Consider a sequence of positive random variables  $\{J_i\}_{i=1}^{\infty}$  with the meaning of inter-event durations and another sequence of (not-necessarily positive) random variables  $\{X_i\}_{i=1}^{\infty}$  with the meaning of jumps. Define the following two random walks:

$$T_n := \sum_{i=1}^n J_i,$$

and

$$Y_n := \sum_{i=1}^n X_i.$$

Introduce the counting process N(t) as

$$N(t) = \max\{n : T_n \le t\},\$$

and define the following random sum of random variables

$$Y(t) := Y_{N(t)} = \sum_{i=1}^{N(t)} X_i$$

A lot is known on Y(t) and its functional limits under appropriate scaling when the  $J_i$ s and the  $X_i$ s are independent and identically distributed random variables and they are mutually independent. Little is known when these hypotheses are not satisfied and, moreover, when these variables are non-stationary as a function of their index *i*. We want to systematically study this situation.

Two recent papers on this are arXiv:1601.03965 [math.PR] as well as arXiv:1711.08768 [math.PR].

**Key words:** Non-stationary stochastic processes, functional limit theorems, large deviations, moderate deviations.