

Whither[†] SUSY?

G. Ross, Sussex, October 2012



†

whither *Archaic or poetic*
adv

1. to what place?
2. to what end or purpose?

conj

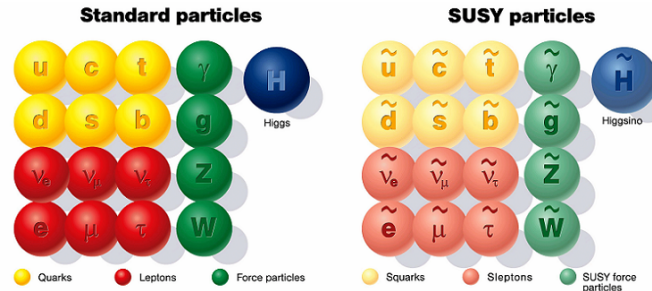
to whatever place, purpose, etc.

[Old English *hwider*, *hwæder*; related to Gothic *hvadrē*; modern English form influenced by HITHER]

Low energy

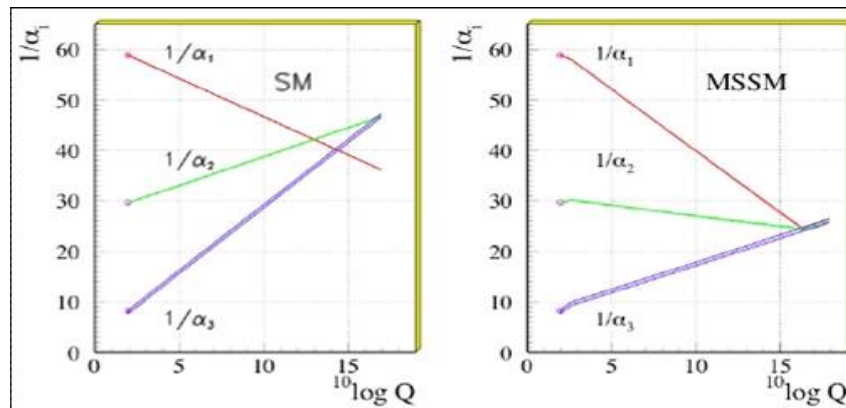
SUSY - to what end or purpose?

^



Unification:

SU(5), SO(10),...



✓

The hierarchy problem:

$$M_{Higgs}, M_{W,Z} \ll M_{Planck}, M_{GUT}, \dots$$

✓

(?)

ATLAS

ATLAS SUSY Searches* - 95% CL Lower Limits (Status: ICHEP 2012)

Search Category	Search Description	Lower Limit	Notes
Inclusive searches	MSUGRA/CMSSM : 0 lep + j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-033]	1.40 TeV $\tilde{q} = \tilde{g}$ mass
	MSUGRA/CMSSM : 1 lep + j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-041]	1.20 TeV $\tilde{q} = \tilde{g}$ mass
	MSUGRA/CMSSM : 0 lep + multijets + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [1206.1760]	840 GeV \tilde{g} mass (large m_0)
	Pheno model : 0 lep + j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-033]	1.38 TeV \tilde{q} mass ($m(\tilde{g}) < 2 \text{ TeV}$, light $\tilde{\chi}_1^0$)
	Pheno model : 0 lep + j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-033]	940 GeV \tilde{g} mass ($m(\tilde{g}) < 2 \text{ TeV}$, light $\tilde{\chi}_1^0$)
	Gluino med. $\tilde{\chi}^\pm (\tilde{g} \rightarrow q\tilde{q}\tilde{\chi}^\pm)$: 1 lep + j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-041]	900 GeV \tilde{g} mass ($m(\tilde{\chi}_1^\pm) < 200 \text{ GeV}$, $m(\tilde{\chi}^\pm) = \frac{1}{2}(m(\tilde{\chi}^0) + m(\tilde{g}))$)
	GMSB : 2 lep OSSF + $E_{T,miss}$	$L=1.0 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2011-156]	810 GeV \tilde{g} mass ($\tan\beta < 35$)
	GMSB : 1- τ + j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1204.3852]	920 GeV \tilde{g} mass ($\tan\beta > 20$)
	GMSB : 2- τ + j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1203.6580]	990 GeV \tilde{g} mass
	GGM : $\gamma\gamma$ + $E_{T,miss}$	$L=4.8 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-072]	1.07 TeV \tilde{g} mass
3rd gen. squarks gluino mediated	$\tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$ (virtual \tilde{b}) : 0 lep + 1/2 b-j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1203.6193]	900 GeV \tilde{g} mass
	$\tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$ (virtual \tilde{b}) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-058]	1.02 TeV \tilde{g} mass
	$\tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$ (real \tilde{b}) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-058]	1.00 TeV \tilde{g} mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (virtual \tilde{t}) : 1 lep + 1/2 b-j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1203.6193]	710 GeV \tilde{g} mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (virtual \tilde{t}) : 2 lep (SS) + j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1203.5763]	650 GeV \tilde{g} mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (virtual \tilde{t}) : 0 lep + multi-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [1206.1760]	870 GeV \tilde{g} mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (virtual \tilde{t}) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-058]	940 GeV \tilde{g} mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (real \tilde{t}) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-058]	820 GeV \tilde{g} mass
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (real \tilde{t}) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1112.3832]	390 GeV \tilde{b} mass ($m(\tilde{\chi}_1^0) = 0 \text{ GeV}$)
	$\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$ (real \tilde{t}) : 0 lep + 3 b-j's + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-059]	135 GeV \tilde{t} mass ($m(\tilde{\chi}_1^0) = 45 \text{ GeV}$)
3rd gen. squarks direct production	$\tilde{t}\tilde{t}$ (very light), $\tilde{t} \rightarrow b\tilde{\chi}_1^\pm$: 2 lep + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-070]	120-173 GeV \tilde{t} mass ($m(\tilde{\chi}_1^0) = 45 \text{ GeV}$)
	$\tilde{t}\tilde{t}$ (light), $\tilde{t} \rightarrow b\tilde{\chi}_1^\pm$: 1/2 lep + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-074]	380-465 GeV \tilde{t} mass ($m(\tilde{\chi}_1^0) = 0$)
	$\tilde{t}\tilde{t}$ (heavy), $\tilde{t} \rightarrow t\tilde{\chi}_1^0$: 0 lep + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-073]	230-440 GeV \tilde{t} mass ($m(\tilde{\chi}_1^0) = 0$)
	$\tilde{t}\tilde{t}$ (heavy), $\tilde{t} \rightarrow t\tilde{\chi}_1^0$: 1 lep + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-071]	298-305 GeV \tilde{t} mass ($m(\tilde{\chi}_1^0) = 0$)
	$\tilde{t}\tilde{t}$ (heavy), $\tilde{t} \rightarrow t\tilde{\chi}_1^0$: 2 lep + b-jet + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1204.6736]	310 GeV \tilde{t} mass ($115 < m(\tilde{\chi}_1^0) < 230 \text{ GeV}$)
	$\tilde{t}\tilde{t}$ (GMSB) : $Z(\rightarrow ll)$ + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-076]	93-180 GeV \tilde{t} mass ($m(\tilde{\chi}_1^0) = 0$)
	$\tilde{t}\tilde{t}$ (GMSB) : $Z(\rightarrow ll)$ + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-076]	120-330 GeV \tilde{t} mass
	$\tilde{t}\tilde{t}$ (GMSB) : $Z(\rightarrow ll)$ + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-077]	118 GeV $\tilde{\chi}_1^\pm$ mass
	$\tilde{t}\tilde{t}$ (GMSB) : $Z(\rightarrow ll)$ + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	118 GeV $\tilde{\chi}_1^\pm$ mass
	$\tilde{t}\tilde{t}$ (GMSB) : $Z(\rightarrow ll)$ + b-jet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	118 GeV $\tilde{\chi}_1^\pm$ mass
EW direct	$\tilde{\chi}_1^\pm \tilde{\chi}_1^\pm \rightarrow l\tilde{l}(\tilde{\nu}) \rightarrow l\nu\tilde{\chi}_1^0$: 2 lep + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-076]	120-330 GeV $\tilde{\chi}_1^\pm$ mass
	$\tilde{\chi}_1^\pm \tilde{\chi}_1^\pm \rightarrow l\nu(\tilde{\nu}) \rightarrow l\nu\tilde{\chi}_1^0$: 2 lep + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-076]	120-330 GeV $\tilde{\chi}_1^\pm$ mass
	$\tilde{\chi}_1^\pm \tilde{\chi}_1^\pm \rightarrow 3l(l\nu\nu) + \nu + 2\tilde{\chi}_1^0$: 3 lep + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-077]	118 GeV $\tilde{\chi}_1^\pm$ mass
	AMS \tilde{b} : long-lived $\tilde{\chi}_1^\pm$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [CONF-2012-034]	118 GeV $\tilde{\chi}_1^\pm$ mass
Long-lived particles	Stable \tilde{g} R-hadrons : Full detector	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	118 GeV $\tilde{\chi}_1^\pm$ mass
	Stable \tilde{b} R-hadrons : Full detector	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	118 GeV $\tilde{\chi}_1^\pm$ mass
	Stable \tilde{t} R-hadrons : Full detector	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	118 GeV $\tilde{\chi}_1^\pm$ mass
	Metastable \tilde{g} R-hadrons : Pixel det. only	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	118 GeV $\tilde{\chi}_1^\pm$ mass
	GMSB : stable $\tilde{\tau}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-075]	310 GeV $\tilde{\tau}$ mass ($5 < \tan\beta < 10$)
RPV	RPV : high-mass $e\mu$	$L=1.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [1109.3089]	1.32 TeV $\tilde{\nu}_\tau$ mass ($\lambda_{311}^2=0.10, \lambda_{312}^2=0.05$)
	Bilinear RPV : 1 lep + j's + $E_{T,miss}$	$L=1.0 \text{ fb}^{-1}, 7 \text{ TeV}$ [1109.6606]	760 GeV $\tilde{q} = \tilde{g}$ mass ($c\tau_{LSP} < 15 \text{ mm}$)
	BC1 RPV : 4 lep + $E_{T,miss}$	$L=2.1 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-035]	1.7 TeV \tilde{g} mass
Other	Hypercolour scalar gluons : 4 jets, $m_g = m_{kl}$	$L=34 \text{ pb}^{-1}, 7 \text{ TeV}$ [1110.2693]	100-185 GeV scalar mass (not excluded, $m_g = 140 \pm 3 \text{ GeV}$)
	Spin dep. WIMP interaction : monojet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-084]	709 GeV M^* scalar ($m_\chi < 100 \text{ GeV}$, vector D5, Dirac χ)
	Spin indep. WIMP interaction : monojet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}, 7 \text{ TeV}$ [ATLAS-CONF-2012-084]	548 GeV M^* scalar ($m_\chi < 100 \text{ GeV}$, tensor D9, Dirac χ)

$$\int L dt = (0.03 - 4.8) \text{ fb}^{-1}$$

$\sqrt{s} = 7 \text{ TeV}$

ATLAS Preliminary

Limit 1 TeV strong interacting particles

Limit 300-400 GeV stop particles

And limits on WEAK INTERACTIONS

Mass scale [TeV]

*Only a selection of the available searches

SUSY - to what place?

Little hierarchy problem \Rightarrow definite SUSY structure ^{breaking}
^

MSSM: 105 +(19) Parameters

$$M_Z^2 = \sum_{\tilde{q}, \tilde{l}} a_i \tilde{m}_i^2 + \sum_{\tilde{g}, \tilde{W}, \tilde{B}} \tilde{M}_i^2 + \dots$$

$$m_{\tilde{q}} > 0.6 - 1 \text{TeV} \Rightarrow \Delta > a \frac{\tilde{m}^2}{M_Z^2} \sim 100$$

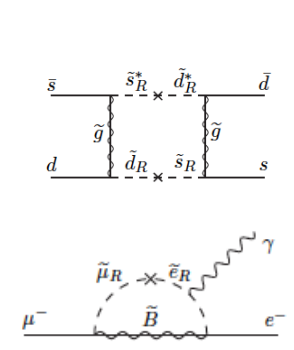
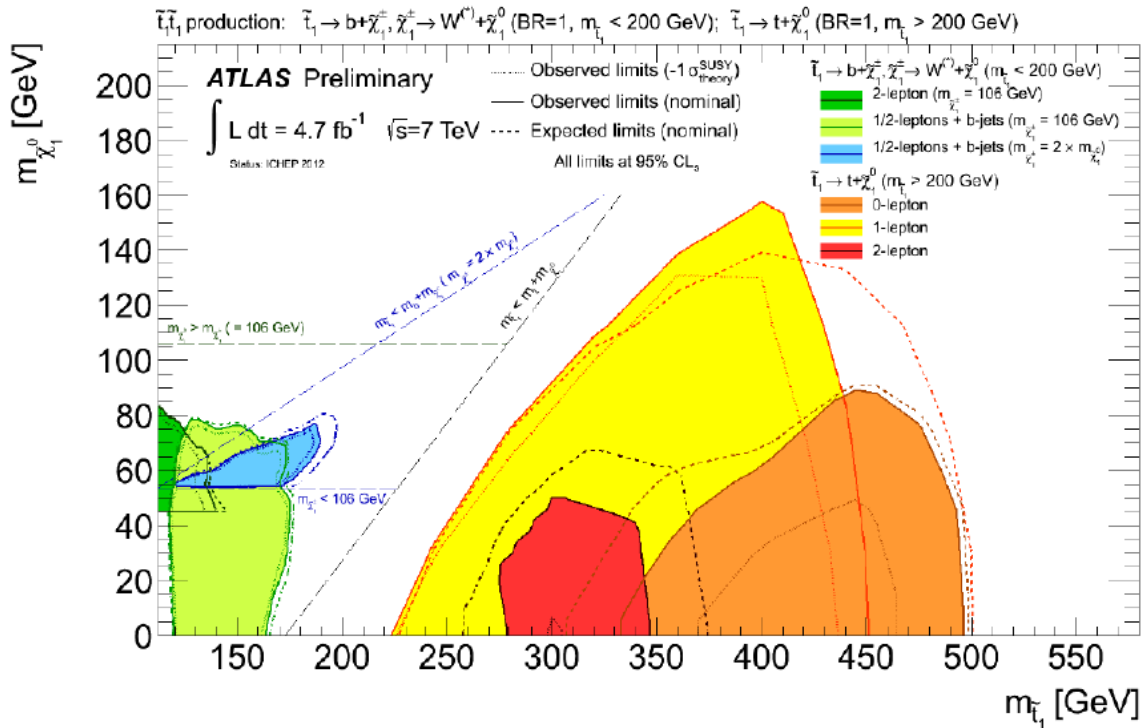
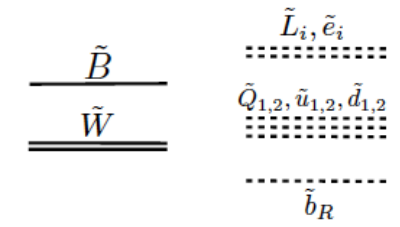
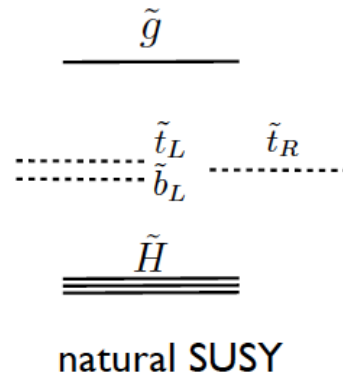
\Rightarrow Correlations between SUSY breaking parameters
and/or additional low-scale states

An exception: "Natural" SUSY

light stop $m_{\tilde{t},LHC} > 250 \text{ GeV}$

FCNC: 1,2 sgenerations heavy

Hierarchy problem: 3rd sgeneration light

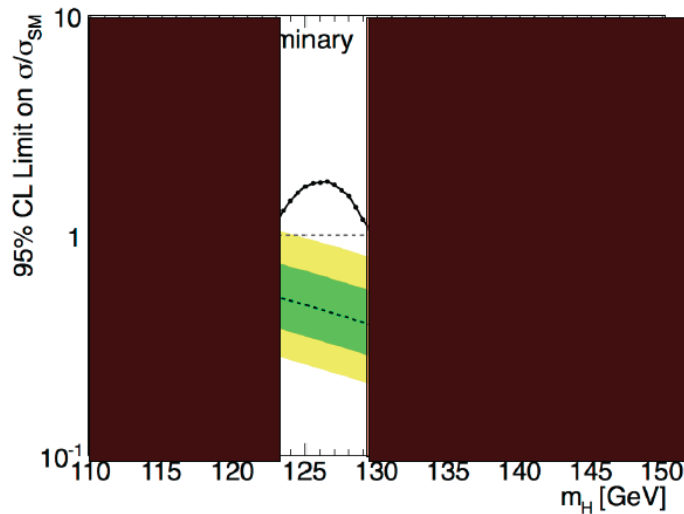


The Higgs mass in SUSY ?

$$M_S^2 = m_{q_3} m_{U_3} \geq (500 \text{ GeV})^2$$

$$M_{h^0}^2 = M_Z^2 \cos^2 2\beta + \frac{3M_t^2 h_t^2}{4\pi^2} \left(\ln\left(\frac{M_S^2}{M_t^2}\right) + \delta_t \right) + \dots \approx 125 \text{ GeV (LHC)}$$

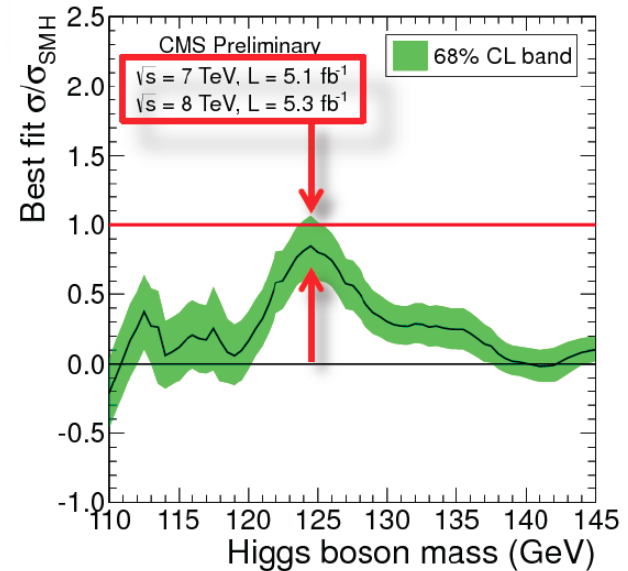
Atlas



Excluded at 95% CL

110-122.7 129-557 GeV

CMS



SUSY - to what place?

Little hierarchy problem \Rightarrow definite SUSY structure ^{breaking}
^

MSSM: 105 +(19) Parameters

$$M_Z^2 = \sum_{\tilde{q}, \tilde{l}} a_i \tilde{m}_i^2 + \sum_{\tilde{g}, \tilde{W}, \tilde{B}} \tilde{M}_i^2 + \dots$$

$$m_{\tilde{q}} > 0.6 - 1 \text{TeV} \Rightarrow \Delta > a \frac{\tilde{m}^2}{M_Z^2} \sim 100$$

\Rightarrow Correlations between SUSY breaking parameters and/or additional low-scale states

Fine Tuning measure:

$$\Delta(a_i) = \left| \frac{a_i}{M_Z} \frac{\partial M_Z}{\partial a_i} \right|,$$

$$\Delta_{\max} = \text{Max}_{a_i} \Delta(a_i)$$

Ellis, Enquist, Nanopoulos, Zwirner

Barbieri, Giudice

Fine Tuning measure:

$$\Delta(\gamma_i) = \left| \frac{\gamma_i}{M_Z} \frac{\partial M_Z}{\partial \gamma_i} \right|,$$

$$\Delta_{\max} = \text{Max}_{a_i} \Delta(\gamma_i)$$

Ellis, Enquist, Nanopoulos, Zwirner

Barbieri, Giudice

Likelihood:

$$L(\text{data} | \gamma_i^0) = \frac{1}{\Delta_q} L(\text{data} | \gamma_i; v_0, \beta, \tilde{y}_t(\beta), \tilde{y}_b(\beta)) \Big|_{\beta = \beta_0(\gamma_i); \gamma_i = \gamma_i^0} \delta\left(v - \left(\frac{m^2}{\lambda}\right)^{1/2}\right)$$

$$\chi^2(\gamma_i) = -2 \ln(L) = \chi_{old}^2(\gamma_i) + 2 \ln \Delta_q$$

Ghilencea, Ross

$$\Delta_q = \left(\sum_i \Delta_{\gamma_i}^2 \right)^{1/2}$$

$$\Delta_q = 100, \quad \delta\chi^2 / d.o.f. \sim 1$$

$$\Delta_q = 1000, \quad \delta\chi^2 / d.o.f. \sim 1.5$$

$$\chi^2 / d.o.f. = 2(2.5), \quad P = 3(0.6)\%$$

- The CMSSM

$$\mu_0, m_0, m_{1/2}, A_0, B_0$$



assume correlation between SUSY breaking parameters

● The CMSSM

$$\mu_0, m_0, m_{1/2}, A_0, B_0$$

$$V = m_1^2 |H_1|^2 + m_2^2 |H_2|^2 - (m_3^2 H_1 \cdot H_2 + h.c.) \\ + \frac{1}{2} \lambda_1 |H_1|^4 + \frac{1}{2} \lambda_2 |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1 \cdot H_2|^2 \\ + \left[\frac{1}{2} \lambda_5 (H_1 \cdot H_2)^2 + \lambda_6 |H_1|^2 (H_1 \cdot H_2) + \lambda_7 |H_2|^2 (H_1 \cdot H_2) + h.c. \right]$$

Minimisation conditions:

$$\underline{v^2 = -m^2/\lambda}, \quad 2\lambda \frac{\partial m^2}{\partial \beta} = m^2 \frac{\partial \lambda}{\partial \beta}$$

$$m^2 = m_1^2 \cos^2 \beta + m_2^2 \sin^2 \beta - m_3^2 \sin 2\beta$$

$$\lambda = \frac{\lambda_1}{2} \cos^4 \beta + \frac{\lambda_2}{2} \sin^4 \beta + \frac{\lambda_{345}}{4} \sin^2 2\beta + \sin 2\beta (\lambda_6 \cos^2 \beta + \lambda_7 \sin^2 \beta)$$

$$\Delta \equiv \max \left| \Delta_p \right|_{p=\{\mu_0^2, m_0^2, m_{1/2}^2, A_0^2, B_0^2\}}, \quad \Delta_p \equiv \frac{\partial \ln v^2}{\partial \ln p}$$

Couplings and masses evaluated to two loop (leading log) order

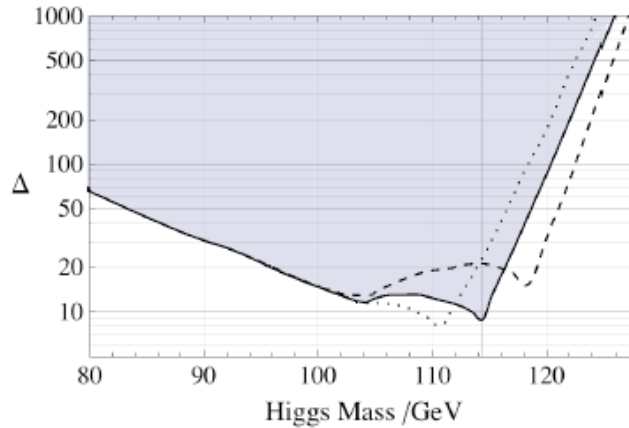
...enhanced sensitivity due to small tree-level $\lambda = \frac{1}{8} (g_1^2 + g_2^2) \cos^2 2\beta$

Cassel, Ghilencea, GGR
c.f. earlier work : Dimopoulos, Giudice
Chankowski, Ellis, Olechowski, Pokorski

● The CMSSM

$$\mu_0, m_0, m_{1/2}, A_0, B_0$$

Constraints



SUSY particle masses

$$3.20 < 10^4 \text{ Br}(b \rightarrow s\gamma) < 3.84$$

$$\text{Br}(b \rightarrow \mu\mu) < 1.8 \times 10^{-8}$$

$$\delta a_\mu < 292 \times 10^{-11}$$

$$-0.0007 < \delta\rho < 0.0012$$

Radiative EW breaking

Relic density unrestricted

$$\Delta \equiv \max |\Delta_p|_{p=\{\mu_0^2, m_0^2, m_{1/2}^2, A_0^2, B_0^2\}}, \quad \Delta_p \equiv \frac{\partial \ln v^2}{\partial \ln p}$$

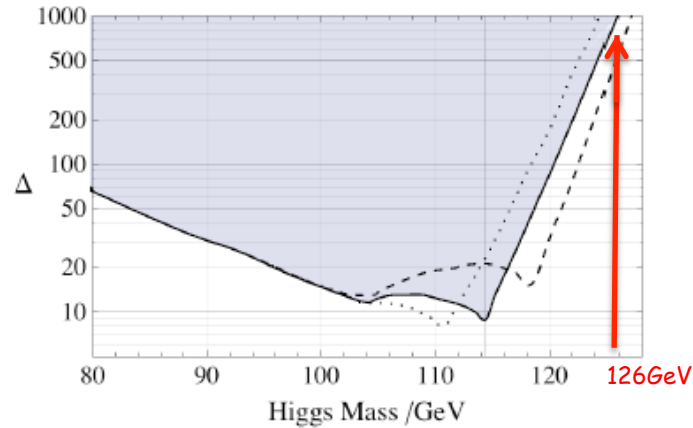
$$\Delta_{Min} = 9, \quad m_h = 114 \pm 2 \text{ GeV}$$

(No Higgs bound applied)

● The CMSSM

$$\mu_0, m_0, m_{1/2}, A_0, B_0$$

...BUT



Constraints

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● The CMSSM

Constraints

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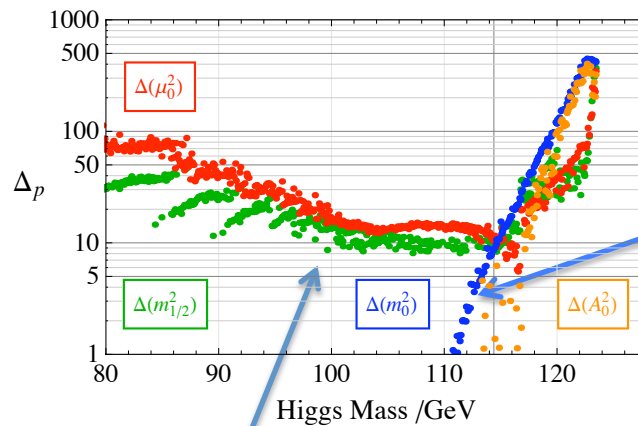
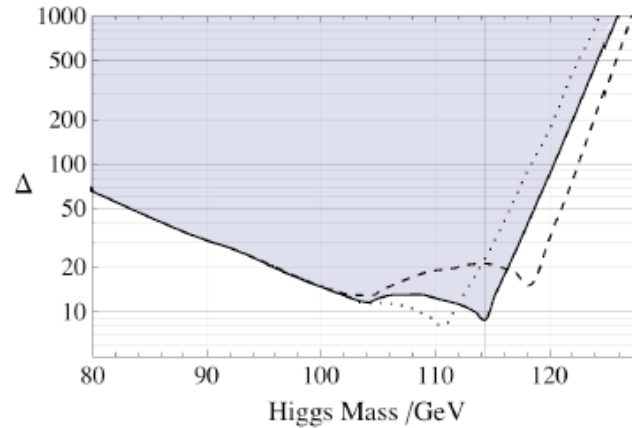
$$\text{Br}(b \rightarrow \mu\mu) < 1.8 \times 10^{-8}$$

$$\delta a_\mu < 292 \times 10^{-11}$$

$$-0.0007 < \delta\rho < 0.0012$$

Radiative EW breaking

Relic density unrestricted



Limit of focus point

λ increase with m_H

$$v^2 = -\frac{m^2}{\lambda}$$

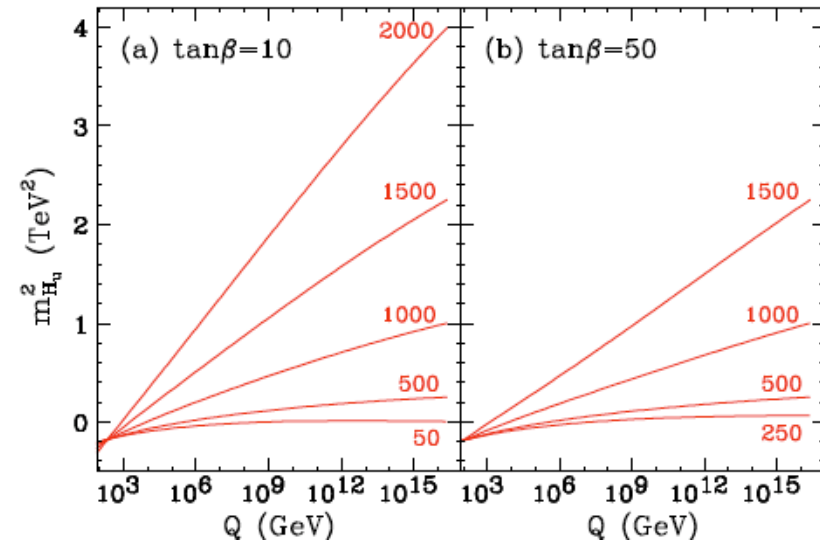
Focus Point

$$2|y_t|^2 (m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2|a_t|^2$$

$$16\pi^2 \frac{d}{dt} m_{H_u}^2 = 3X_t - 6g_2^2 |M_2|^2 - \frac{6}{5}g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{Q_3}^2 = X_t + X_b - \frac{32}{3}g_3^2 |M_3|^2 - 6g_2^2 |M_2|^2 - \frac{2}{15}g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{u_3}^2 = 2X_t - \frac{32}{3}g_3^2 |M_3|^2 - \frac{32}{15}g_1^2 |M_1|^2$$



$$m_{H_u}^2(Q^2) = m_{H_u}^2(M_P^2) + \frac{1}{2} \left(m_{H_u}^2(M_P^2) + m_{Q_3}^2(M_P^2) + m_{u_3}^2(M_P^2) \right) \left[\left(\frac{Q^2}{M_P^2} \right)^{\frac{3y_t^2}{4\pi^2}} - 1 \right]$$

m_0^2

$3m_0^2$

$\approx -\frac{2}{3}, Q^2 \approx M_Z^2$

“Focus point”: $m_{H_u}^2(0) = m_{Q_3}^2(0) = m_{u_3}^2(0) \equiv m^2$

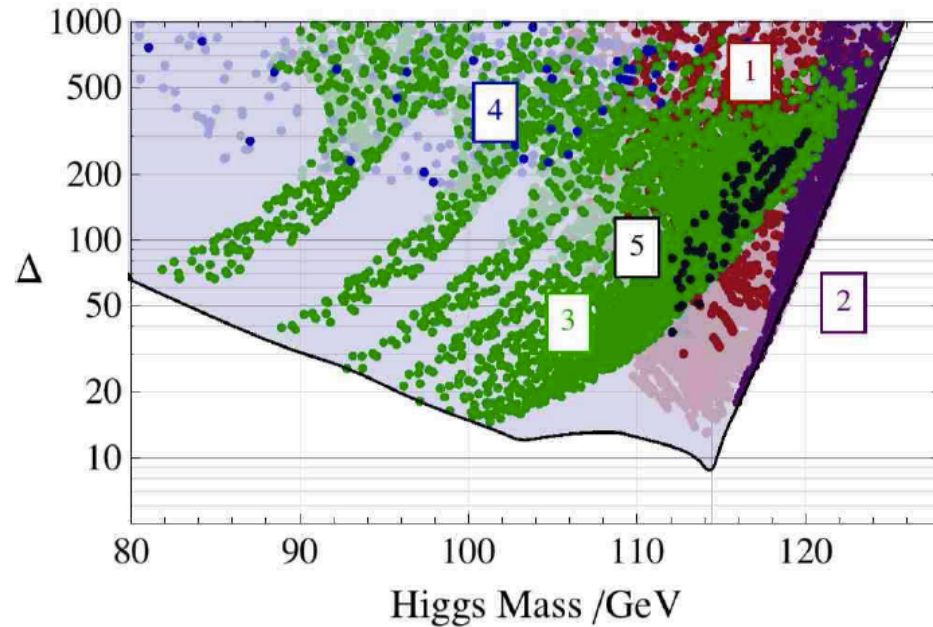
$$m_{H_u}^2(t_0) = a_0 m^2 + \dots, a_0 \leq 0.1$$

i.e. $m_{Q_3}^2, m_{u_3}^2 \gg M_Z^2$ possible

Natural choice

Feng, Matchev, Moroi
 Chan, Chattopadhyay, Nath
 Barbieri, Giudice
 Feng, Sanford

Dark Matter structure



Relic density restricted

- 1 h^0 resonant annihilation
- 2 \tilde{h} t-channel exchange
- 3 $\tilde{\tau}$ co-annihilation
- 4 \tilde{t} co-annihilation
- 5 A^0 / H^0 resonant annihilation

Within 3σ WMAP:

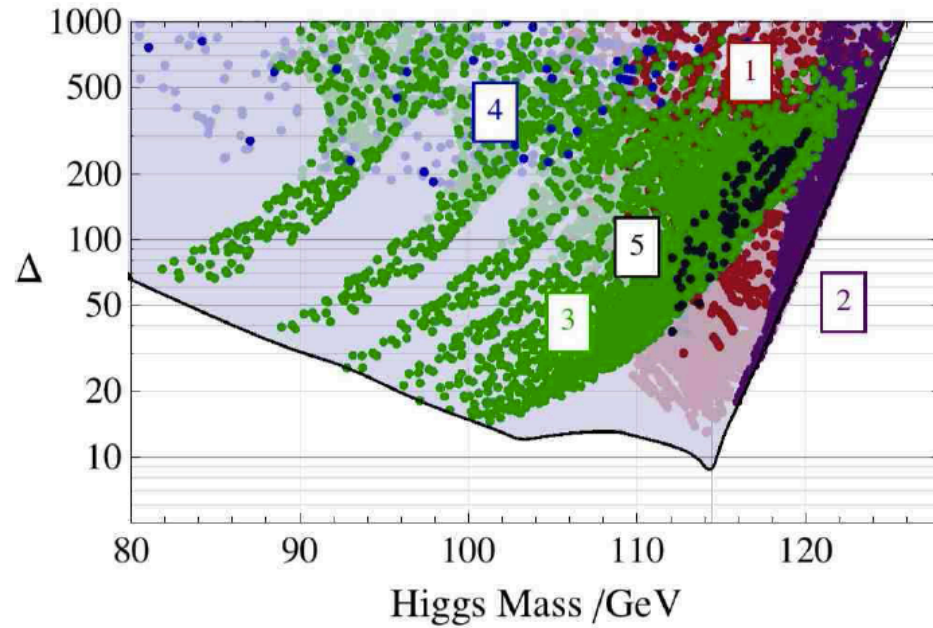
$$\Delta_{Min} = 15, \quad m_h = 114.7 \pm 2 GeV$$

< 3σ WMAP:

$$\Delta_{Min} = 18, \quad m_h = 115.9 \pm 2 GeV$$

Cassel, Ghilencea, GGR

Relic density restricted



- 1 h^0 resonant annihilation
- 2 \tilde{h} t-channel exchange
- 3 $\tilde{\tau}$ co-annihilation
- 4 \tilde{t} co-annihilation
- 5 A^0 / H^0 resonant annihilation

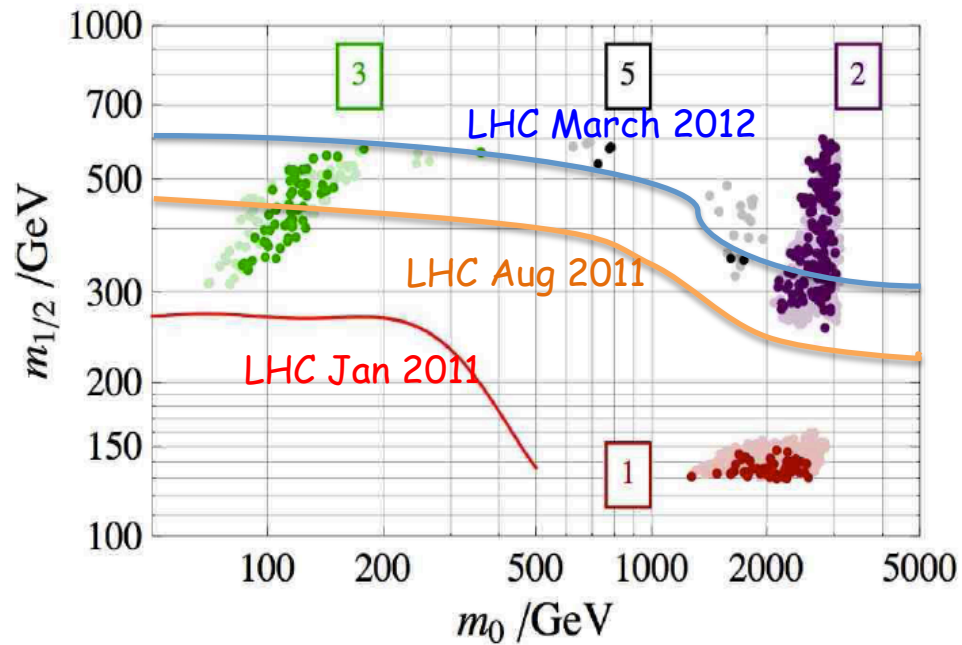
Within 3σ WMAP:

$$\Delta_{Min} = 15, \quad m_h = 114.7 \pm 2 GeV$$

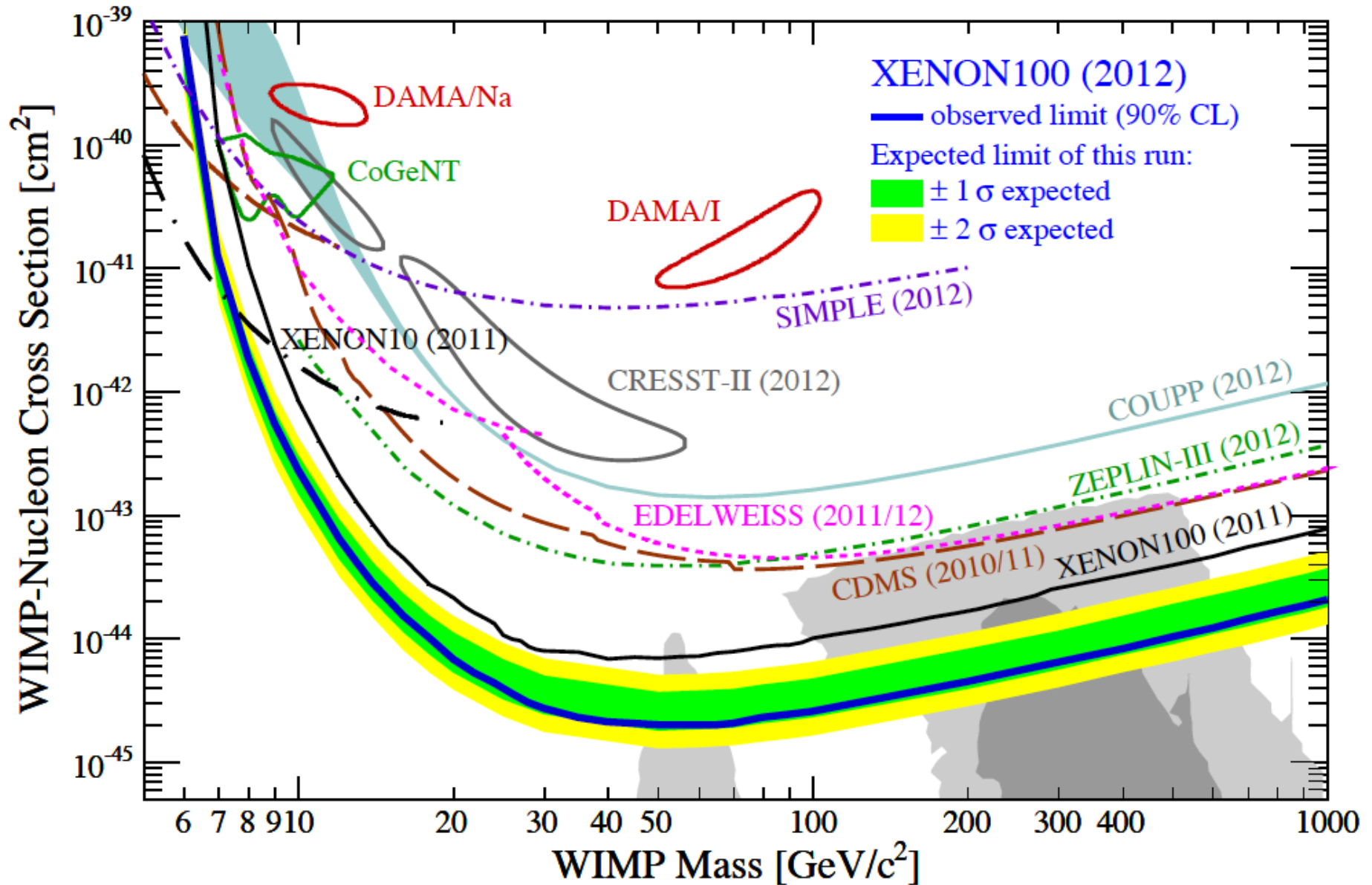
$< 3\sigma$ WMAP:

$$\Delta_{Min} = 18, \quad m_h = 115.9 \pm 2 GeV$$

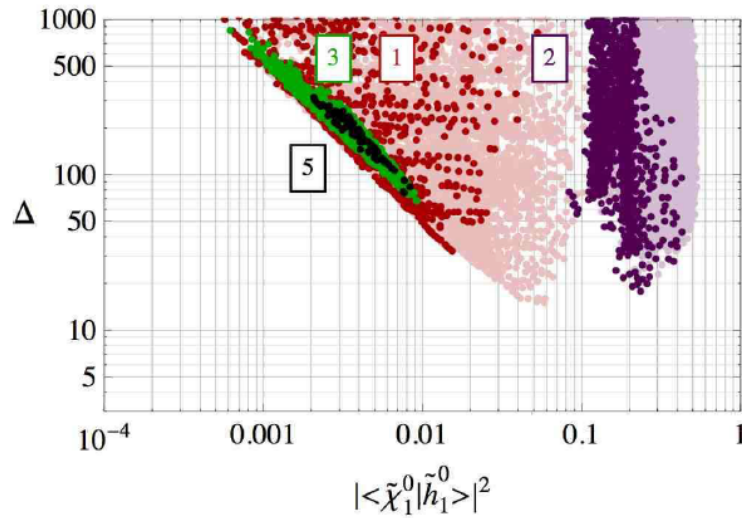
Cassel, Ghilencea, GGR



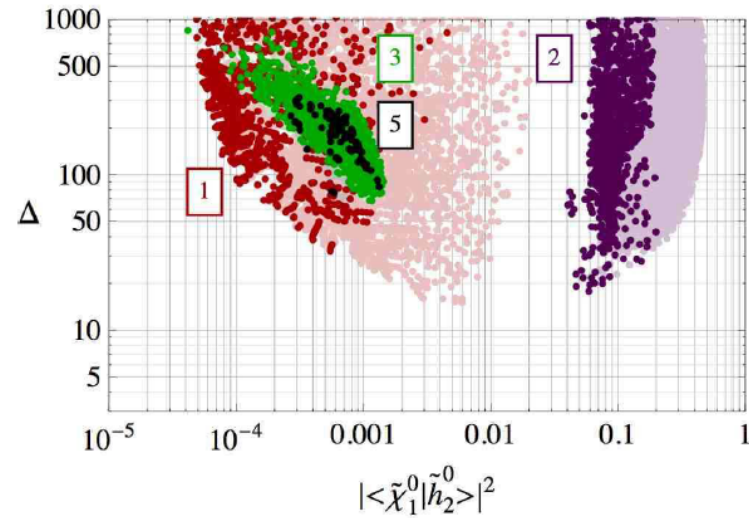
Direct dark matter searches: (spin independent)



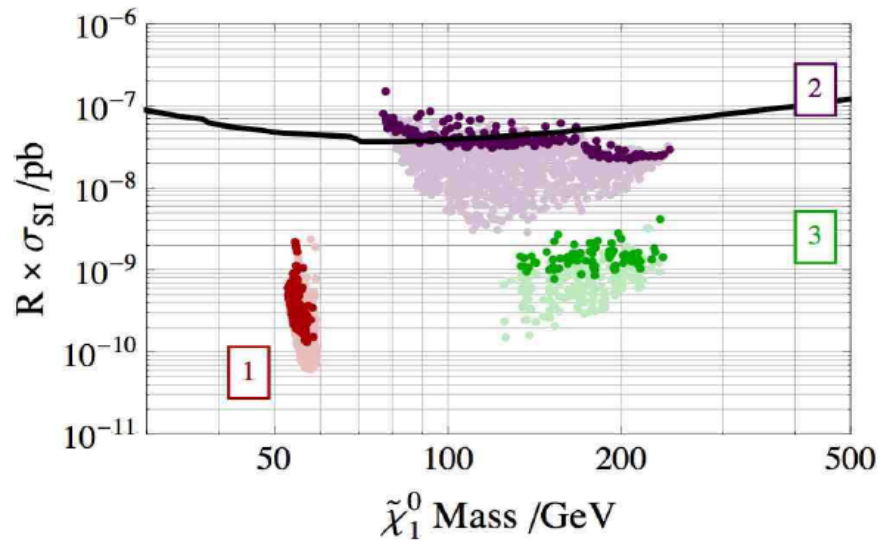
DM - Scaled spin independent cross section for LSP-proton scattering:



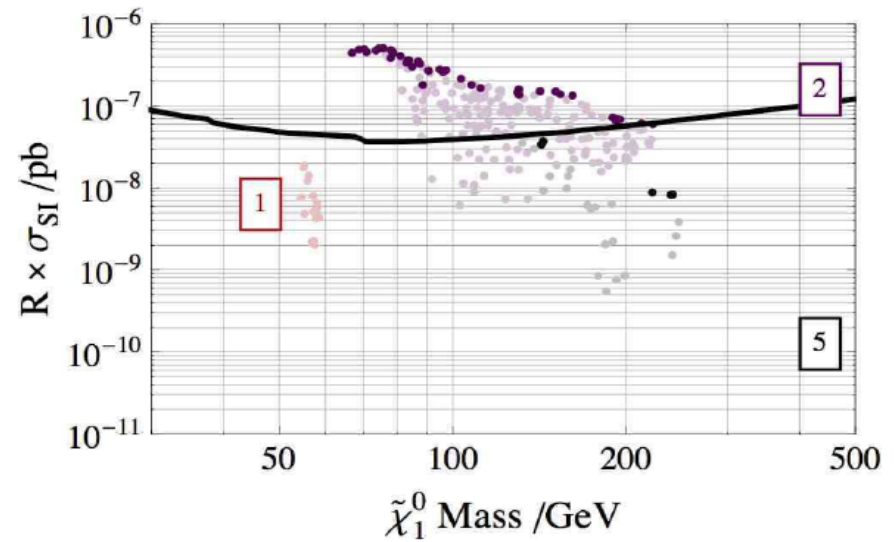
(a) LSP \tilde{h}_1^0 component



(b) LSP \tilde{h}_2^0 component



(a) $\tan \beta \leq 45$
 $\Delta < 100$



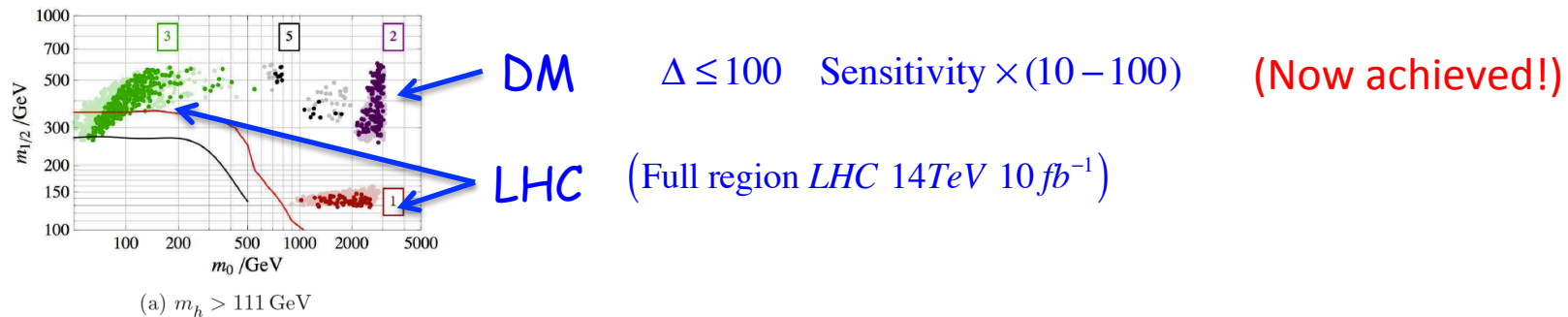
(b) $50 \leq \tan \beta \leq 55$
 $\Delta < 100$

CMSSM summary:

- Minimises MSSM fine tuning (focus point) (c.f. gauge mediation $\Delta \gg \Delta_{CMSSM}$)

$$\text{Max}[\Delta_{EW}, \Delta_{\Omega}] = 15(29), \quad m_h = 114(116) \pm 2 \text{ GeV}$$

- Complementary DM & LHC searches

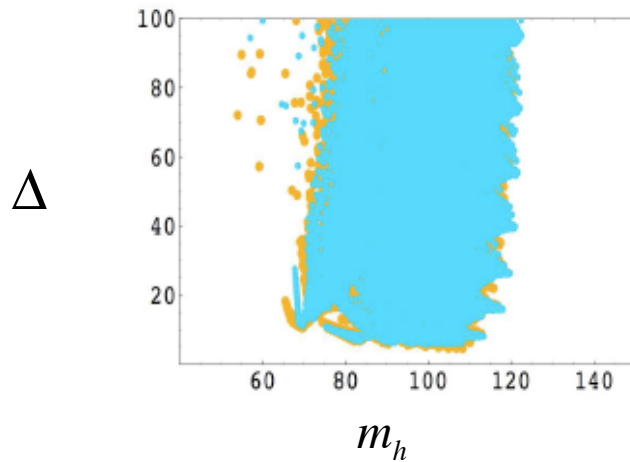


- **BUT** $\Delta > 300$ for $m_H = 126 \text{ GeV}$

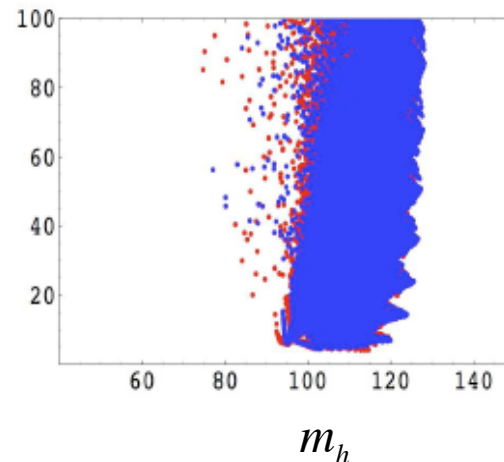
I. Reduced fine tuning : New heavy states - higher dimension operators

$$\delta L = \int d^2\theta \frac{1}{M_*} (\mu_0 + c_0 S) (H_1 H_2)^2, \quad S = m_0 \theta \theta \quad \text{Dimension 5}$$

$$\delta V = \varsigma_1 (|h_1|^2 + |h_2|^2) h_1 h_2 + \varsigma_2 (h_1 h_2)^2; \quad \varsigma_1 = \frac{\mu_0}{M_*}, \quad \varsigma_2 = \frac{c_0 m_0}{M_*}$$



MSSM



+ dim 5 operators

Cassel, Ghilencea, GGR
Casas, Espinosa, Hidalgo
Dine, Seiberg, Thomas
Batra, Delgado, Tait
Kaplan,

Even for $M_* = 65 \mu_0$ a significant shift of m_h for constant Δ

...effect mainly comes from ς_1 term ... origin?

Reduced fine tuning : singlet extensions

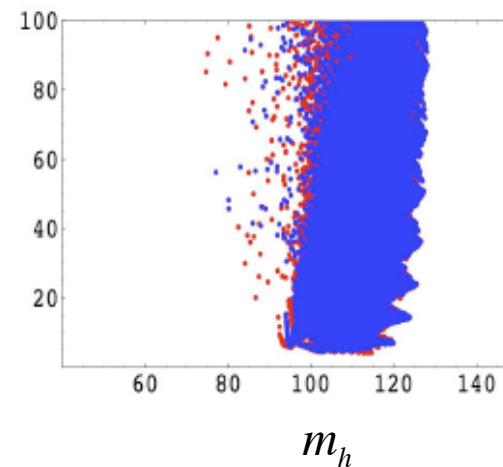
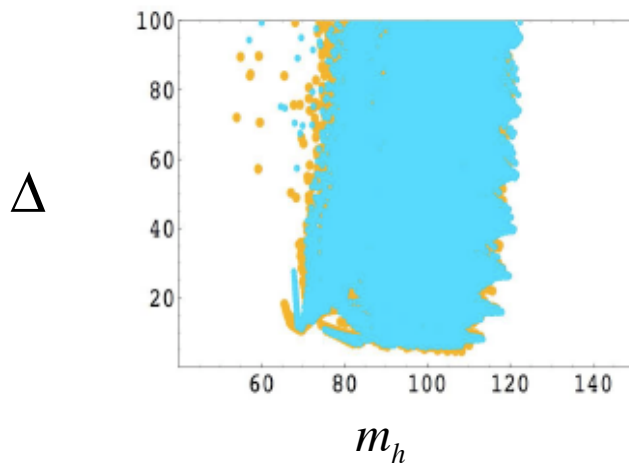
$$W = W_{\text{Yukawa}} + (\mu + \lambda S)H_u H_d + \frac{\mu S}{2}S^2 + \frac{\kappa}{3}S^3 + \xi S \quad \text{GNMSSM}$$

$$\mu_s \gg m_{3/2} \quad \dagger$$

$$\text{c.f. } W = W_{\text{Yukawa}} + \lambda S H_u H_d + \frac{\kappa}{3}S^3 \quad \text{NMSSM}$$

$$W_{\text{eff}}^{\text{GNMSSM}} = (H_u H_d)^2 / \mu_s + \mu H_u H_d$$

$$\frac{\mu}{\mu_s} (|H_u|^2 + |H_d|^2) H_u H_d \quad \xrightarrow{\nu^2 = -\frac{m^2}{\lambda}}$$



Reduced fine tuning in GNMSSM (but not NMSSM) \dagger

SUSY extensions of the Standard Model

R-symmetry ensures Singlet extensions natural

SUSY extensions of the Standard Model

NMSSM spectrum

No perturbative μ term

Commutates with $SO(10)$

Anomaly cancellation

N	q_{10}	$q_{\bar{5}}$	q_{H_u}	q_{H_d}	q_S
4	1	1	0	0	2
8	1	5	0	4	6

R-symmetry ensures singlets light

D=5 operators

up and down Yukawas allowed

$$3q_{10} + q_{\bar{5}} + q_{H_u} + q_{H_d} = 4 \pmod{N} \Rightarrow 3q_{10} + q_{\bar{5}} = 0 \pmod{N} \Rightarrow \frac{1}{M} \cancel{QQQL} \quad \frac{1}{M} LLH_u H_u$$

Weinberg operator

SUSY breaking

$\langle W \rangle, \langle \lambda \lambda \rangle$ R=2 non=perturbative breaking

Domain walls and tadpoles safe Abel

$$Z_{4,8}^R \rightarrow Z_2^R \quad R\text{-parity}$$

$$\mu \sim m_{3/2}, \quad O\left(\frac{m_{3/2}}{M^2} QQQL\right)$$

$$W = W_{MSSM} + \lambda S H_u H_d + \kappa S^3 + \Delta W$$

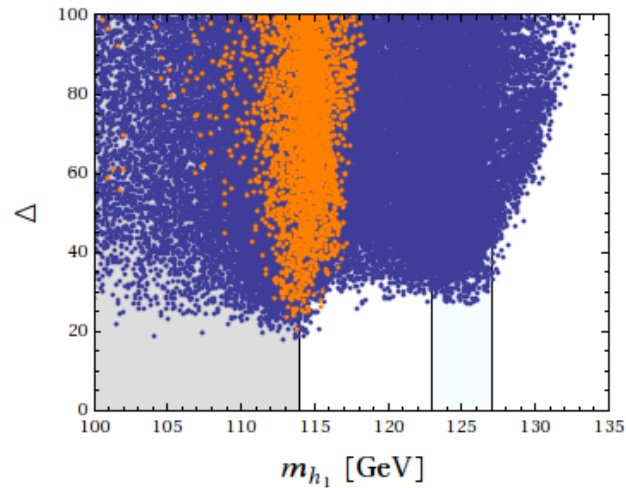
$$\Delta W_{Z_4^R} \sim m_{3/2} H_u H_d + m_{3/2}^2 S + m_{3/2} S^2$$

$$\Delta W_{Z_8^R} \sim m_{3/2}^2 S$$

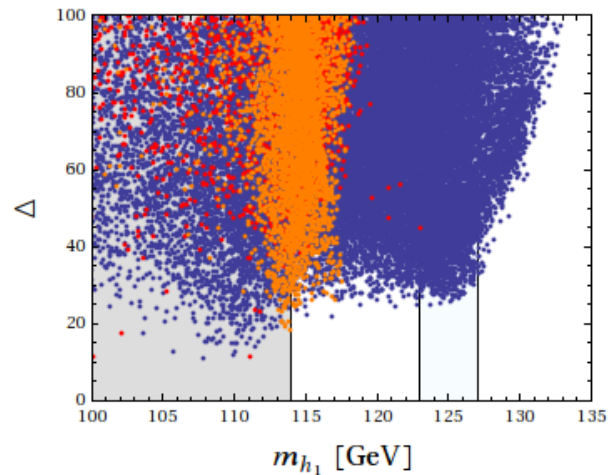
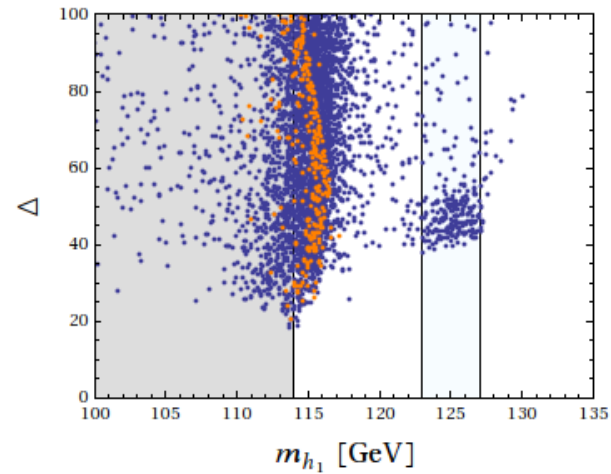
← μ term and mass terms “natural”

GNMSSM (c.f. NMSSM)

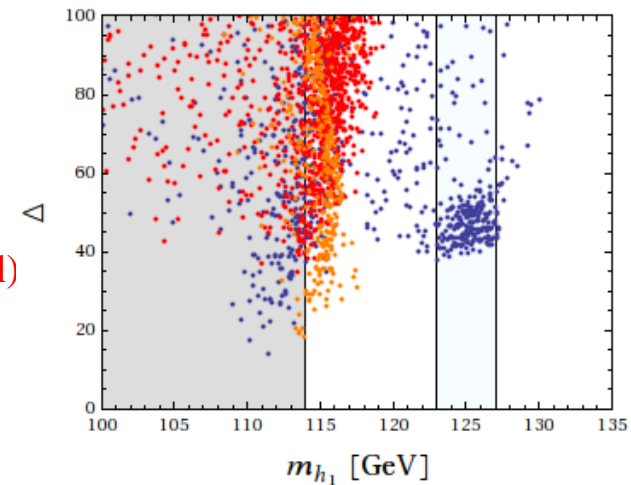
Fine tuning in the GNMSSM $(\lambda \leq 0.7^\dagger)$



- CMSSM
- CGNMSSM
- (universal masses)



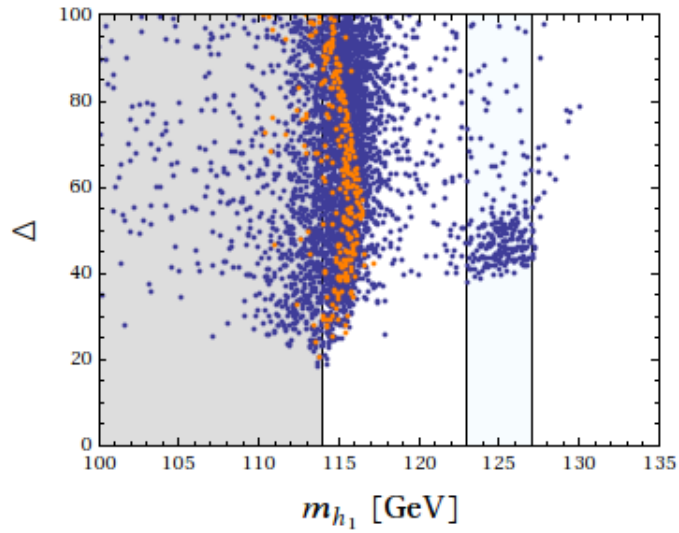
- CMSSM
- CGNMSSM
- CNMSSM
- (Higgs not universal)



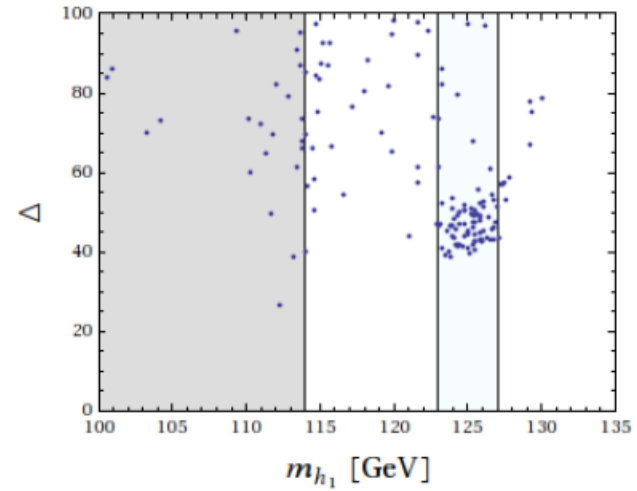
LHC constraints
applied

LHC + DM constraints
applied

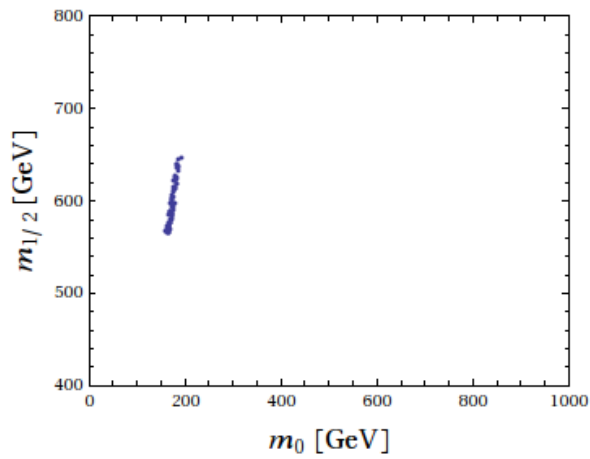
Dark Matter structure



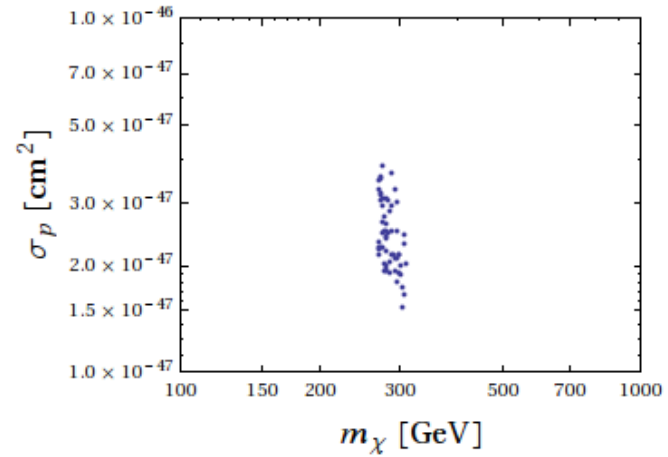
$$\rho_{LSP} \leq \rho_{DM}$$



$$\rho_{LSP} \approx \rho_{DM}$$



Stau co-annihilation



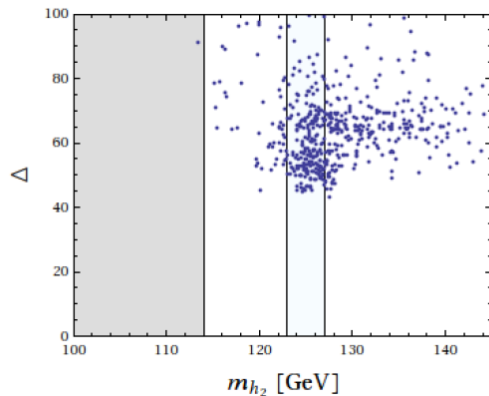
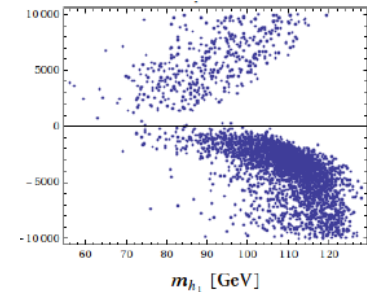
DM searches insensitive

GENERAL-NMSSM PHENOMENOLOGY

Higgs structure (h_u, h_d, s)

- $\mu_s \gg \mu$ MSSM SUSY structure with heavy Higgs
- $\mu_s, m_s, b_s \sim \mu$ $h_1 \simeq H_{u,d} + \epsilon S, \quad h_2 = S - \epsilon H_{u,d}$

... h_2 may be lighter than LEP bound



$m_{h_1} \text{ v/s } \Delta$ for the case $m_{h_2} < m_{h_1}$

Benchmark points

	BP1	BP2	BP3	BP4	BP5
m_0 [GeV]	746	163	957	573	752
$m_{1/2}$ [GeV]	476	568	557	482	472
$\tan \beta$	2.7	2.9	2.8	3.4	2.8
A_0 [GeV]	1433	1666	782	27	-198
λ	1.43	1.47	1.58	1.34	1.12
κ	-0.1	0.09	-0.005	1.52	1.03
A_λ [GeV]	A_0	A_0	A_0	400	192
A_κ [GeV]	A_0	A_0	A_0	-323	-326
v_S [GeV]	-841	-190	-929	390	281
μ_S [GeV]	-5931	-5354	-5799	131	-37
$m_{h_d}^2$ [GeV ²]	m_0^2	m_0^2	m_0^2	$9.1 \cdot 10^5$	$5.4 \cdot 10^5$
$m_{h_u}^2$ [GeV ²]	m_0^2	m_0^2	m_0^2	$2.3 \cdot 10^6$	$2.4 \cdot 10^6$
m_s^2 [GeV ²]	m_0^2	m_0^2	m_0^2	$2.8 \cdot 10^6$	$1.7 \cdot 10^6$
μ [GeV]	-750	-1136	-934	-33	10
$b\mu$ [GeV ²]	$-2.4 \cdot 10^6$	$-1.2 \cdot 10^6$	$-2.3 \cdot 10^6$	147	26
b_s [GeV ²]	$-1.9 \cdot 10^7$	$-5.4 \cdot 10^6$	$-1.4 \cdot 10^7$	326	144
ξ_s [GeV ³]	$2.2 \cdot 10^9$	$1.5 \cdot 10^9$	$3.0 \cdot 10^9$	22	-8
m_{squark} [GeV]	1256-1293	1207-1263	1507-1548	1211-1248	1280-1315
$m_{\tilde{g}}$ [GeV]	1219	1389	1416	1242	1235
m_{h_1} [GeV]	124	123.5	125	93.5	78
m_{h_2} [GeV]	1002	856	1257	125	124
h_1 singletfraction	$\mathcal{O}(10^{-4})$	$\mathcal{O}(10^{-6})$	$\mathcal{O}(10^{-4})$	0.8	0.85
$\text{Br}(h \rightarrow \gamma\gamma)$	$2.29 \cdot 10^{-3}$	$2.28 \cdot 10^{-3}$	$2.2 \cdot 10^{-3}$	$2.5 \cdot 10^{-3}$	$2.66 \cdot 10^{-3}$
$\text{Br}(b \rightarrow s\gamma)$	$3.1 \cdot 10^{-4}$	$3.1 \cdot 10^{-4}$	$3.1 \cdot 10^{-4}$	$3.1 \cdot 10^{-4}$	$3.3 \cdot 10^{-4}$
Δa_μ	$-7.8 \cdot 10^{-11}$	$-2.5 \cdot 10^{-10}$	$-5.4 \cdot 10^{-11}$	$1.7 \cdot 10^{-10}$	$8 \cdot 10^{-11}$
$\delta\rho$	$6.2 \cdot 10^{-5}$	$6.6 \cdot 10^{-5}$	$7.5 \cdot 10^{-5}$	$1.9 \cdot 10^{-4}$	$3.1 \cdot 10^{-4}$
$m_{\tilde{\chi}_1^0}$ [GeV]	229	270	168	99	70
$\tilde{\chi}_1^0$ singlinofraction	$\mathcal{O}(10^{-5})$	$\mathcal{O}(10^{-5})$	$\mathcal{O}(10^{-5})$	0.1	0.2
Ωh^2	7.5	0.10	7.4	0.017	0.11
σ_p [cm ²]	$2.8 \cdot 10^{-47}$	$2.2 \cdot 10^{-47}$	$6 \cdot 10^{-47}$	$1.2 \cdot 10^{-44}$	$1.3 \cdot 10^{-45}$
Δ (Fine-tuning)	34.9	51.0	51.8	44.9	52.7



Table 1: Benchmark scenarios for the GNMSSM for the universal (BP1-BP3) and the general (BP4-BP5) case. m_{squark} shows the range of squark masses of the first two generations. For the last two points the second lightest Higgs is mostly MSSM-like.

GENERAL-NMSSM PHENOMENOLOGY

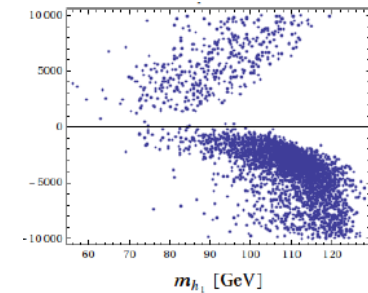
Higgs structure (h_u, h_d, s)

- $\mu_s \gg \mu$ MSSM SUSY structure with heavy Higgs

- $\mu_s, m_s, b_s \sim \mu$ $h_1 \simeq H_{u,d} + \epsilon S, \quad h_2 = S - \epsilon H_{u,d}$

... h_2 may be lighter than LEP bound

$h_1 \rightarrow h_2 h_2$ large



... DM and SUSY phenomenology modified

e.g. Bino LSP

... h_1 may have enhanced $\gamma\gamma$ rate

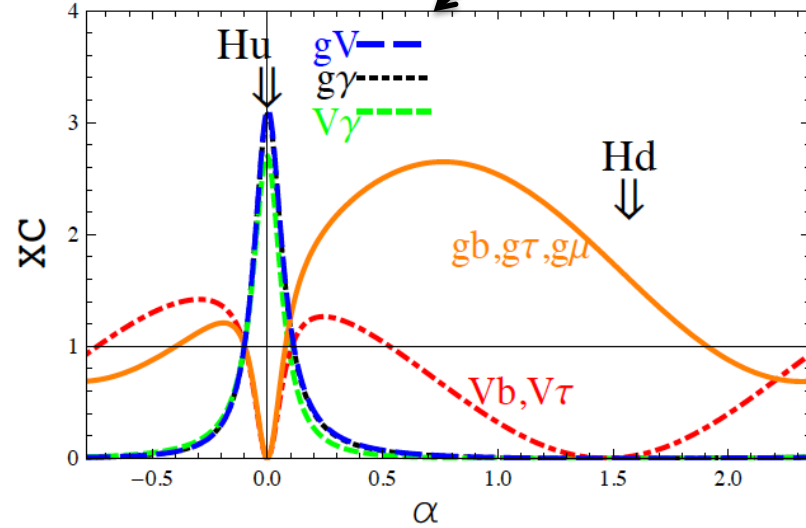
$h \rightarrow \gamma\gamma$ enhancement in the MSSM

$g\gamma \equiv gg \rightarrow \gamma\gamma$ etc

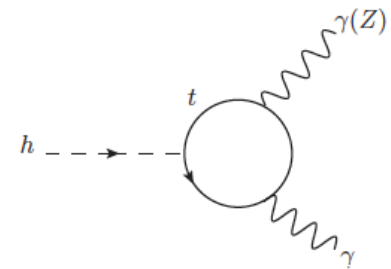
$$\frac{h}{\sqrt{2}} = c_\alpha H_u^0 - s_\alpha H_d^0$$

$\alpha \approx 0$ fine tuned

$$(M_H^2)_{12} = -(m_A^2 + M_Z^2) \sin\beta \cos\beta + \text{Loop}_{12} = 0$$

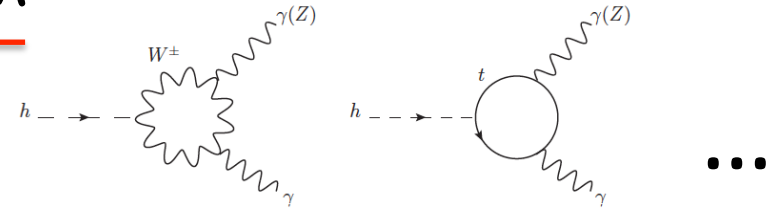


	$\sigma_h/\sigma_{h_{\text{SM}}}$	FT($\alpha = 0$) ($\alpha = 0.06$)		CMS[2]	ATLAS[1]	Tevatron[11]
$VV \rightarrow \tau\tau$	$V\tau$	0	0.60			
$q\bar{q} \rightarrow Vb\bar{b}$	qb	0	0.60	$1.2^{+2.1}_{-1.9}$	$-0.8^{+1.8}_{-1.7}$	2.0 ± 0.7
$gg \rightarrow \tau^-\tau^+$	$g\tau$	0	0.74	$0.63^{+1.00}_{-1.28}$	0.0 ± 1.7	
$gg \rightarrow \gamma\gamma$	$g\gamma$	3.1	1.9	1.62 ± 0.68	$1.6^{+0.8}_{-0.7}$	$3.4^{+3.1}_{-2.4}$
$gg \rightarrow WW^*$	gW	3.1	2.0	0.40 ± 0.55	0.20 ± 0.62	$0.0^{+1.0}_{-0.0}$
$gg \rightarrow ZZ^*$	gZ	3.1	2.0	$0.58^{+0.94}_{-0.58}$	$1.4^{+1.3}_{-0.8}$	
$VV \rightarrow \gamma\gamma$	$V\gamma$	2.7	1.6	$3.8^{+2.4}_{-1.8}$ [2]		



$h \rightarrow \gamma \gamma$ enhancement in the MSSM

See Djouadi review



New heavy particle contributions:

$$\mathcal{L}_{\gamma\gamma} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \sum_i \frac{b_i e^2}{16\pi^2} \log \frac{\Lambda^2}{m_i^2} + \dots$$

$$\left\{ \begin{array}{ll} b_{1/2} = \frac{4}{3} N_{c,f} Q_f^2 & \text{for a Dirac fermion ,} \\ b_1 = -7 & \text{for the } W \text{ boson ,} \\ b_0 = \frac{1}{3} N_{c,S} Q_S^2 & \text{for a charged scalar .} \end{array} \right.$$

Carena et al

SUSY: light $\tilde{\tau}$ ($LEP : m_{\tilde{\tau}} > 100 GeV$)

$$A_{\gamma\gamma}^{SM} + \Delta A_{\gamma\gamma} \propto -13 - \frac{m_{\tilde{\tau}_2}}{6m_{\tilde{\tau}_1}} \left(1 - \frac{m_{\tilde{\tau}_2}}{m_{\tilde{\tau}_1}} \right)$$

anomaly/mirage..?

requires $\tan \beta \sim 60$, $\mu \geq 300 GeV$, $m_{\tilde{\tau}} \sim 100 GeV$

maximally mixed stau, heavy higgsinos, LSP light Bino

$h \rightarrow \gamma \gamma$ enhancement in the GNMSSM (λ NMSSM)

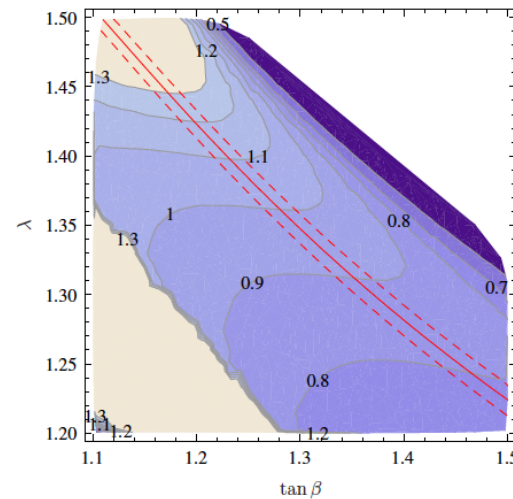
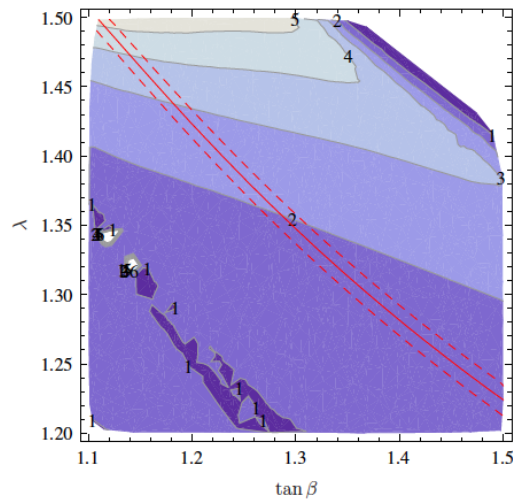
New interaction allows sizeable correction at small $\tan\beta$:

$$W = \lambda S H_u H_d \Rightarrow V \supset \lambda^2 |H_u H_d|^2$$

$$g_{hH^+H^-} = \frac{i}{4} \left\{ v \cos \beta \left[2(\lambda^2 - g_2^2) + (g_1^2 + g_2^2 - 2\lambda^2) \cos 2\beta \right] Z_1^h \right.$$

$$- v \sin \beta \left[2(g_2^2 - \lambda^2) + (g_1^2 + g_2^2 - 2\lambda^2) \cos 2\beta \right] Z_2^h$$

$$\left. - 4\lambda \left[v_s \lambda + \sqrt{2}\mu + \left(\frac{1}{\sqrt{2}}(A_\lambda + \mu_s) + v_s \kappa \right) \sin 2\beta \right] Z_3^h \right\}$$



Higgsino (and chargino) enhancement in large λ limit

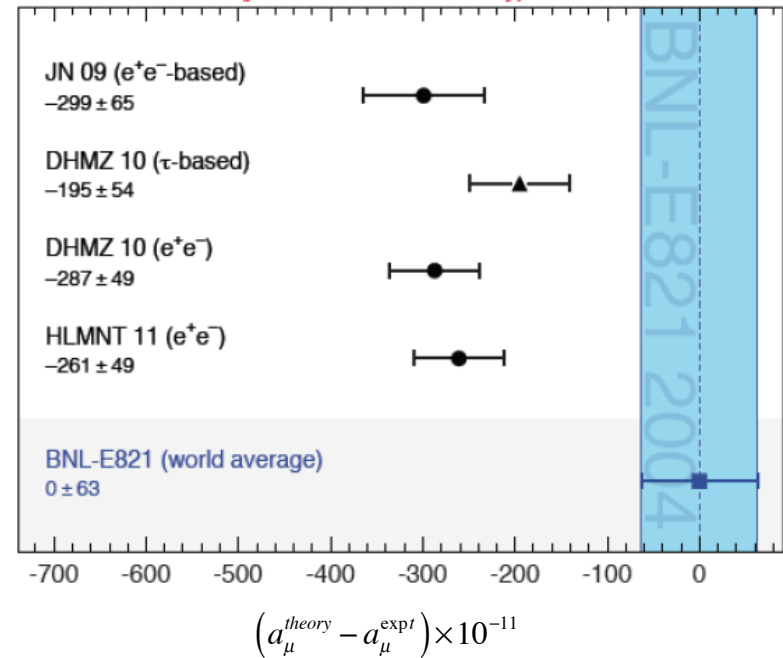
Muon g-2

$$a_\mu^{theory} - a_\mu^{expt} = -(28.7 \pm 8.0) \times 10^{-10}$$

Theory error from hadronic contribution:

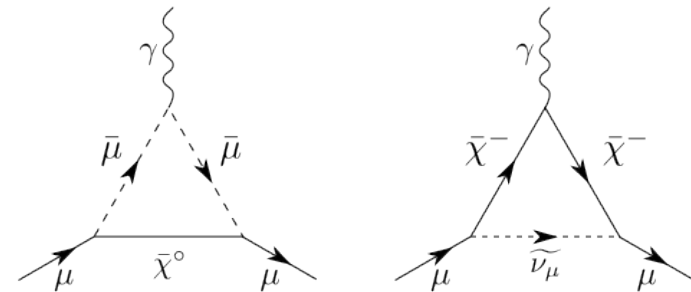
$$\delta a_\mu^{e^+e^-} = 3.6 \sigma$$

$$\delta a_\mu^\tau = 2.4 \sigma$$



SUSY

$$\delta a_\mu^{SUSY} = -13 \times 10^{-10} \left(\frac{100 \text{ GeV}}{M_{SUSY}} \right)^2 \tan \beta$$



Needs light sleptons - anomaly/mirage spectrum?

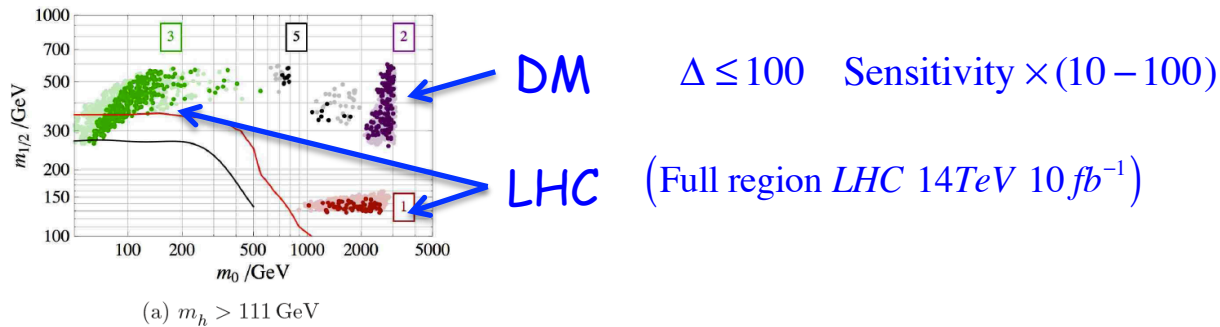
With slepton universality - $h \rightarrow \gamma \gamma$ plausibly correct!

Summary (before Higgs discovery)

- Hierarchy problem \Rightarrow SUSY breaking structure and/or further states

- CMSSM $m_i = M_0$ $Max[\Delta_{EW}, \Delta_{\Omega}] = 15(29)$, $m_h = 114(116) \pm 2 GeV$

Complementary DM & LHC searches



(Gauge mediation $\Delta \gg 100$)

- NMSSM Reduced $\Delta \Rightarrow$ GNMSSM $\Rightarrow Z_{4R}, Z_{8R}$

SUSY states can be (slightly) heavier
 $m_h \rightarrow 130 GeV$

- Gaugino focus point $M_i = \eta_i M_{1/2}$

Characteristic η_i

Light $\chi^{0,\pm}$

$\delta(b \rightarrow s\gamma)$ significant

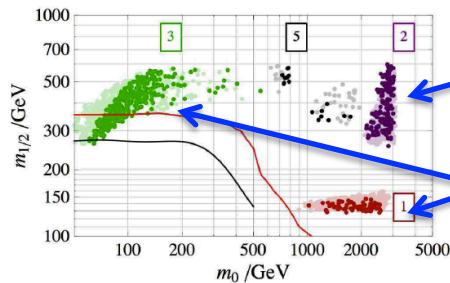
$\delta(g-2)$ Small(?)

Summary (after Higgs discovery)

- Hierarchy problem \Rightarrow SUSY breaking structure and/or further states

- CMSSM $m_i = M_0$ $Max[\Delta_{EW}, \Delta_{\Omega}] = 15(29)$, $m_h = 114(116) \pm 2 GeV$

Complementary DM & LHC searches



(a) $m_h > 111 GeV$

DM $\Delta \leq 100$ Sensitivity $\times (10 - 100)$ (Now achieved!)

LHC (Full region LHC 14TeV $10 fb^{-1}$)

$\Delta_{MSSM} > 300$ for $m_H = 126 GeV$

- NMSSM Reduced $\Delta \Rightarrow$ GNMSSM $\Rightarrow Z_{4R}, Z_{8R}$

Further light/invisible Higgs a possibility



- Gaugino focus point

Mixed anomaly mediation, mirage mediation ...

Light sleptons...g-2, $h \rightarrow \gamma \gamma$



- Natural SUSY (but 125GeV Higgs?), SPLIT SUSY(!) ...

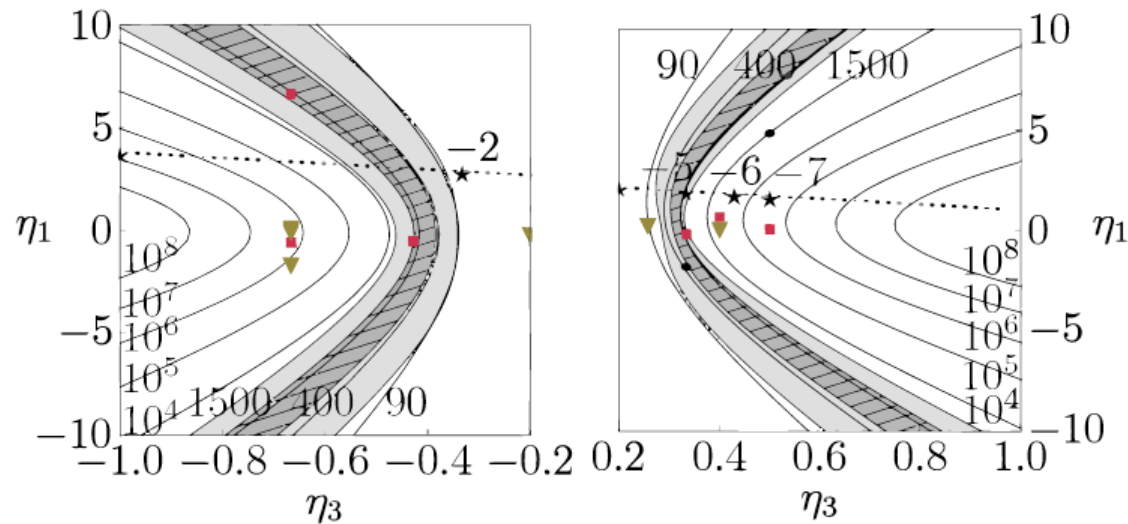
$$\begin{aligned}
\frac{M_Z^2}{2} = & - .87 \mu^2(0) + 3.6 M_3^2(0) - .12 M_2^2(0) + .007 M_1^2(0) \\
& - .71 m_{H_U}^2(0) + .19 m_{H_D}^2(0) + .48 (m_Q^2(0) + m_U^2(0)) \\
& - .34 A_t(0) M_3(0) - .07 A_t(0) M_2(0) - .01 A_t(0) M_1(0) + .09 A_t^2(0) \\
& + .25 M_2(0) M_3(0) + .03 M_1(0) M_3(0) + .007 M_1(0) M_2(0)
\end{aligned}$$

II. Reduced fine tuning : nonuniversal gaugino masses

Reduced fine tuning: nonuniversal gaugino masses

$$16\pi^2 \frac{d}{dt} m_{H_u}^2 = 3 \left(2 |y_t|^2 (m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2 |a_t|^2 \right) - 6g_2^2 |M_2|^2 - \frac{6}{5} g_1^2 |M_1|^2$$

New focus point: cancellation between M_3 and M_2 contributions if $|M_2|^2 \simeq |M_3|^2$ at M_{SUSY}



$$M_3 : M_2 : M_1 = \eta_3 : 1 : \eta_1$$

Reduced fine tuning: nonuniversal gaugino masses

$$16\pi^2 \frac{d}{dt} m_{H_u}^2 = 3 \left(2 |y_t|^2 (m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2 |a_t|^2 \right) - 6g_2^2 |M_2|^2 - \frac{6}{5} g_1^2 |M_1|^2$$

New focus point: cancellation between M_3 and M_2 contributions if $|M_2|^2 \simeq |M_3|^2$ at M_{SUSY}

Natural ratios? e.g.:

GUT: $SU(5): \Phi^N \subset (24 \times 24)_{\text{symm}} = 1 + 24 + 75 + 200; \quad SO(10): (45 \times 45)_{\text{symm}} = 1 + 54 + 210 + 770$

	$\eta_3 : 1 : \eta_1$	$2.7\eta_3 : 1 : 0.5\eta_1$
Representation	$M_3 : M_2 : M_1$ at M_{GUT}	$M_3 : M_2 : M_1$ at M_{EWSB}
1	1:1:1	6:2:1
24	2:(-3):(-1)	12:(-6):(-1)
75	1:3:(-5)	6:6:(-5)
200	1:2:10	6:4:10

String: $(3 + \delta_{GS}) : (-1 + \delta_{GS}) : \left(-\frac{33}{5} + \delta_{GS} \right)$ (OII, also mixed moduli anomaly)

Phenomenology

- Gaugino mass ratios

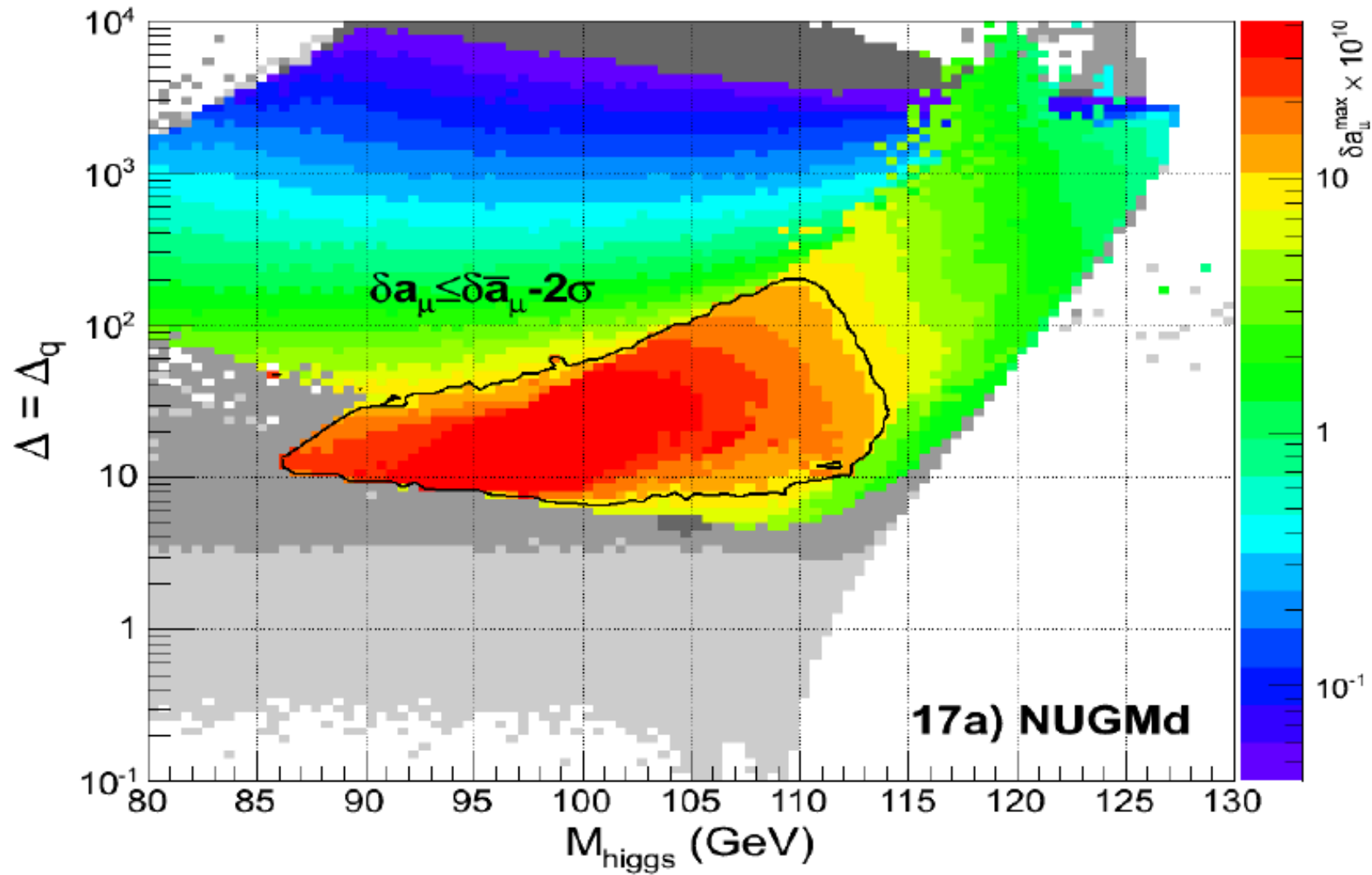
$$\frac{M_i(Q)}{M_{1/2}} = \eta_i \frac{\alpha_i(Q)}{\alpha_i(M_X)} \Rightarrow \begin{aligned} \frac{M_1(Q)}{M_2(Q)} &\approx 0.5\eta_1 \\ M_2(Q) &\approx 0.8M_{1/2} \\ \frac{M_3(Q)}{M_2(Q)} &\approx 2.7\eta_3 \end{aligned}$$

.... gauginos can be very heavy

- Light neutralino and 2 charginos nearly degenerate

$$\begin{aligned} m_{\chi_2^0} - m_{\chi_1^0} &= M_Z^2 \left(\frac{s_W^2}{M_1} + \frac{c_W^2}{M_2} \right) + \mathcal{O}\left(\frac{M_Z^3}{M_2^2}\right) \\ m_{\chi_1^\pm} - m_{\chi_1^0} &= \frac{1}{2}M_Z^2 \left(\frac{s_W^2}{M_1} + \frac{c_W^2}{M_2} \right) + \frac{1}{2}M_Z^2 \left(\frac{s_W^2}{M_1} - \frac{c_W^2}{M_2} \right) \epsilon \sin 2\beta + \mathcal{O}\left(\frac{M_Z^3}{M_2^2}\right) \end{aligned}$$

+ for $|M_1| < \mu$, Bino or Higgsino LSP candidate



2-loop fine tuning in 75 case

Ghilenca, Lee, Park