Precision Constraints on Higgs and Z couplings

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With Ulrich Haisch, Jure Zupan – JHEP 1311 (2013) 180 [arXiv:1310.1385] With Admir Grelio, Emmanuel Stamou, Patipan Uttayarat – JHEP 1502 (2015) 141 [arXiv:1408.0792] With Wolfgang Altmannshofer, Martin Schmaltz – arXiv:1503.04830

Introduction

The goal of Particle Physics

What is \mathcal{L} ?

- Current knowledge contained in the "Standard Model of Particle Physics"
- Good agreement with collider and precision experiments

(Selected) problems of the SM

- Dark Matter?
- Neutrino masses?
- Flavor structure? (14 of 19 parameters in the flavor sector!)
- Sakharov conditions:
 - B violation
 - C, CP violation
 - Thermal non-equilibrium
- More specific questions:
 - Are the gauge boson interactions as in the SM?
 - Are the Higgs boson interactions as in the SM?
 - Are there additional sources of CP violation?

Outline

- Anomalous *ttZ* couplings
- CP-violating Higgs couplings to top and bottom quarks
- What do we know about the electron Yukawa?

Indirect searches for new physics

- Strategy for the search for new physics:
 - Choose process that is suppressed in the SM
 - E.g., FCNC transition; one-loop + GIM
 - New particles can contribute via loops
 - General parameterisation by EFT
- Two steps:
 - Precise SM prediction
 - Comparison with experiment
- Complements direct searches for new physics ("high-p_T")

Example: Rare *B* and *K* decays

- Rare decays with theory uncertainty $\mathcal{O}(1\%)$:
- ${\sf BR}(B_s o \mu^+ \mu^-) = 3.65(23) imes 10^{-9}$ [Bobeth et al., arXiv:1311.0903]
- BR $(K^+ \to \pi^+ \nu \bar{\nu}) = 7.81(75)(29) \times 10^{-11}$ [Brod et al., arXiv:1009.0947]
- BR $(K_L o \pi^0 \nu \bar{\nu}) = 2.43(39)(6) imes 10^{-11}$ [Brod et al., arXiv:1009.0947]



• Look for new physics in $b \rightarrow s \ (s \rightarrow d)$ transistions

One more step

- What we have learned from LHC:
 - There is a "SM-like" Higgs particle
 - Other new particles are most likely very heavy $(M \gg v)$
- All SM particles are then light in comparison
- Construct all operators using SM fields ⇒ "SM-EFT" [See, e.g., Buchmüller et al. 1986, Grzadkowski et al. 2010]
- $SU(2) \times U(1)$ gauge invariance explicit

$$\mathcal{L}^{\mathsf{eff}} = \mathcal{L}^{\mathsf{SM}} + \mathcal{L}^{\mathsf{dim.6}} + \dots$$

- Higher orders suppressed by powers of v/M
- Explicit examples follow!

Anomalous $t\overline{t}Z$ Couplings

Anomale *ttZ*-Kopplungen

- Direct searches at LHC extremely difficult
- Unconventional example for the sensitivity of rare decays
 - (... and the application of SM-EFT)

Direct bounds on anomalous $t\bar{t}Z$ **couplings**



• *ttZ* production at NLO [Röntsch, Schulze, arXiv:1404.1005]

• pprox 20% - 30% deviation from SM still allowed even with 3000 fb $^{-1}$

Basic idea

- Can we constrain anomalous $t\bar{t}Z$ couplings by precision observables?
- Yes using mixing via electroweak loops



Assumption I: Operators in the UV

• At NP scale Λ , only the following operators have nonzero coefficients:

$$\begin{split} Q^{(3)}_{Hq} &\equiv (H^{\dagger} i \stackrel{\leftrightarrow}{D_{\mu}^{a}} H) (\bar{Q}_{L,3} \gamma^{\mu} \sigma^{a} Q_{L,3}) \,, \\ Q^{(1)}_{Hq} &\equiv (H^{\dagger} i \stackrel{\leftrightarrow}{D}_{\mu} H) (\bar{Q}_{L,3} \gamma^{\mu} Q_{L,3}) \,, \\ Q_{Hu} &\equiv (H^{\dagger} i \stackrel{\leftrightarrow}{D}_{\mu} H) (\bar{t}_{R} \gamma^{\mu} t_{R}) \,. \end{split}$$

- Here, $Q_{L,3}^T = (t_L, V_{ti} d_{L,i})$
- Only these operators induce tree-level ttZ couplings

Assumption II: LEP bounds

• After EWSB these operators induce

 $\mathcal{L}' = g'_R \, \bar{t}_R Z t_R + g'_L \, \bar{t}_L Z t_L + g''_L \, V^*_{3i} \, V_{3j} \, \bar{d}_{L,i} Z d_{L,j} + (k_L \, V_{3i} \, \bar{t}_L \, W^+ d_{L,i} + \text{h.c.})$

$$g_R' \propto C_{Hu}, \qquad g_L' \propto C_{Hq}^{(3)} - C_{Hq}^{(1)}, \qquad g_L'' \propto C_{Hq}^{(3)} + C_{Hq}^{(1)}, \qquad k_L \propto C_{Hq}^{(3)}$$

- LEP data on $Z \to b \bar{b} : ~g_L^{\prime\prime} \sim 10^{-3}$
- $C_{Hq}^{(3)}(\Lambda) + C_{Hq}^{(1)}(\Lambda) = 0$
- This scenario could be realized with vector-like quarks [del Aguila et al., hep-ph/0007316]

Assumption III: Only top Yukawa

- Only the top-quark Yukawa is nonvanishing
- Neglect other Yukawas in RGE
- Comment later on deviations from that assumption

A Comment on the Literature

- In [arxiv:1112.2674, arxiv:1301.7535, arxiv:1109.2357] indirect bounds on *qtZ*, *tbW* couplings have been derived using a similar approach
- They calculated the diagrams, with $\Lambda \sim M_W$:

$$\mathcal{A} = \frac{g^2}{16\pi^2} \Big(A + B \log \frac{\mu_W}{\Lambda} \Big)$$

• Note that the finite part A is renormalization-scheme dependent!



Operator Mixing

• Weak gauge boson and Higgs exchange induces mixing into [Jenkins et al., 2013; see also Brod et al. 2014]

•
$$Q^{(3)}_{\phi q,ii} \equiv (\phi^{\dagger} i \stackrel{\leftrightarrow}{D^{a}_{\mu}} \phi) (\bar{Q}_{L,i} \gamma^{\mu} \sigma^{a} Q_{L,i}) \rightarrow b \bar{b} Z$$

•
$$Q^{(1)}_{\phi q,ii} \equiv (\phi^{\dagger} i \stackrel{\leftrightarrow}{D}_{\mu} \phi) (\bar{Q}_{L,i} \gamma^{\mu} Q_{L,i}) \rightarrow b \bar{b} Z$$

•
$$Q_{lq,33jj}^{(3)} \equiv (\bar{Q}_{L,3}\gamma_{\mu}\sigma^{*}Q_{L,3})(\bar{L}_{L,j}\gamma^{\mu}\sigma^{*}L_{L,j}) \rightarrow \text{rare K} / B$$

•
$$Q_{lq,33jj}^{(1)} \equiv (\bar{Q}_{L,3}\gamma_{\mu}Q_{L,3})(\bar{L}_{L,j}\gamma^{\mu}L_{L,j}) \rightarrow \text{rare K} / B$$

•
$$Q_{\phi D} \equiv \left| \phi^{\dagger} D_{\mu} \phi \right|^2
ightarrow \mathsf{T}$$
 parameter



Analytic result

$$\begin{split} \delta g_L^b &= -\frac{e}{2s_w c_w} \frac{\alpha}{4\pi} \bigg\{ V_{33}^* V_{33} \bigg[\frac{x_t}{2s_w^2} \Big(8 C_{\phi q, 33}^{(1)} - C_{\phi u} \Big) + \frac{17 c_w^2 + s_w^2}{3s_w^2 c_w^2} C_{\phi q, 33}^{(1)} \bigg] \\ &+ \bigg[\frac{2s_w^2 - 18c_w^2}{9s_w^2 c_w^2} C_{\phi q, 33}^{(1)} + \frac{4}{9c_w^2} C_{\phi u} \bigg] \bigg\} \frac{v^2}{\Lambda^2} \log \frac{\mu_W}{\Lambda} \end{split}$$

$$\delta T = -\left[rac{1}{3\pi c_w^2} \left(C_{\phi q,33}^{(1)} + 2C_{\phi u,33}
ight) + rac{3x_t}{2\pi s_w^2} \left(C_{\phi q,33}^{(1)} - C_{\phi u,33}
ight)
ight]rac{v^2}{\Lambda^2}\lograc{\mu_W}{\Lambda}$$

$$\delta \boldsymbol{Y}^{\mathrm{NP}} = \delta \boldsymbol{X}^{\mathrm{NP}} = \frac{x_t}{8} \left(C_{\phi u} - \frac{12 + 8x_t}{x_t} C_{\phi q, 33}^{(1)} \right) \frac{v^2}{\Lambda^2} \log \frac{\mu_W}{\Lambda}$$

•

Numerical result



$$\begin{array}{ll} T & 0.08 \pm 0.07 & \mbox{[Ciuchini et al., arxiv:1306.4644]} \\ \delta g^b_L & 0.0016 \pm 0.0015 & \mbox{[Ciuchini et al., arxiv:1306.4644]} \\ Br(B_s \rightarrow \mu^+ \mu^-) \mbox{[CMS]} & (3.0^{+1.0}_{-0.9}) \times 10^{-9} & \mbox{[CMS, arxiv:1307.5025]} \\ Br(B_s \rightarrow \mu^+ \mu^-) \mbox{[LHCb]} & (2.9^{+1.1}_{-1.0}) \times 10^{-9} & \mbox{[LHCb, arxiv:1307.5024]} \\ Br(K^+ \rightarrow \pi^+ \nu \bar{\nu}) & (1.73^{+1.05}_{-1.05}) \times 10^{-10} & \mbox{[E949, arxiv:0808.2459]} \end{array}$$

How general are our results?

- A generic NP model can generate FCNC transitions in the up sector
- Consider models with large enhancement of the bottom Yukawa (2HDM...)
- Assume MFV e.g., now, have $\bar{Q}_L(Y_u Y_u^{\dagger} + Y_d Y_d^{\dagger})Q_L$
- Large bottom Yukawa induces flavor off-diagonal operators in the up sector
- They will contribute to FCNC top decays and $D-ar{D}$ mixing
- These effects are suppressed by powers of $\lambda \equiv |V_{us}| pprox 0.22$
- $D-ar{D}$ mixing is suppressed by $\lambda^{10}pprox 10^{-7}$
- FCNC top-quark decays:

$$\mathsf{Br}(t \to cZ) \simeq \frac{\lambda^4 v^4}{\Lambda^4} \left[\left(C_{\phi q, 33}^{(3)} - C_{\phi q, 33}^{(1)} \right)^2 + C_{\phi u, 33}^2 \right]$$

• $\mathsf{Br}(t o cZ) < 0.05\%$ [CMS, arxiv:1312.4194] \Rightarrow not competitive

t-channel single top production

- $\sqrt{\sigma(t)/\sigma_{SM}(t)} = 0.97(10)$ [ATLAS-CONF-2014-007]
- $\sqrt{\sigma(t)/\sigma_{\rm SM}(t)} = 0.998(41)$ [CMS, arxiv:1403.7366]
- *t*-channel single top production constrains $v^2 C_{Ha}^{(3)}/\Lambda^2 = -0.006 \pm 0.038$ [arxiv:1408.0792]



$t\bar{t}Z$: Summary and outlook

- Strong constraints from rare *B* and *K* decays
- Bounds on other interaction are possible: e.g. *WWZ* [Bobeth, Haisch, arxiv:1503.04829]
- Use other decays that get a Z-penguin contribution: e.g. $B \to K^* \ell \ell$
- More generally: Global SU(2)-invariant analysis of flavor and electroweak precision data

[See also Alonso, Grinstein, Camalich, arXiv:1407.7044]

CP-violating Higgs Couplings

CP-violating Higgs couplings

- The discovery of the Higgs particle opened a new window for the search for new physics!
 - CP Violation in Higgs-fermion couplings?
- Difficult to measure at LHC
- Elektric dipole moments (EDM) of electron and neutron very sensitive to CP violation
 - SM background many orders of magnitude below experimental limits

How can we change the Higgs couplings?



- Mass and Yukawa term become independent
- Relative complexe phase \rightarrow CP violation
- More generally, we write:

$$\mathcal{L}'_{Y} = -\frac{y_{f}}{\sqrt{2}} (\kappa_{f} + i\tilde{\kappa}_{f}) \overline{f}_{L} f_{R} h + \text{h.c.}$$

CP-violating $t\bar{t}H$ Couplings

Electron EDM



- "Barr-Zee" diagrams induce EDM [Weinberg 1989, Barr & Zee 1990]
- $|d_e/e| < 8.7 imes 10^{-29} \, {
 m cm}$ (90% CL) [ACME 2013]
- $\Rightarrow |\tilde{\kappa}_t| < 0.01$
- Constraint on $\tilde{\kappa}_t$ vanishes if the Higgs does not couple to the electron

Neutron EDM – The Weinberg Operator



- Barr-Zee diagrams similar as in electron case
- Contribution of the Weinberg Operator: Higgs couples only to top quark
- Get constraint even if couplings to light quarks vanish

Neutron EDM – RG running





• Operator mixing: $\mu \frac{d}{d\mu} C(\mu) = \gamma^T C(\mu)$

$$\gamma = \frac{\alpha_s}{4\pi} \begin{pmatrix} \frac{32}{3} & 0 & 0\\ \frac{32}{3} & \frac{28}{3} & 0\\ 0 & -6 & 14 + \frac{4N_f}{3} \end{pmatrix}$$

- Hadronic matrix element are evaluated at $\mu_H \sim 1 \; {
 m GeV}$
- QCD sum rules (large $\mathcal{O}(1)$ uncertainties!)

[Pospelov, Ritz, hep-ph/0504231]

Neutron EDM – Constraints

$$\begin{aligned} \frac{d_n}{e} &= \left\{ (1.0 \pm 0.5) \left[-5.3 \,\kappa_q \tilde{\kappa}_t + 5.1 \cdot 10^{-2} \,\kappa_t \tilde{\kappa}_t \right] \right. \\ &+ \left(22 \pm 10 \right) 1.8 \cdot 10^{-2} \,\kappa_t \tilde{\kappa}_t \right\} \cdot 10^{-25} \,\mathrm{cm} \,. \end{aligned}$$

• terms $\propto \kappa_t \tilde{\kappa}_t$ subdominant, but proportional only to top Yukawa

- $|d_n/e| < 2.9 imes 10^{-26} \, {
 m cm} \, \left(90\% \, {
 m CL}
 ight)$ [Baker et al., 2006]
 - $| ilde{\kappa}_t| \lesssim 0.1 \mathsf{SM}$ couplings to light quarks
 - $| ilde\kappa_t| \lesssim 0.7$ only coupling to top quark

Constraints from Higgs production and decay



$$\frac{\sigma(gg \to h)}{\sigma(gg \to h)_{\rm SM}} = \kappa_t^2 + 2.6 \,\tilde{\kappa}_t^2 + 0.11 \,\kappa_t \,(\kappa_t - 1)$$



Combined bounds – SM couplings to light fermions



- Assume SM couplings to electrons and light quarks
- Future projection for 3000fb⁻¹ @ high-luminosity LHC [J. Olsen, talk at Snowmass Energy Frontier workshop]
- Factor 90 (300) improvement on electron (neutron) EDM [Fundamental Physics at the Energy Frontier, arXiv:1205.2671]

Combined bounds – only top Yukawa

- Set couplings to electron and light quarks to zero
- Weinberg operator will lead to strong constraints in future scenario



CP-violating $b\bar{b}H$ Couplings

Constraints from EDMs

- Contributions to EDMs suppressed by small Yukawas; still get meaningful constraints in future scenario
- For electron EDM, simply replace charges and couplings
- For neutron EDM, extra scale $m_b \ll M_h$ important

$$\begin{split} d_q(\mu_W) &\simeq -4 e \, Q_q \, N_c \, Q_b^2 \, \frac{\alpha}{(4\pi)^3} \sqrt{2} G_F \, m_q \, \kappa_q \tilde{\kappa}_b \, \frac{m_b^2}{M_h^2} \left(\log^2 \frac{m_b^2}{M_h^2} + \frac{\pi^2}{3} \right) \,, \\ \tilde{d}_q(\mu_W) &\simeq -2 \, \frac{\alpha_s}{(4\pi)^3} \sqrt{2} G_F \, m_q \, \kappa_q \tilde{\kappa}_b \, \frac{m_b^2}{M_h^2} \left(\log^2 \frac{m_b^2}{M_h^2} + \frac{\pi^2}{3} \right) \,, \\ w(\mu_W) &\simeq -g_s \, \frac{\alpha_s}{(4\pi)^3} \, \sqrt{2} G_F \, \kappa_b \tilde{\kappa}_b \, \frac{m_b^2}{M_h^2} \left(\log \frac{m_b^2}{M_h^2} + \frac{3}{2} \right) \,. \end{split}$$



RGE analysis of the *b*-quark contribution to EDMs

- $\bullet~\approx$ 3 scale uncertainty in CEDM Wilson coefficient
- Two-step matching at M_h and m_b :









• $\mathcal{O}_1^q = \bar{q}q\,\bar{b}i\gamma_5 b$

Mixing into

$$\bullet \ \mathcal{O}_4^q = \bar{q}\sigma_{\mu\nu} T^a q \, \bar{b} i \sigma^{\mu\nu} \gamma_5 T^a b$$



Matching onto

•
$$\mathcal{O}_6^q = -\frac{i}{2} \frac{m_b}{g_s} \bar{q} \sigma^{\mu\nu} T^a \gamma_5 q G^a_{\mu\nu}$$

RG Running

• Above $\mu_b \sim m_b$ have 10 operators which mix:

CEDM operator



•
$$C_{\tilde{d}_q}(\mu_b) = \frac{432}{2773 \, \eta_5^{9/23}} + \frac{0.07501}{\eta_5^{1.414}} + 9.921 \cdot 10^{-4} \, \eta_5^{0.7184} - \frac{0.2670}{\eta_5^{0.0315}} + \frac{0.03516}{\eta_5^{0.06417}}$$

•
$$\eta_5 \equiv \alpha_s(\mu_W)/\alpha_s(\mu_b)$$

• Expand:
$$\mathcal{C}_{\tilde{d}_q}(\mu_b) \simeq \left(\frac{\alpha_s}{4\pi}\right)^2 \frac{\gamma_{14}^{(0)}\gamma_{48}^{(0)}}{8} \log^2 \frac{m_b^2}{M_b^2} + \mathcal{O}(\alpha_s^3)$$

EDM operator



•
$$C_{d_q}(\mu_b) = -4 \frac{lpha \, \alpha_s}{(4\pi)^2} \, Q_q \log^2 \frac{m_b^2}{M_b^2} + \left(\frac{lpha_s}{4\pi}\right)^3 \frac{\gamma_{14}^{(0)} \gamma_{48}^{(0)} \gamma_{67}^{(0)}}{48} \, \log^3 \frac{m_b^2}{M_b^2} + \mathcal{O}(\alpha_s^4)$$

• QCD mixing term dominates by a factor of $\approx 4.5(-9.0)!$

Weinberg operator



•
$$\mathcal{C}_w(\mu_b) = \left(\frac{\alpha_s}{4\pi}\right)^2 \frac{\gamma_{5,11}^{(1)}}{2} \log \frac{m_b^2}{M_b^2} + \mathcal{O}(\alpha_s^3)$$

• Linear log requires two-loop running

Neutron EDM at the hadronic scale

• Below $\mu_b \sim m_b$, analysis is analogous to case of top quarks

$$\frac{d_n}{e} = \left\{ (1.0 \pm 0.5) \left[-18.1 \,\tilde{\kappa}_b + 0.15 \,\kappa_b \tilde{\kappa}_b \right] + (22 \pm 10) \, 0.48 \,\kappa_b \tilde{\kappa}_b \right\} \cdot 10^{-27} \,\mathrm{cm} \,.$$

Collider constraints

- Modifications of $gg \rightarrow h$, $h \rightarrow \gamma \gamma$ due to $\kappa_b \neq 1$, $\tilde{\kappa}_b \neq 0$ are subleading
- $\bullet\,\Rightarrow\,$ Main effect: modifications of branching ratios / total decay rate

$$Br(h \to b\bar{b}) = \frac{(\kappa_b^2 + \tilde{\kappa}_b^2)Br(h \to b\bar{b})_{SM}}{1 + (\kappa_b^2 + \tilde{\kappa}_b^2 - 1)Br(h \to b\bar{b})_{SM}}$$
$$Br(h \to X) = \frac{Br(h \to X)_{SM}}{1 + (\kappa_b^2 + \tilde{\kappa}_b^2 - 1)Br(h \to b\bar{b})_{SM}}$$

- Use naive averages of ATLAS / CMS signal strengths $\hat{\mu}_X$ for $X = b\bar{b}$, $\tau^+\tau^-$, $\gamma\gamma$, WW, ZZ
- $\hat{\mu}_X = Br(h \to X)/Br(h \to X)_{SM}$ up to subleading corrections of production cross section

Combined bounds: SM couplings to light fermions



- Assume SM couplings to electron and light quarks
- Future projection for 3000fb⁻¹ @ high-luminosity LHC
- Factor 90 (300) improvement on electron (neutron) EDM

Combined bounds: only bottom Yukawa

- Set couplings to electron and light quarks to zero
- Contribution of Weinberg operator will lead to competitive constraints in the future scenario



What do we know about the electron Yukawa?

It's small and real! (In the SM.)

$$y_e^{\rm SM}=\sqrt{2}rac{m_e}{v}\simeq 2.9 imes 10^{-6}$$

Indirect bounds: Imaginary part – electron EDM



- ... + 117 more two-loop diagrams
- Complete analytic result [Altmannshofer, Brod, Schmaltz, arxiv:1503.04830]
- $|d_e/e| < 8.7 imes 10^{-29} \, {
 m cm} \, \left(90\% \, {
 m CL}
 ight)$ [acme 2013]
- ... leads to $| ilde\kappa_e| < 0.017$

Indirect bounds: Real part – $(g - 2)_e$

- Usually, the measurement of $a_e \equiv (g-2)_e/2$ is used to extract lpha
- Using independent α measurement, can make a prediction for a_e [cf. Giudice et al., arXiv:1208.6583]
- With
 - $\alpha = 1/137.035999037(91)$ [Bouchendira et al., arXiv:1012.3627]
 - $a_e = 11596521807.3(2.8) \times 10^{-13}$ [Gabrielse et al. 2011]
- ... we find $|\kappa_e| \lesssim 3000$
- Bound expected to improve by a factor of 10 in the next few years

Indirect bounds: Real part – rare *B* decays





• SM prediction [Bobeth et al., arXiv:1311.0903]

- ${\sf Br}(B_s o e^+e^-)_{\sf SM} = (8.54 \pm 0.55) imes 10^{-14}$
- ${\sf Br}(B_d o e^+e^-)_{\sf SM} = (2.48 \pm 0.21) imes 10^{-15}$
- Current bounds [CDF 2009]
 - $Br(B_s \to e^+e^-) < 2.8 \times 10^{-7}$
 - ${\sf Br}(B_d o e^+e^-) < 8.3 imes 10^{-8}$
- ... leads to $|\kappa_e| = \mathcal{O}(10^6)$

Collider bounds: LEP II



- LEP / LEP II did not run on the Higgs resonance
- ullet They collected $\sim 500/\text{pb}$ per experiment between $\sqrt{s}=189\ldots 207$ GeV
- A bound could be obtained via "radiative return" to the Z pole
- Requiring $N_{\rm r.r.}/\sqrt{N_{\rm bkg.}} = 1$ we find $\sqrt{\kappa_e^2 + \tilde{\kappa}_e^2} \lesssim 2000$
- A dataset at $\sqrt{s} = 130$ GeV leads a similar bound

Collider bounds: CMS

$$\mathsf{Br}(h \to e^+ e^-) = \frac{\left(\kappa_e^2 + \tilde{\kappa}_e^2\right)\mathsf{Br}(h \to e^+ e^-)_{\mathsf{SM}}}{1 + \left(\kappa_e^2 + \tilde{\kappa}_e^2 - 1\right)\mathsf{Br}(h \to e^+ e^-)_{\mathsf{SM}}}$$

• CMS limit Br
$$(h
ightarrow e^+e^-)$$
 < 0.0019 [CMS, arxiv:1410.6679] leads to $\sqrt{\kappa_e^2 + \tilde{\kappa}_e^2}$ < 611

- Estimated future sensitivities at hadron colliders:
 - 14 TeV LHC with 3000/fb: $\sqrt{\kappa_{\rm e}^2+\tilde{\kappa}_{\rm e}^2}\sim 150$
 - 100 TeV collider with 3000/fb: $\sqrt{\kappa_e^2 + \tilde{\kappa}_e^2} \sim 75$

Collider bounds: Future e^+e^- machines



- A future e^+e^- machine...
 - $\bullet\,$ collecting 100 fb^{-1} on the Higgs resonance
 - assuming 0.05% beam-energy spread
- \bullet \ldots would be sensitive to $\sqrt{\kappa_e^2+\tilde{\kappa}_e^2}\sim 15$

Summary

- Precision observables can often yield constraints that are compatible or stronger than bounds from direct searches
- EMDs yield strong constraints on CP-violating Yukawa couplings
- FCNC down-sector transitions yield strong constraints on up-sector diagonal couplings
- The electron Yukawa will likely never be measured precisely