(h^{125 \text{ GeV}} \rightarrow \gamma\gamma) = \frac{\Gamma(h^{125 \text{ GeV}} \rightarrow \gamma\gamma)}{(\Gamma_{b\bar{b}} + \Gamma_{WW} + \Gamma_{ZZ} + \dots)[h^{125 \text{ GeV}}]}$$

Suppression of $\Gamma(h^{125 \text{ GeV}} \rightarrow b\bar{b})$ due to strong singlet-doublet mixing



Enhanced $\Gamma(h^{125 \text{ GeV}} \rightarrow \gamma\gamma)$ due to chargino loop contributions

NMSSM Higgs Benchmarks Near 125 GeV

Point	NMP1	NMP2	NMP3
$\tan \beta$	3	2	2
μ_{eff} [GeV]	200	200	200
λ	0.64	0.6	0.57
κ	0.25	0.18	0.2
A_λ [GeV]	560	405	395
A_κ [GeV]	-10	-10	-80
$M_{Q_{3L}}$ [GeV]	650	700	530
M_{t_R} [GeV]	650	700	530
M_1 [GeV]	106	91	115
M_2 [GeV]	200	200	200
M_3 [GeV]	600	600	600

SM-like Higgs boson H_1			
M_{H_1} [GeV]	124.5	126.5	124.6
$R_{\gamma\gamma}(H_1)$	1.06	1.24	1.47
$R_{WW}(H_1)$	0.85	0.93	1.02
$R_{ZZ}(H_1)$	0.76	0.85	0.90
$R_{b\bar{b}}(H_1)$	1.12	1.09	1.04
$R_{\Gamma_{\text{tot}}}(H_1)$	1.02	0.93	0.76
$R_{\sigma_{gg}}(H_1)$	0.97	0.96	0.77
$R_{\sigma_{\text{tot}}}(H_1)$	0.84	0.91	0.82

$m_{\tilde{t}_1}$ [GeV]	548	587	358
$m_{\tilde{t}_2}$ [GeV]	782	838	686
$X_t/m_{\tilde{t}}$	1.74	1.86	2.26

Relic density			
Ωh^2	0.9819	0.1170	0.1100

Point	NMP4	NMP5	NMP6
$\tan \beta$	3	3	2
μ_{eff} [GeV]	200	200	140
λ	0.67	0.66	0.55
κ	0.1	0.12	0.31
A_λ [GeV]	650	650	210
A_κ [GeV]	-10	-10	-210
$M_{Q_{3L}}$ [GeV]	600	600	800
M_{t_R} [GeV]	600	600	600
M_1 [GeV]	200	200	145
M_2 [GeV]	400	400	300
M_3 [GeV]	600	600	800

SM-like Higgs boson H_2			
M_{H_2} [GeV]	123.8	126.5	124.5
$R_{\gamma\gamma}(H_2)$	1.09	1.19	1.431
$R_{WW}(H_2)$	0.91	0.98	1.00
$R_{ZZ}(H_2)$	0.80	0.89	0.89
$R_{b\bar{b}}(H_2)$	1.08	1.06	1.04
$R_{\Gamma_{\text{tot}}}(H_2)$	0.96	0.90	0.78
$R_{\sigma_{gg}}(H_2)$	1.00	0.96	0.91
$R_{\sigma_{\text{tot}}}(H_2)$	0.92	0.95	0.93

$m_{\tilde{t}_1}$ [GeV]	517	483	549
$m_{\tilde{t}_2}$ [GeV]	724	741	892
$X_t/m_{\tilde{t}}$	1.56	1.89	-1.83

Relic density			
Ωh^2	0.0999	0.1352	0.1258

King, Muhlleitner, Nevzorov
arXiv:1201.2671

Key features:

- Stops below 1 TeV
in all cases

- Two photon Higgs
rate enhanced

$$R_{\gamma\gamma}(H_i) \equiv R_{\sigma_{\text{incl}}}(H_i) R_{\gamma\gamma}^{BR}(H_i)$$

$$R_{VV}(H_i) \equiv R_{\sigma_{\text{incl}}}(H_i) R_{VV}^{BR}(H_i)$$

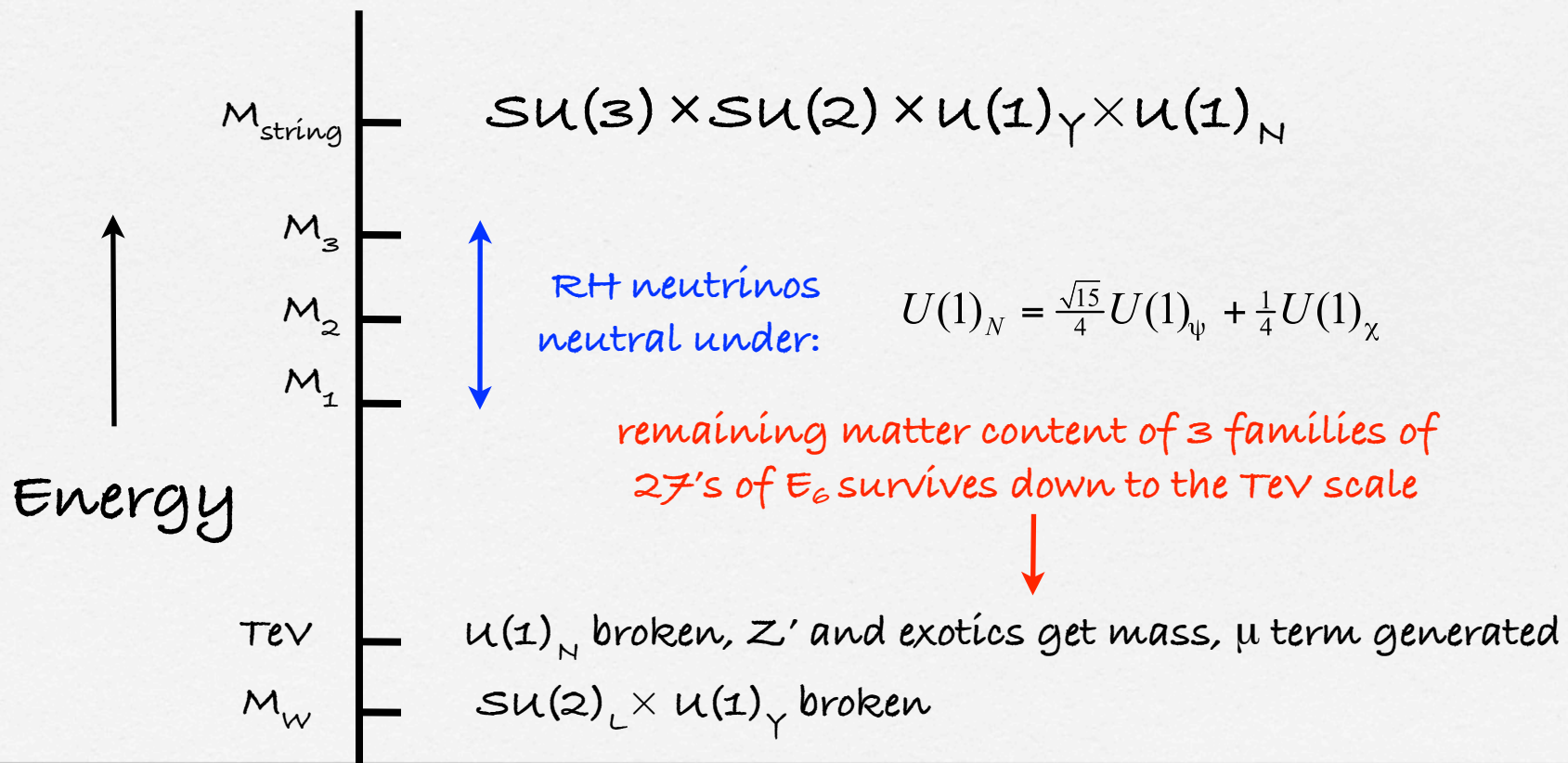
$$R_{b\bar{b}}(H_i) \equiv R_{\sigma_{\text{incl}}}(H_i) R_{b\bar{b}}^{BR}(H_i)$$

Summary of Part 1

- Particle discovered at LHC consistent with SM Higgs boson
- But LHC Higgs decay signal strengths have large errors (two photon rate too high)
- Higgs may be window into BSM physics
- Higgs theory fine-tuning problem solved by SUSY
- Natural SUSY requires stops = 500 GeV, gluino = 1 TeV (or less)
- These are not excluded by LHC searches (so far!)
- Stops > 500 GeV required for Higgs mass in MSSM
- Stops = 500 GeV possible for Higgs mass in NMSSM
- NMSSM can lead to large di-photon rate especially with $h(125) = H_2$
- Other decays such as WW , ZZ , bb , $\tau\tau$ can also have different rates
- We eagerly await the next LHC results!

Exceptional SUSY SM (E_6 SSM)

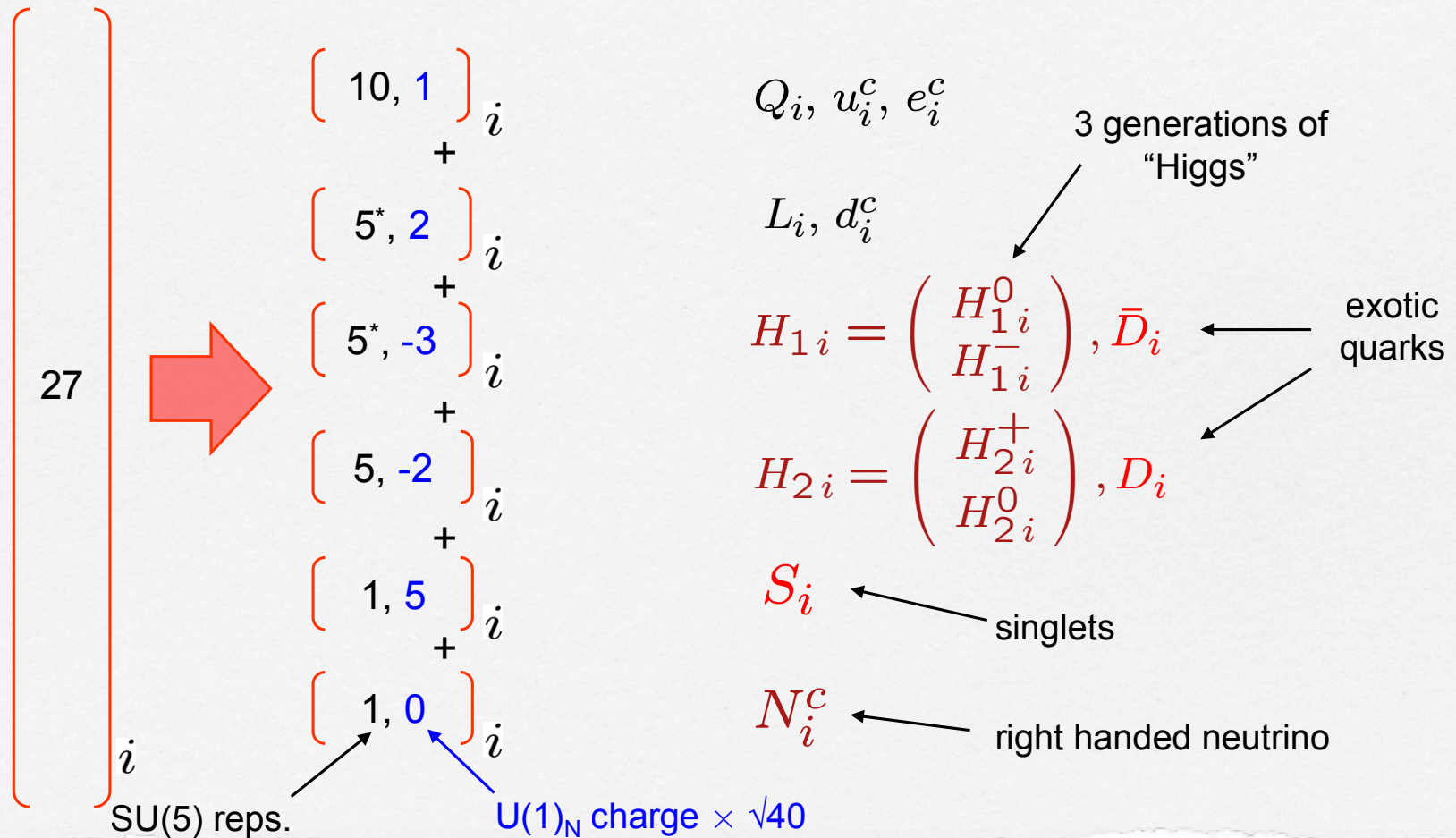
$$E_6 \rightarrow SO(10) \times U(1)_\psi \quad SO(10) \rightarrow SU(5) \times U(1)_\chi$$



Matter Content of 27's of E_6

All the SM matter fields are contained in one 27-plet of E_6 per generation.

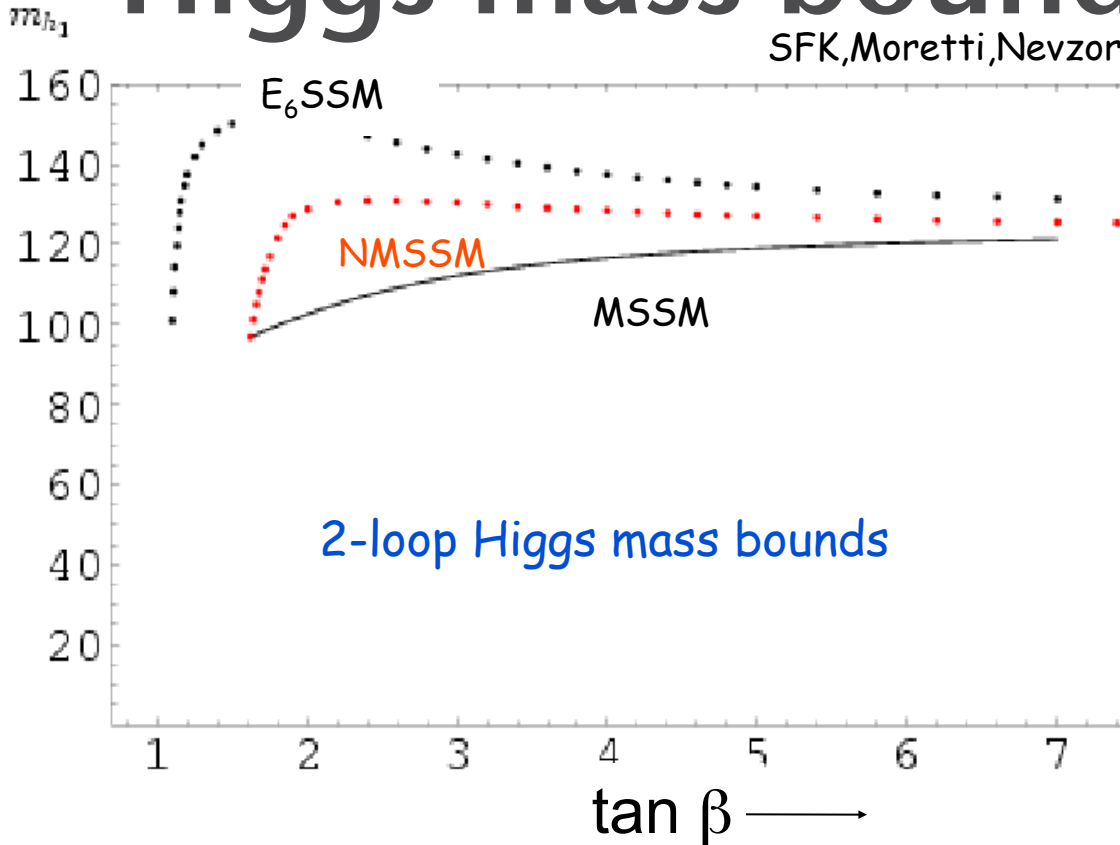
Miller



Higgs mass bounds

SFK, Moretti, Nevzorov

m_h



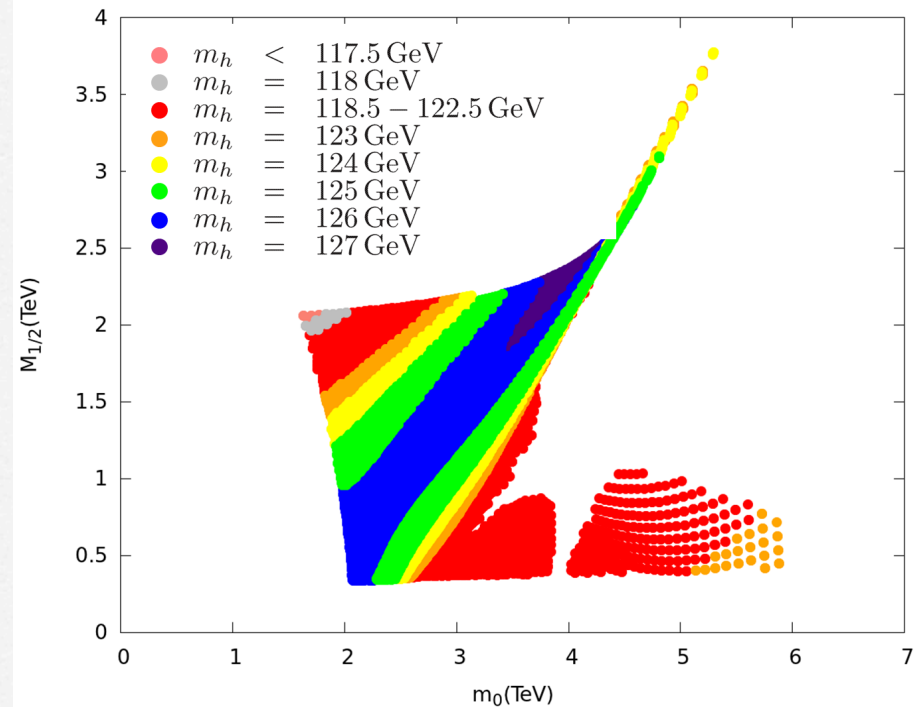
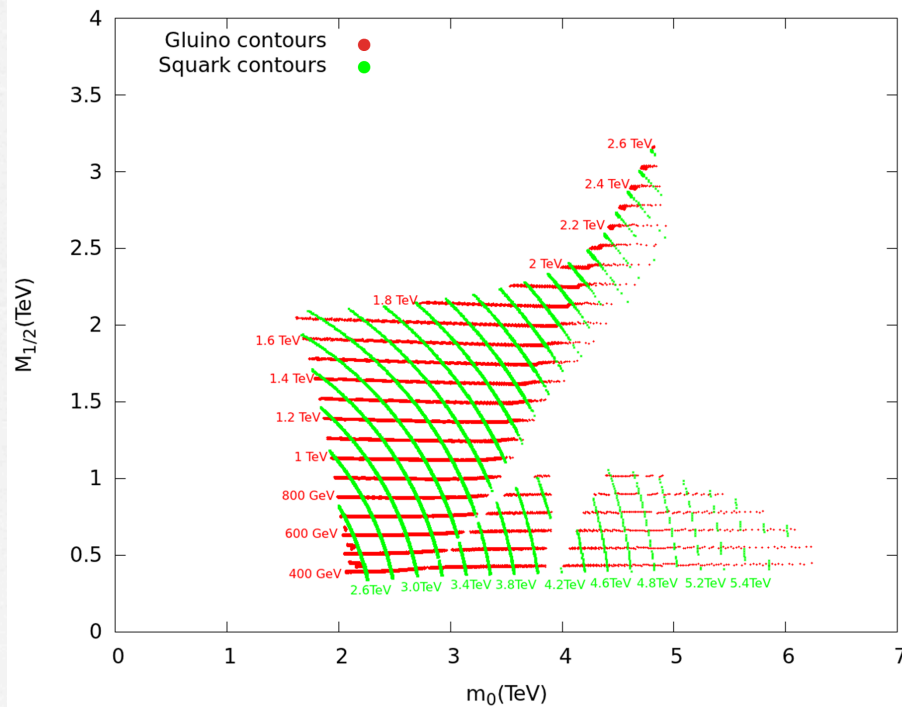
$$m_h^2 \approx \underbrace{M_Z^2 \cos^2 2\beta}_{MSSM} + \frac{\lambda^2}{2} v^2 \sin^2 2\beta + \frac{M_Z^2}{4} \left(1 + \frac{1}{4} \cos 2\beta\right)^2 + \Delta m_h^2$$

$\underbrace{\hspace{10em}}_{NMSSM}$
 $\underbrace{\hspace{15em}}_{E_6SSM}$

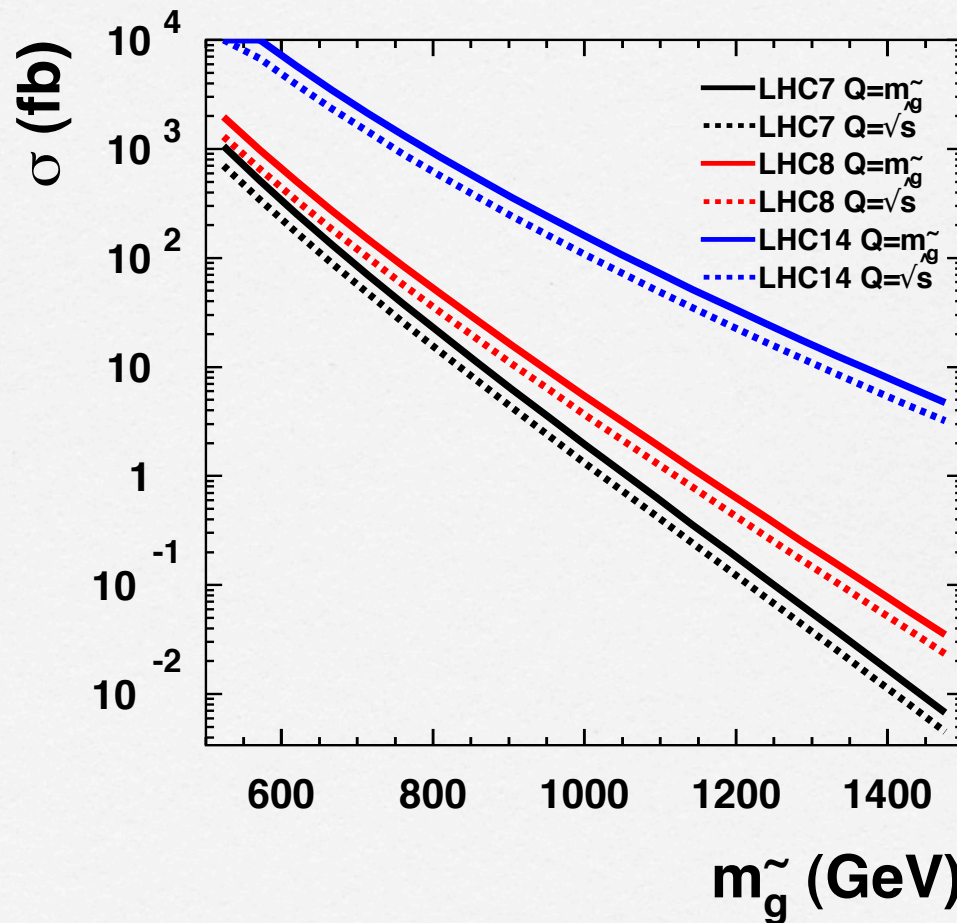
Higgs, Squarks, Gluinos in CE6SSM

Athron, King, Miller, Moretti, Nevzorov

$$\tan \beta = 10, \lambda_{12} = 0.1, s = 10 \text{ TeV.}$$

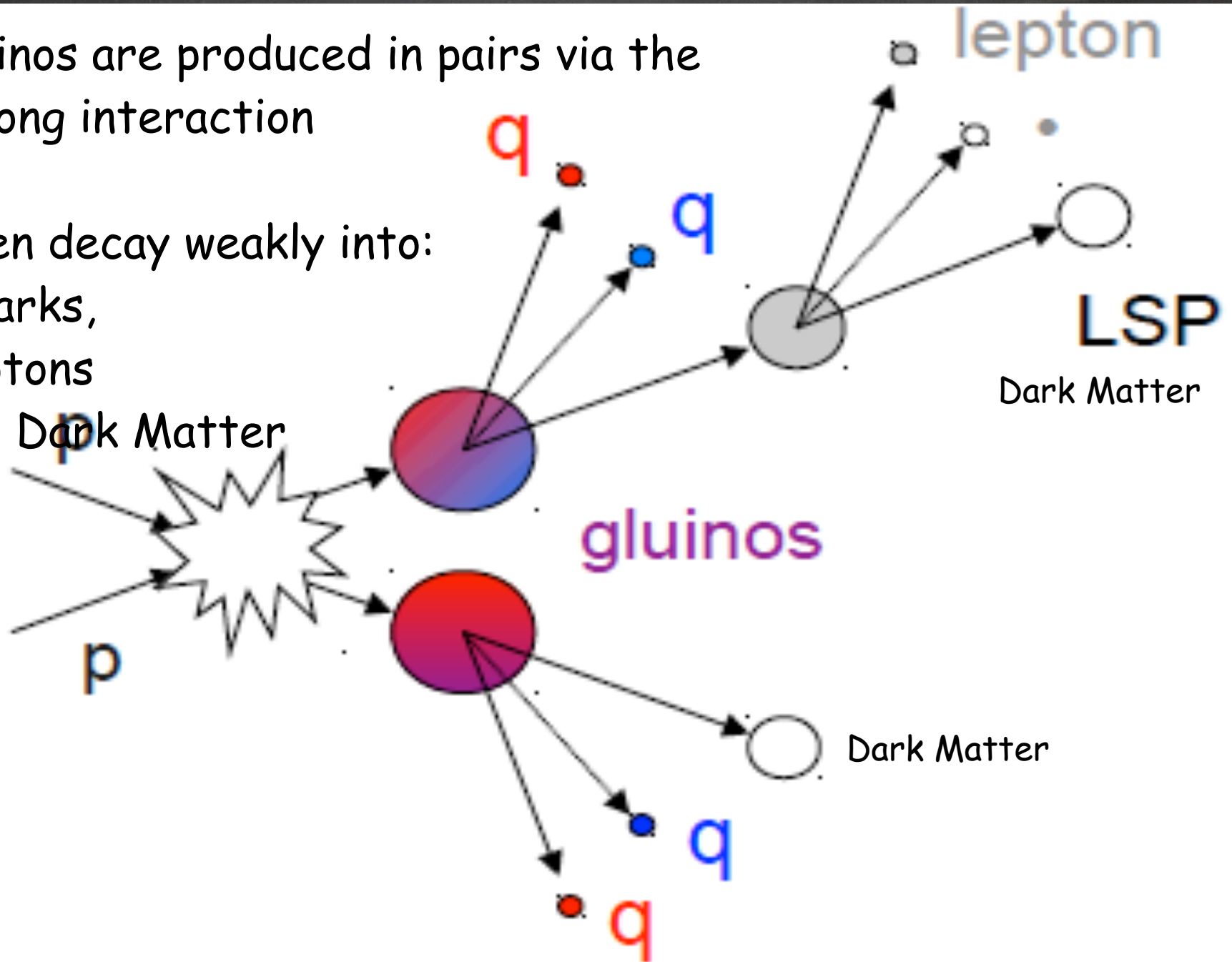


Gluino pair production



Gluginos are produced in pairs via the strong interaction

Then decay weakly into:
Quarks,
Leptons
and Dark Matter



Neutralinos in E₆SSM

Hall, King

- 3 Higgs families = 1 MSSM family $H_u H_d$ + 2 inert families $H_{u1} H_{d1} H_{u2} H_{d2}$
- 3 families of singlets = 1 NMSSM singlet S + 2 inert singlets $S_1 S_2$

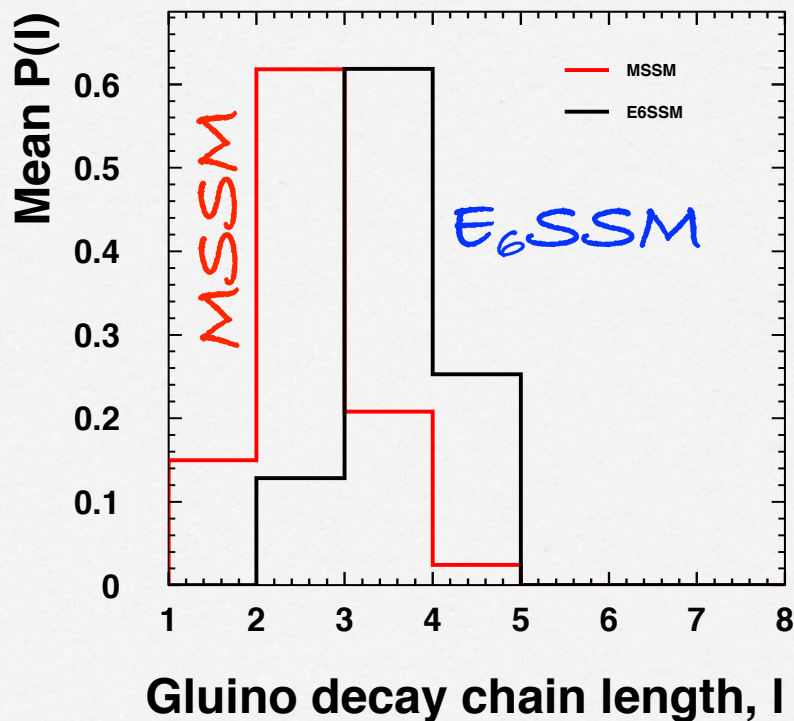
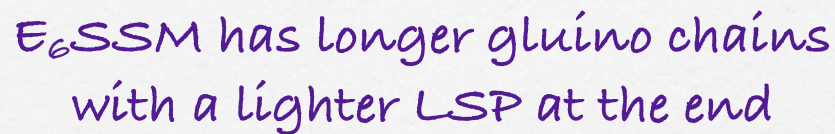
The full neutralino mass matrix

$$\tilde{\chi}_{\text{int}}^0 = (\underbrace{\tilde{B} \quad \tilde{W}^3 \quad \tilde{H}_d^0 \quad \tilde{H}_u^0}_{M_{\text{USSM}}^n} \mid \underbrace{\tilde{S} \quad \tilde{B}'}_{B_2} \mid \underbrace{\tilde{H}_{d2}^0 \quad \tilde{H}_{u2}^0 \quad \tilde{S}_2}_{B_1} \mid \underbrace{\tilde{H}_{d1}^0 \quad \tilde{H}_{u1}^0 \quad \tilde{S}_1}_{A_{21}})^T$$

$$M_{\text{E}_6\text{SSM}}^n = \begin{pmatrix} M_{\text{USSM}}^n & B_2 & B_1 \\ B_2^T & A_{22} & A_{21} \\ B_1^T & A_{21}^T & A_{11} \end{pmatrix}$$

12x12 matrix!!

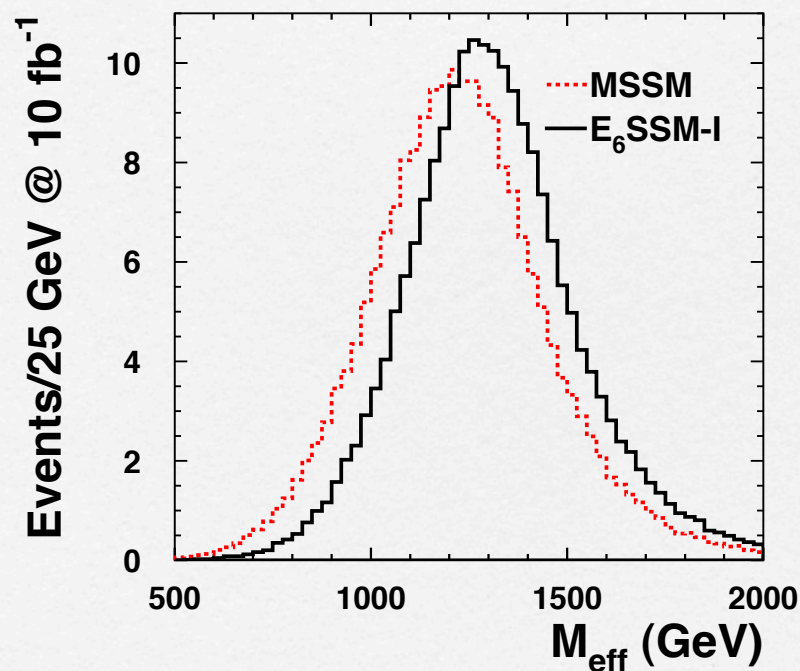
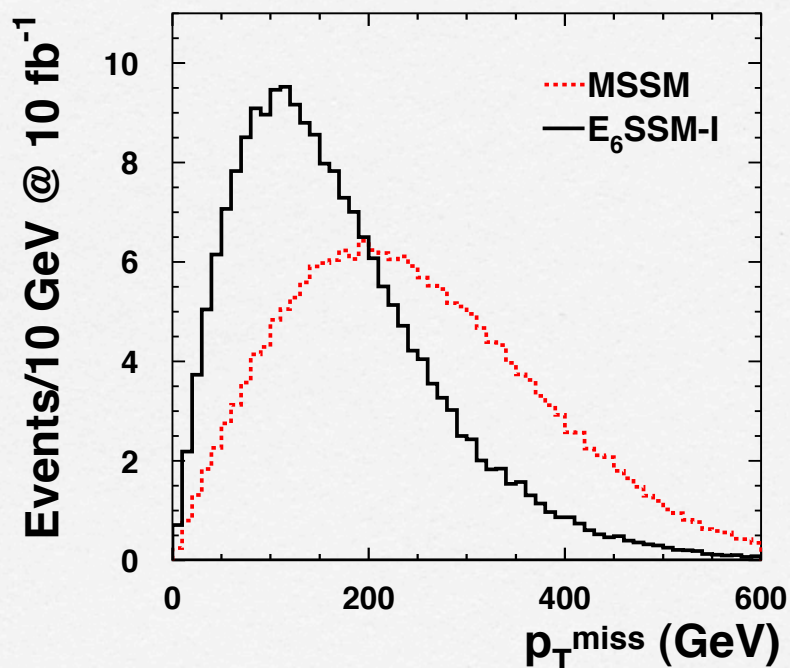
Belyaev, Hall, King,
Svantesson (preliminary)



	MSSM	E ₆ SSM-I	E ₆ SSM-II	E ₆ SSM-III	E ₆ SSM-IV	E ₆ SSM-V	E ₆ SSM-VI	
$\tan \beta$	10	1.5	1.42	1.77	3	1.42	1.42	
λ	-	0.497	0.598	-0.462	-0.4	0.598	0.598	
s	-	5180	5268	5418	5500	5268	5268	
μ	1578	(1820)	(2228)	(1770)	(-1556)	(2228)	(2228)	
$A_t = A_b = A_\tau$	-2900	-3110	-3100	476.2	4638	-2684	-2684	
M_A	302.5	3666	4365	2074	4341	4010	4000	[GeV]
M_1	150	150	150	150	150	150	150	
M_2	285	300	300	300	300	300	300	
$M_{1'}$	-	151	151	151	151	151	151	
$m_{\tilde{g}}$	800.2	800.0	800.0	800.0	800.0	800.0	800.0	
$m_{\tilde{\chi}_{M1}^0}$	148.7	148.9	149.1	151.2	150.6	149.1	149.1	
$m_{\tilde{\chi}_{M2}^0}$	302.2	296.1	296.8	303.7	301.7	296.8	296.8	
$m_{\tilde{\chi}_{M3}^0}$	1582	1763	2233	1766	1557	2233	2233	
$m_{\tilde{\chi}_{M4}^0}$	1584	1823	2246	1771	1558	2246	2246	
$m_{\tilde{\chi}_{M1}^\pm}$	302.2	299.0	299.2	300.9	300.4	299.2	299.2	
$m_{\tilde{\chi}_{M2}^\pm}$	1584	1822	2229	1771	1557	2229	2229	
$m_{\tilde{\chi}_{U1}^0}$	-	1878	1835	1909	1937	1835	1835	[GeV]
$m_{\tilde{\chi}_{U2}^0}$	-	1973	2003	2062	2087	2003	2003	
$m_{\tilde{\chi}_{E1}^0}$	-	62.7	43.5	45.2	0	0	0.00011	
$m_{\tilde{\chi}_{E2}^0}$	-	62.8	48.6	53.2	0	0	1.53	
$m_{\tilde{\chi}_{E3}^0}$	-	119.8	131.3	141.6	164.1	119.9	120.1	
$m_{\tilde{\chi}_{E4}^0}$	-	121.0	163.6	187.4	164.1	119.9	122.8	
$m_{\tilde{\chi}_{E5}^0}$	-	183.0	197.0	227.8	388.9	185.8	185.8	
$m_{\tilde{\chi}_{E6}^0}$	-	184.4	224.3	265.6	388.9	185.8	187.0	
$m_{\tilde{\chi}_{E1}^\pm}$	-	109.8	119.9	122.7	164.1	119.9	119.9	
$m_{\tilde{\chi}_{E2}^\pm}$	-	117.7	185.8	225.1	388.9	185.8	185.8	
m_h	124.4	125.4	133.8	116.3	124.7	126.1	125.8	
$P(l=1)$	0.188	$< 10^{-9}$	$< 10^{-5}$	$< 10^{-5}$	0.1727	$< 10^{-8}$	$< 10^{-12}$	
$P(l=2)$	0.812	$< 10^{-4}$	0.01524	0.1723	0.8273	0.01	$< 10^{-5}$	
$P(l=3)$	0	0.1746	0.2336	0.7986	$< 10^{-6}$	0.2	0.1721	
$P(l=4)$	0	0.8196	0.7512	0.02915	$< 10^{-15}$	0.8	0.8280	
$P(l=5)$	0	0.0058	$< 10^{-7}$	0	0	$< 10^{-15}$	0	
Ωh^2	0.00628	0.00114	0.0006842	0.0006937	0.101	0.00154		
σ_{SI}	0.401×10^{-9}	15.34×10^{-8}	9.35×10^{-8}	16.35×10^{-8}	3.75×10^{-11}	3.98×10^{-13}		[pb]

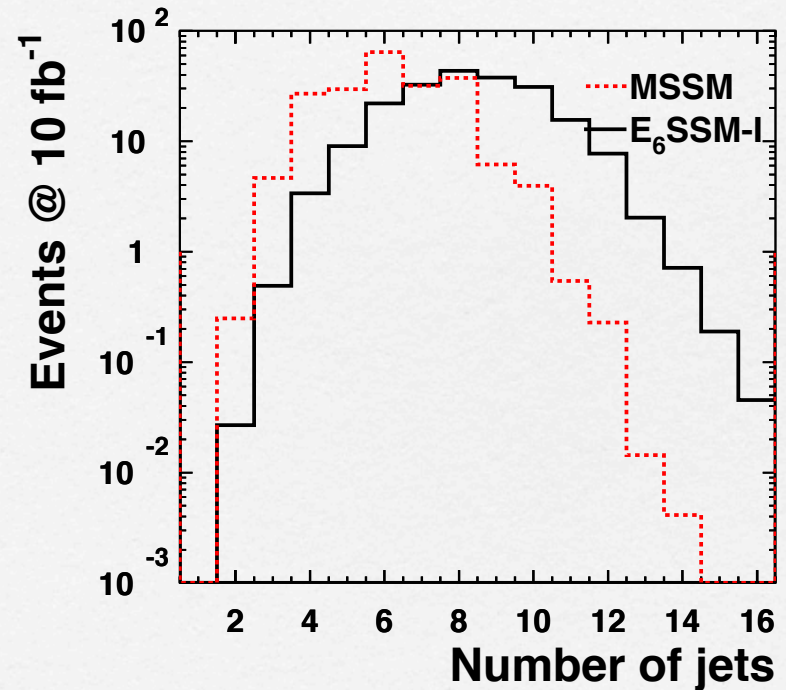
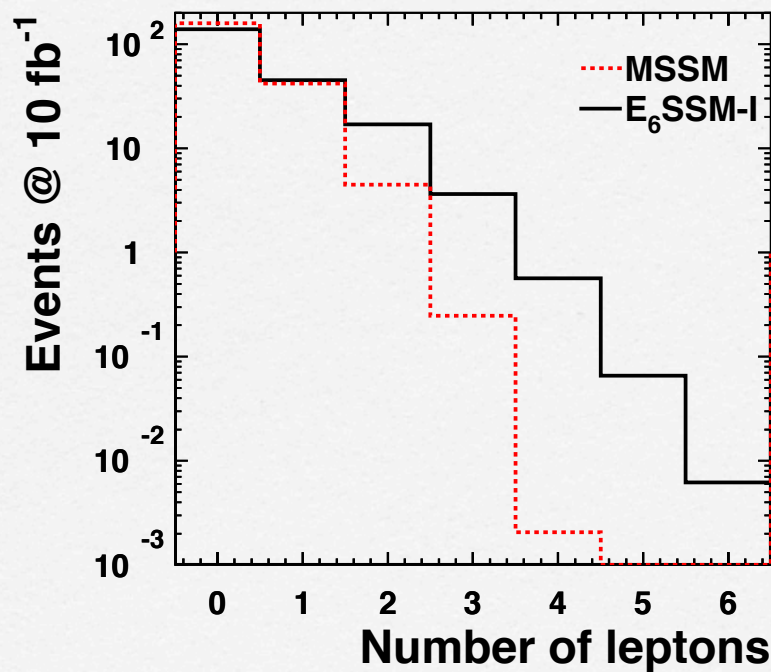
E_6SSM gluino gives less p_T^{miss}

Belyaev, Hall, King,
Svantesson (preliminary)



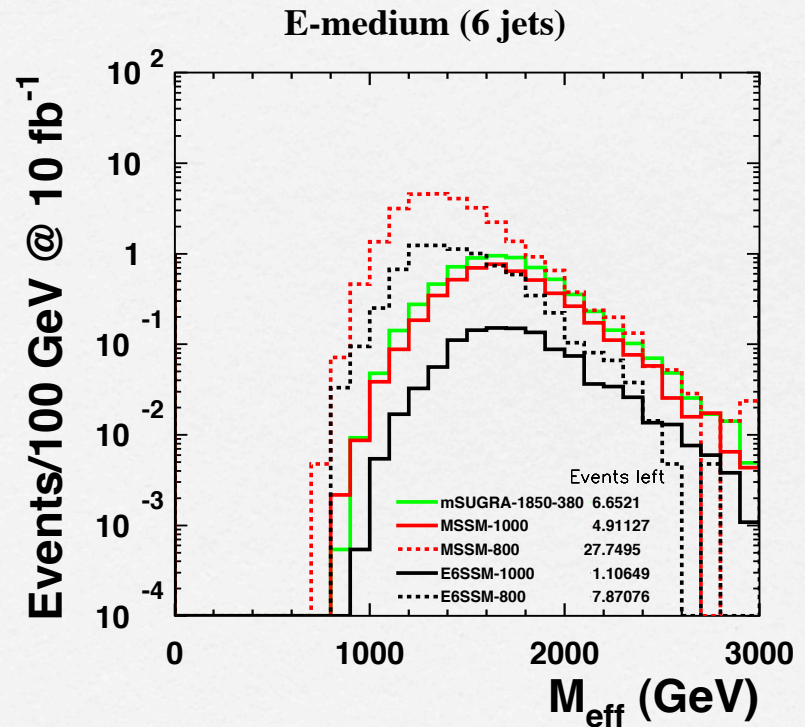
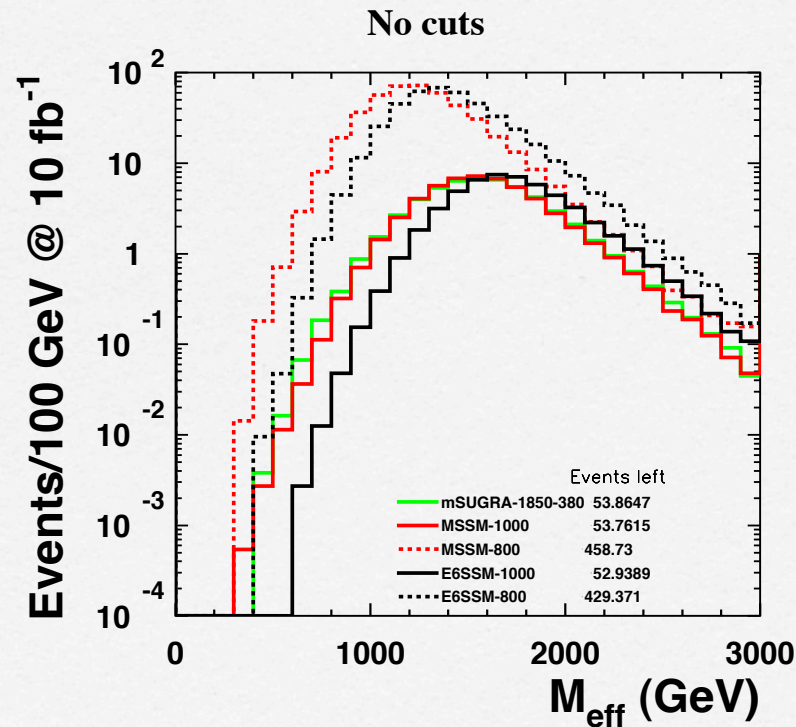
E_6 SSM gluino gives more jets and leptons

Belyaev, Hall, King,
Svantesson (preliminary)

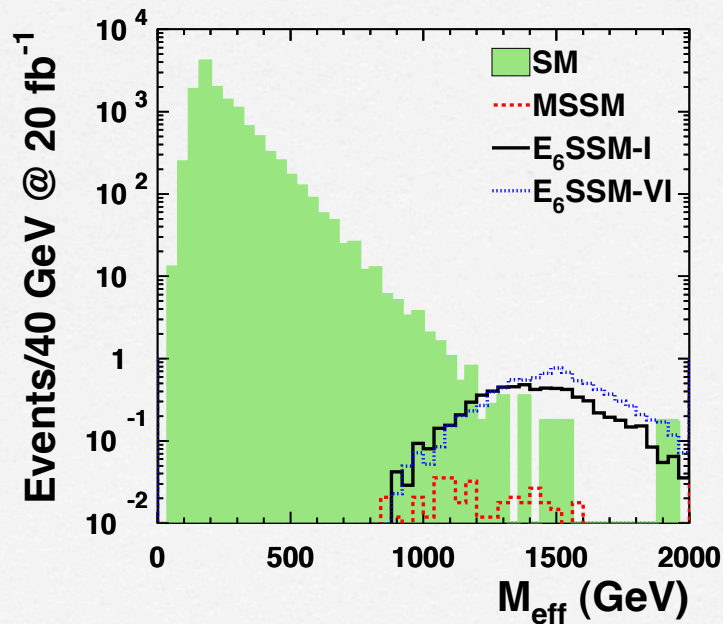


LHC@7 TeV, gluino@800 GeV

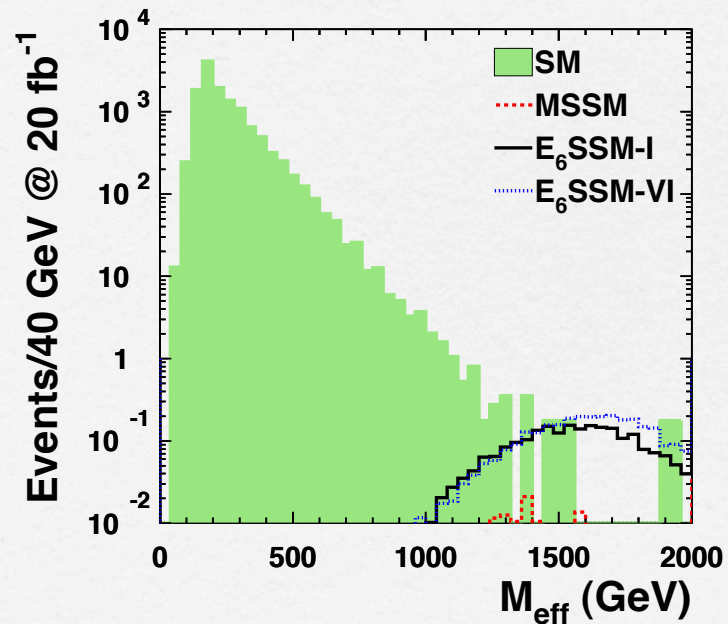
E_6 SSM gluino harder to see in 6 jet channel



E_6 SSM gluino easier to see in 3 lepton channel at 8 TeV

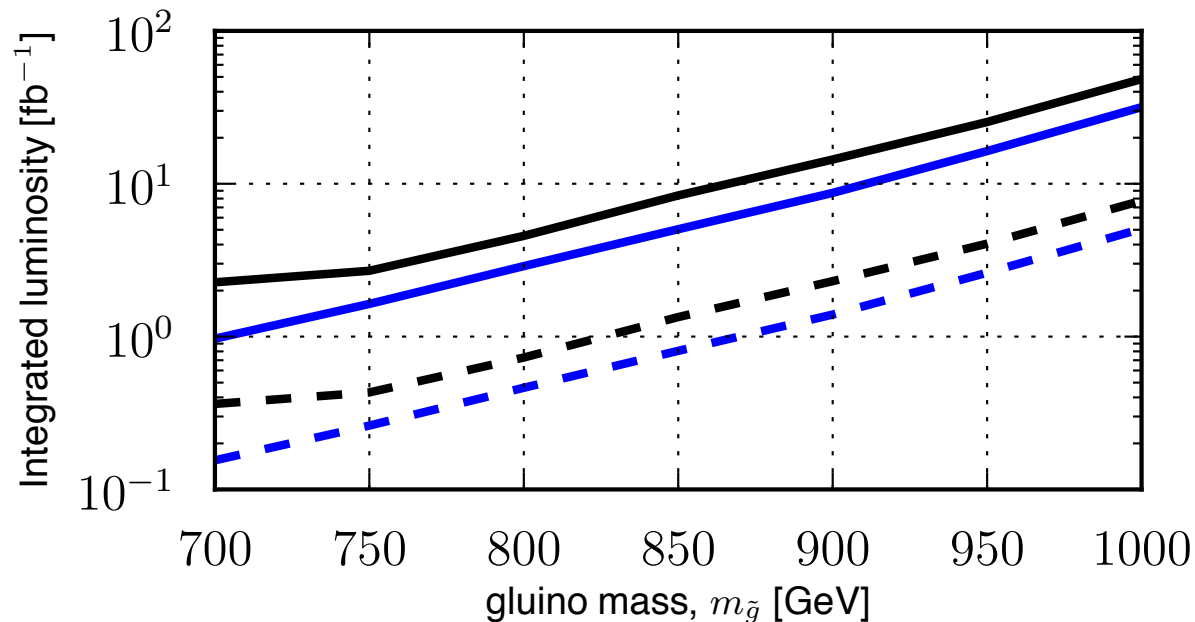
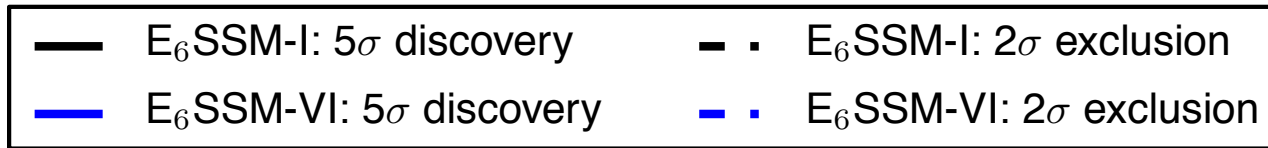


(c) $m_{\tilde{g}} = 900$ GeV



(d) $m_{\tilde{g}} = 1000$ GeV

Luminosity required for 5σ discovery and 2σ exclusion, $\sqrt{s} = 8\text{TeV}$ in 3 lepton channel



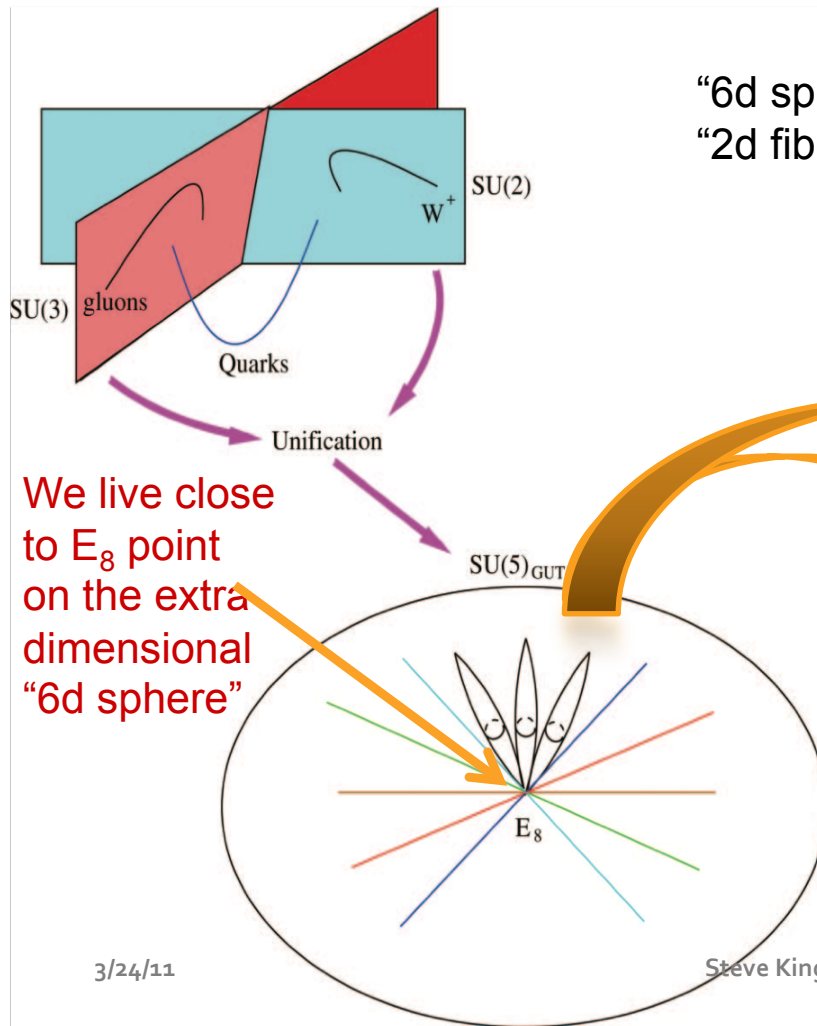
Summary of Part 2

- E_6 SSM is richer theory with many LHC signals
- Matter spectrum with 3 families of 27 dimensional particle reps and a Z'
- Higgs at 125 GeV possible in E_6 SSM
- Typical spectrum is heavy squarks but lighter gluino
- Gluino has longer decay chains with more jets and leptons and less missing transverse momentum
- E_6 SSM Gluino is harder to see in 6 jet channel
- But easier to see in 3 lepton channel
- We eagerly await the next LHC results!

Extra Slides

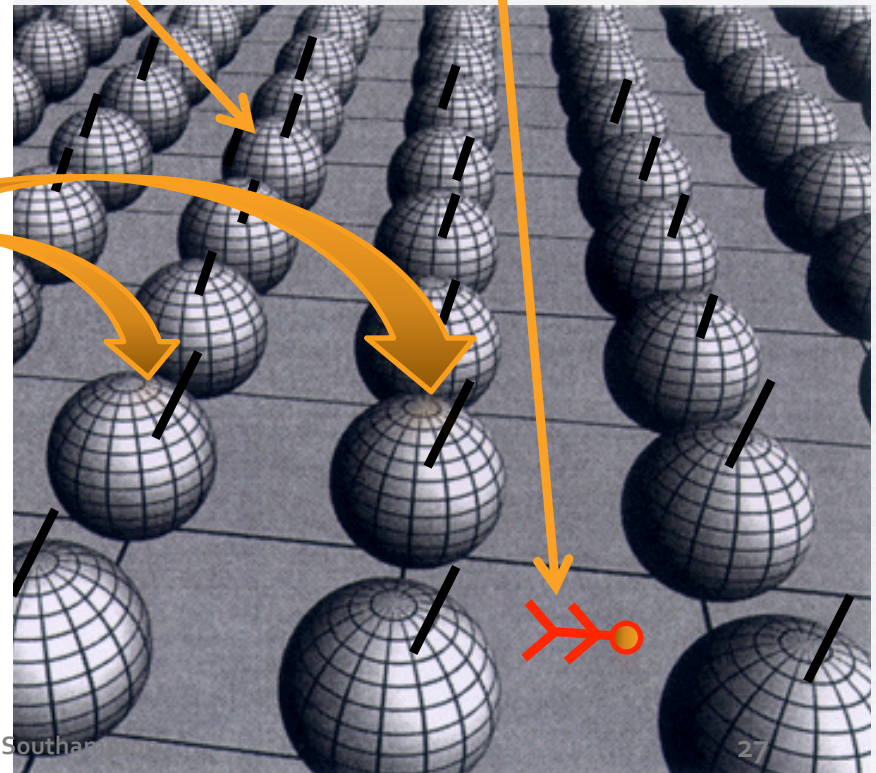
F-Theory GUTs: a 12d string theory

Heckman and Vafa



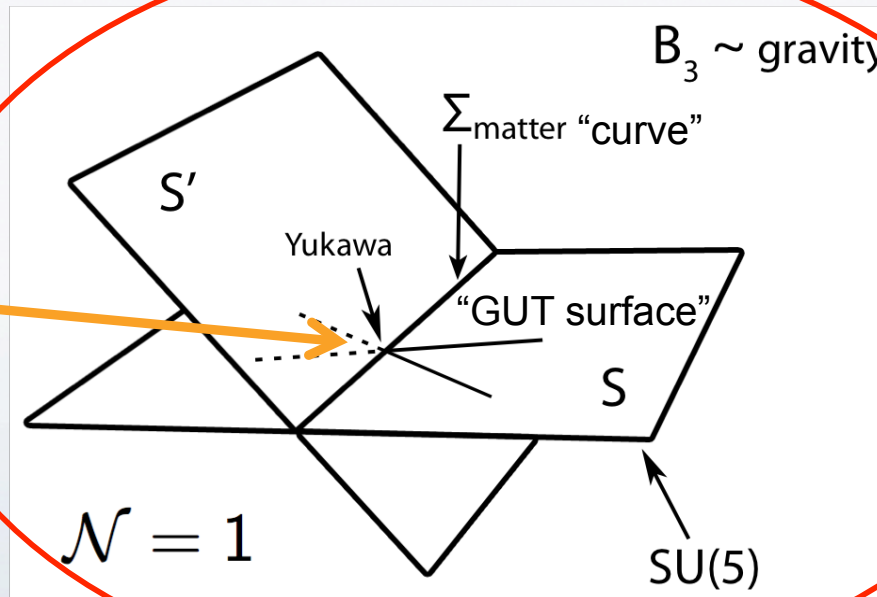
"6d spheres" with
"2d fibres"

"4d Flatlander"



The "6d sphere"

We live close to here



dim.	internal dim.	feature
10	$6 = \dim(B_3)$	gravity
8	$4 = \dim(S)$	gauge fields
6	$2 = \dim(S \cap S')$	matter
4	$0 = \dim(S \cap S' \cap S'')$	interactions

"gravity bulk"

"GUT surface S "

"matter curve Σ "

"Yukawa point"

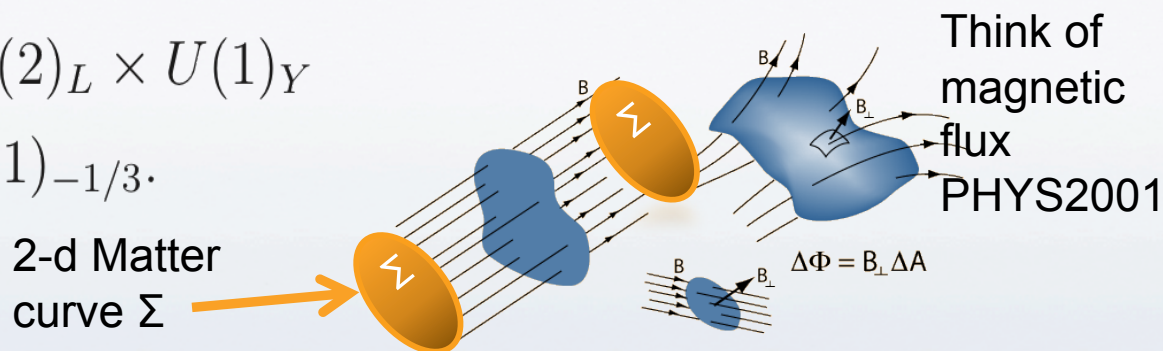
Figure 1: The structure of an F-theory GUT

GUT breaking is achieved not with Higgs but with Hypercharge Flux

$$SU(5) \supset SU(3)_C \times SU(2)_L \times U(1)_Y$$

$$5 \rightarrow (1, 2)_{1/2} + (3, 1)_{-1/3}.$$

2-d Matter
curve Σ



Index theorem gives number of chiral doublets and triplets (think of Gauss's law):

$$(1, 2)_{1/2} : n_L - n_R = 3 \int_{\Sigma} F_{U(1)_Y} + q \int_{\Sigma} F_{U(1)_{\perp}}$$

$$(3, 1)_{-1/3} : n_L - n_R = -2 \int_{\Sigma} F_{U(1)_Y} + q \int_{\Sigma} F_{U(1)_{\perp}}$$

Doublet-triplet Higgs splitting requires:

$$\text{Higgs: } \int_{\Sigma} F_{U(1)_Y} \neq 0$$

$$\text{Matter: } \int_{\Sigma} F_{U(1)_Y} = 0.$$

Typically predicts exotics

Callaghan, King, Leontaris, Ross

E6SSM from F-theory

E_6	$SO(10)$	$SU(5)$	Weight vector	N_Y	$M_{U(1)}$	SM particle content	Low energy spectrum
$27_{t'_1}$	16	$\bar{5}_3$	$t_1 + t_5$	1	4	$4d^c + 5L$	$3d^c + 3L$
$27_{t'_1}$	16	10_M	t_1	-1	4	$4Q + 5u^c + 3e^c$	$3Q + 3u^c + 3e^c$
$27_{t'_1}$	16	θ_{15}	$t_1 - t_5$	0	n_{15}	$3\nu^c$	-
$27_{t'_1}$	10	5_1	$-t_1 - t_3$	-1	3	$3D + 2H_u$	$3D + 2H_u$
$27_{t'_1}$	10	$\bar{5}_2$	$t_1 + t_4$	1	3	$3\bar{D} + 4H_d$	$3\bar{D} + 3H_d$
$27_{t'_1}$	1	θ_{14}	$t_1 - t_4$	0	n_{14}	θ_{14}	-
$27_{t'_3}$	16	$\bar{5}_5$	$t_3 + t_5$	-1	-1	$\bar{d}^c + 2\bar{L}$	-
$27_{t'_3}$	16	10_2	t_3	1	-1	$\bar{Q} + 2\bar{u}^c$	-
$27_{t'_3}$	16	θ_{35}	$t_3 - t_5$	0	n_{35}	-	-
$27_{t'_3}$	10	5_{H_u}	$-2t_1$	1	0	H_u	H_u
$27_{t'_3}$	10	$\bar{5}_4$	$t_3 + t_4$	-1	0	\bar{H}_d	-

F-theory model predicts incomplete multiplets
with matter content of 3 copies of 27s of E_6

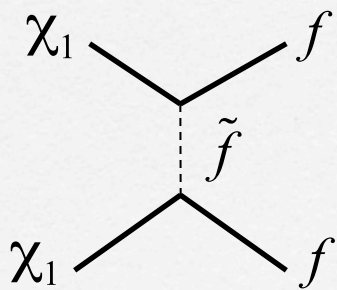
CMSSM Dark Matter

Neutralino mass matrix

$$\begin{pmatrix} \tilde{B} & \tilde{W}_3 & \tilde{H}_d & \tilde{H}_u \\ M_1 & & & \\ & M_2 & & \\ & & 0 & -\mu \\ & & -\mu & 0 \end{pmatrix}$$

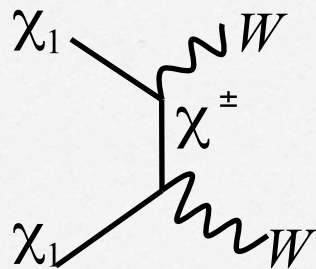
$$\chi_1 = N_1 \tilde{B} + N_2 \tilde{W} + N_3 \tilde{H}_d + N_4 \tilde{H}_u$$

$$\Omega_{DM} h^2 = C \frac{T_0^3}{M_P^2} \frac{1}{\langle \sigma v \rangle}$$



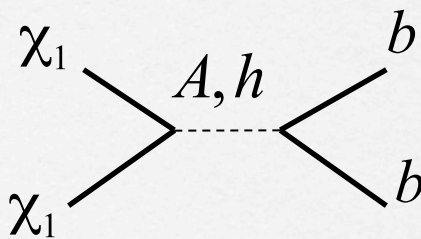
Bulk

$$m_{\tilde{f}} \approx m_{\chi_1}$$



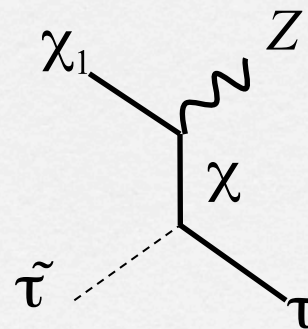
Focus

Higgsino LSP



Funnel

$$m_{A,h} \approx 2m_{\chi_1}$$



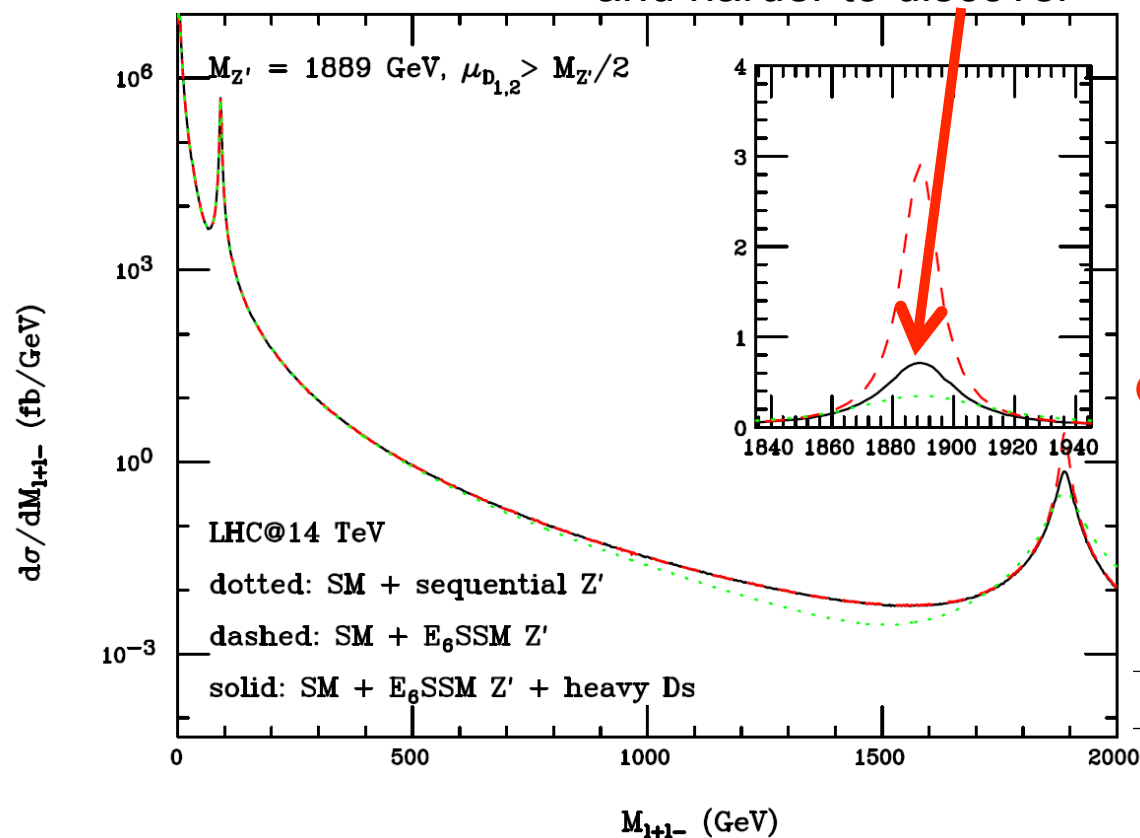
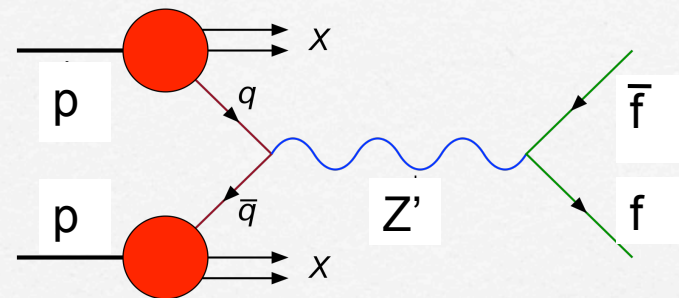
Co-annihilation

$$m_{\tilde{\tau}} \approx m_{\chi_1}$$

Athron, SFK, Miller, Moretti, Nevzorov

Z'_N

Latest ATLAS limit is
 $M_{Z'_N} > 1520 \text{ GeV}$
 but exotic decays
 makes Z' peak smaller
 and harder to discover



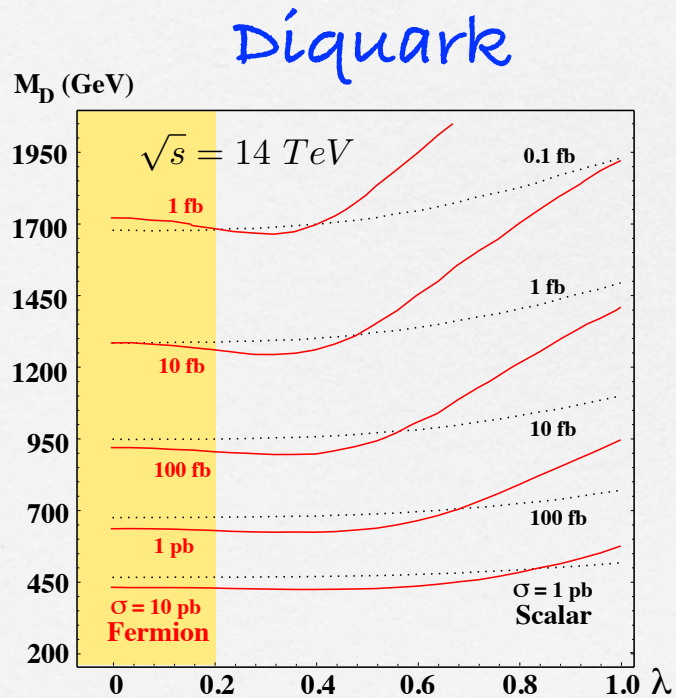
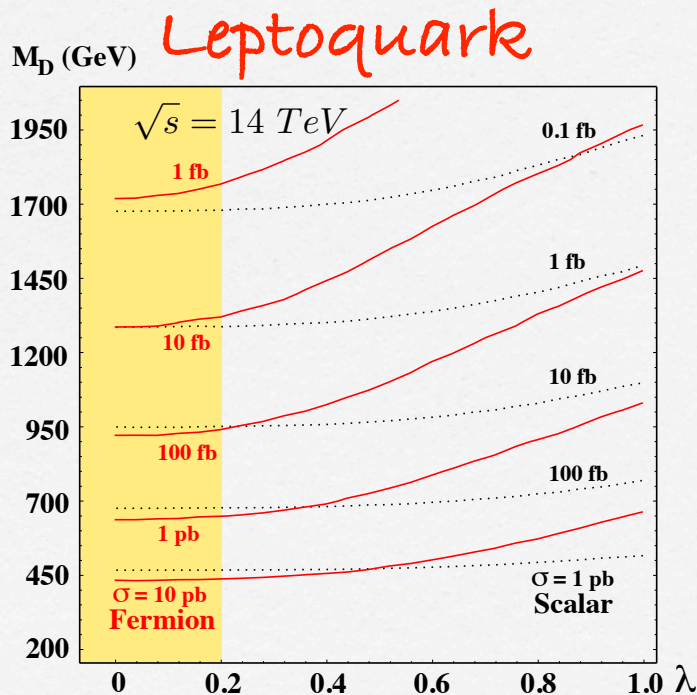
$\Gamma(Z'_N \rightarrow l^+l^-)$ ($l = e, \mu$ or τ)	0.77
$\Sigma_l \Gamma(Z'_N \rightarrow \nu_l \bar{\nu}_l)$ (all neutrinos)	1.64
$\Sigma_l \Gamma(Z'_N \rightarrow l^+l^-, \nu_l \bar{\nu}_l)$ (all leptons)	3.96
$\Sigma_q \Gamma(Z'_N \rightarrow q\bar{q})$ (all quarks)	10.08
$\Sigma_i \Gamma(Z'_N \rightarrow D_i \bar{D}_i)$ (exotic fermions)	0.00
$\Sigma_\alpha \Gamma(Z'_N \rightarrow \tilde{H}_\alpha \tilde{H}_\alpha)$ (inert Higgsinos)	5.19
$\Sigma_\alpha \Gamma(Z'_N \rightarrow \tilde{S}_\alpha \tilde{S}_\alpha)$ (singlinos)	7.63
$\Sigma_i \Gamma(Z'_N \rightarrow \tilde{D}_i \tilde{D}_i)$ (exotic scalars)	0.19
$\Sigma_f \Gamma(Z'_N \rightarrow \tilde{f} \tilde{f})$ (sfermions)	0.010
$\Sigma_\alpha \Gamma(Z'_N \rightarrow H_\alpha H_\alpha)$ (inert Higgses)	0.39
$\Sigma_j \Gamma(Z'_N \rightarrow \tilde{\chi}_j \tilde{\chi}_j)$ (gauginos)	7.92×10^{-5}
Γ_{tot} (all)	27.45

Exotic D-particles

Kang, Langacker, Nelson

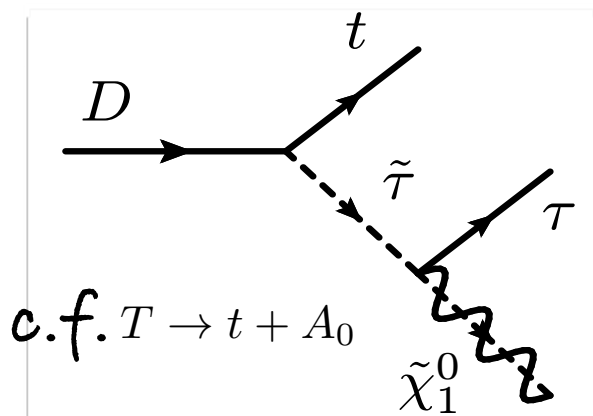
D-particles are **coloured** and may be pair produced at LHC

D-particles may be **Leptoquarks** $D \rightarrow LQ$ or **Diquarks** $D \rightarrow QQ$



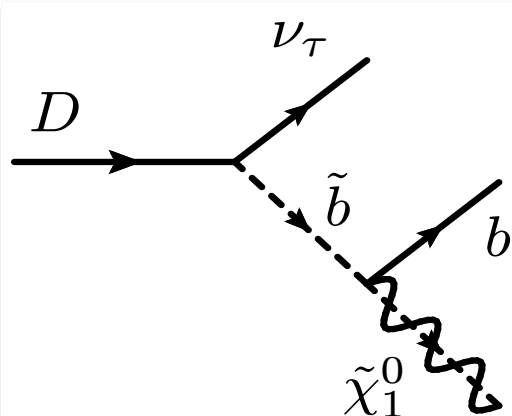
D-fermion decays

Leptoquark



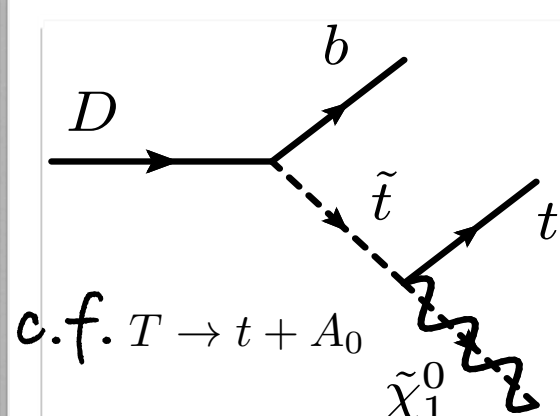
$$pp \rightarrow t\bar{t}\tau^+\tau^- + E_T^{miss} + X$$

Leptoquark



$$pp \rightarrow b\bar{b} + E_T^{miss} + X$$

Diquark



$$pp \rightarrow t\bar{t}b\bar{b} + E_T^{miss} + X$$

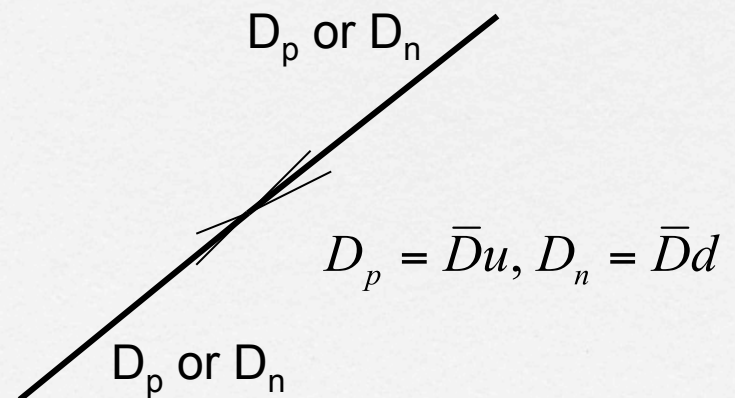
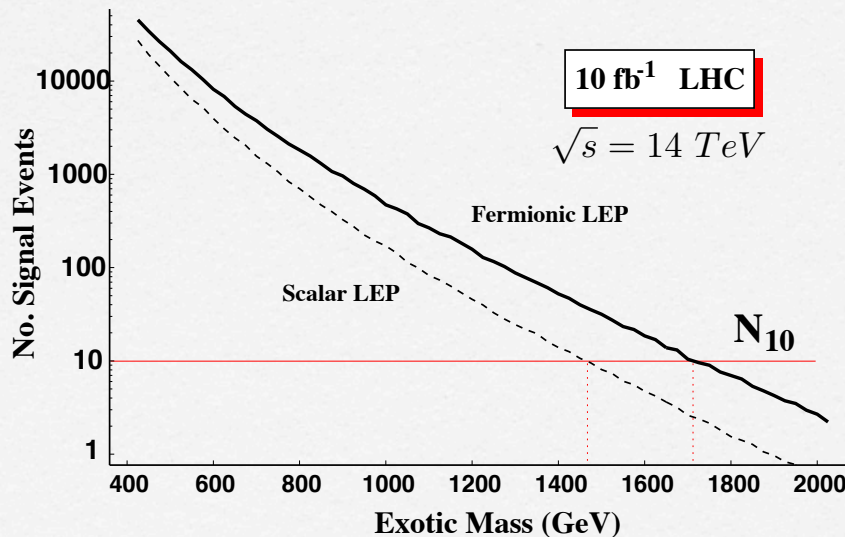
spectacular signals!

D-fermion as R-hadron

- Imposing B and L all couplings DFF forbidden
- D-particle are quasi-stable R-hadrons, decay via

dim5 : $D^c Q H_d S$, $D^c Q Q u^c$, $D^c Q L \nu^c$

punch through to muon chambers



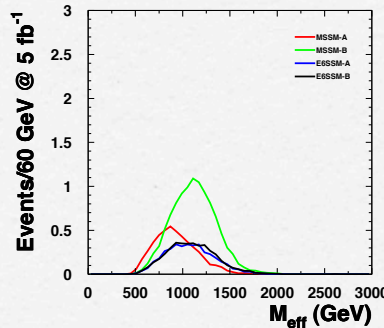
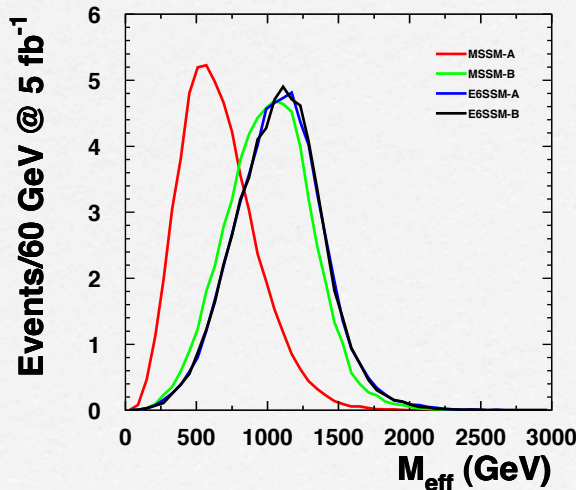
Belyaev, Hall, King,
Svantesson (preliminary)

M_{eff}

$$M_{\text{eff}} = p_T^{\text{miss}} + \sum_{\text{jets}} |p_T^{\text{jet}}|$$

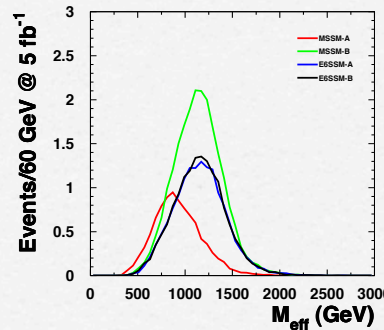
M_{eff} does not really help
to distinguish models

ATLAS style cuts



No.	CUT	MSSM-A		MSSM-B		E ₆ SSM-A		E ₆ SSM-B	
	limit	Eff.	Frac.	Eff.	Frac.	Eff.	Frac.	Eff.	Frac.
0	no cut	0.00	1.00	0.00	1.00	0.00	1.00	0.00	1.00
1	$p_T^{\text{miss}} > 130$	0.12	0.88	0.19	0.81	0.40	0.60	0.40	0.60
2	$p_T^{\text{jet1}} > 130$	0.42	0.51	0.04	0.77	0.03	0.58	0.03	0.59
3	$p_T^{\text{jet2}} > 40$	0.13	0.44	0.01	0.76	0.00	0.58	0.00	0.58
4	$p_T^{\text{jet3}} > 40$	0.36	0.28	0.11	0.68	0.04	0.56	0.04	0.56
5	$p_T^{\text{jet4}} > 40$	0.55	0.13	0.20	0.54	0.11	0.50	0.11	0.50
6	$\Delta\phi(p_T, \text{jet})_{\text{min}} > 0.4$	0.28	0.09	0.37	0.34	0.59	0.20	0.58	0.21
7	$p_T/M_{\text{eff}} > 0.25$	0.15	0.08	0.49	0.17	0.69	0.06	0.68	0.07

CMS style cuts



No.	CUT	MSSM-A		MSSM-B		E ₆ SSM-A		E ₆ SSM-B	
	limit	Eff.	Frac.	Eff.	Frac.	Eff.	Frac.	Eff.	Frac.
0	no cut	0.00	1.00	0.00	1.00	0.00	1.00	0.00	1.00
1	$H_T > 200$ GeV	0.58	0.42	0.34	0.66	0.47	0.53	0.47	0.53
2	$p_T^{\text{jet1}} > 50$ GeV	0.00	0.42	0.00	0.66	0.00	0.53	0.00	0.53
3	$p_T^{\text{jet2}} > 50$ GeV	0.13	0.37	0.02	0.64	0.01	0.52	0.01	0.53
4	$p_T^{\text{jet3}} > 50$ GeV	0.43	0.21	0.13	0.56	0.06	0.49	0.06	0.50
5	$\Delta\phi(p_T, \text{jet1}) > 0.5$	0.02	0.21	0.02	0.55	0.03	0.48	0.03	0.48
6	$\Delta\phi(p_T, \text{jet2}) > 0.5$	0.05	0.19	0.08	0.50	0.12	0.42	0.12	0.42
7	$\Delta\phi(p_T, \text{jet3}) > 0.3$	0.04	0.19	0.07	0.47	0.10	0.38	0.10	0.38
8	$\Delta R(\text{jet}, \text{lep})_{\text{min}} < 0.3$	0.18	0.15	0.24	0.36	0.37	0.24	0.36	0.25
9	$H_T > 800$ GeV	0.88	0.02	0.49	0.18	0.38	0.15	0.38	0.15

Two potential problems: rapid proton decay + FCNCs

- FCNC problem may be tamed by introducing a Z_2^H under which **third family Higgs and singlet** are **even** all else odd \rightarrow only allows Yukawa couplings involving **third family Higgs and singlet** H_u, H_d, S

- Z_2^H also forbids all DFF and hence forbids D decay (and p decay)
 $\rightarrow Z_2^H$ cannot be an exact symmetry!

How do we reconcile D decay with p decay?

In E_6 SSM can have extra discrete symmetries:

Z_2^L under which L are odd \rightarrow forbids DQL, allows DQQ \rightarrow exotic D are diquarks

Z_2^B with L & D odd \rightarrow forbids DQQ, allows DQL \rightarrow exotic D are leptoquarks

Or:-- small DFF couplings $\sim 10^{-12}$ will suppress p decay sufficiently while couplings $\sim 10^{-12}$ will allow D decay with lifetime < 0.1 s (nucleosynth) N.B. $\Gamma_D \propto g^2, \Gamma_p \propto g^4$ (Howl, SFK)