## **Resilient Entangling Gates for Trapped Ions**

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Constructing a large-scale ion trap quantum processor will require entangling gate operations that are robust in the presence of noise and experimental imperfection. We experimentally demonstrate how a new type of Mølmer-Sørensen gate protects against infidelity caused by heating of the motional mode used during the gate. Furthermore, we show how the same technique simultaneously provides significant protection against slow fluctuations and mis-sets in the secular frequency. Since this parameter sensitivity is worsened in cases where the ions are not ground-state cooled, our method provides a path towards relaxing ion cooling requirements in practical realizations of quantum computing and simulation.

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Building a quantum processor capable of solving some of the most complex real-world problems will require both a large number of qubits and the ability to accurately perform gate operations on these qubits. While such gate operations have been demonstrated on pairs of carefully controlled ions with high fidelity [1,2], maintaining such fidelities as systems scale towards a large quantum computer will require more robust operations. Many proposed trapped ion quantum processors will require large numbers of ions to be trapped close to the surface of a microfabricated chip [3-6], which can cause increased gate infidelities due to heating and dephasing of the ions' motion caused by voltage fluctuations in the electrodes of the chip [7]—the heating rate scales unforgivingly with distance as approximately  $d^{-4}$  [8]. In addition, it is likely that there will be slowly changing variations in experimental parameters, differing both from position to position on the chip and drifting in time, which will be difficult to fully characterize and correct for during the operation of the processor. This problem is exacerbated when the initial mean excitation of the motional mode,  $\bar{n}$ , is higher. This could, e.g., occur as a result of heating during shuttling processes which form a core part of a number of architectures for a large-scale quantum computer [3,5]. A quantum processor thus requires gate operations that provide low error rates not just under ideal conditions, but that are resilient enough to be successfully implemented in realistic experimental environments.

The two-qubit Mølmer-Sørensen (MS) gate is one of a class of trapped ion gates that operate by state-dependent coherent excitation and deexcitation of a motional mode of a pair of ions during the gate operation [9-11], and this motional excitation can be represented as a circular path in phase space. Sørensen and Mølmer discussed how the effect of heating could be reduced by performing multiple smaller circles in phase space [10]. While this is effective in

reducing the impact of heating, the gate time scales as the square root of the number of loops. Hayes *et al.* experimentally demonstrated a similar technique as a method of reducing the effect of a "symmetric" detuning error, such as would be caused by an incorrectly measured trap frequency [12].

Noise suppression can be effectively achieved with less impact on the gate time by tracing out more complicated paths in phase space [13–15]. Recent theoretical work proposed a method whereby the infidelity due to heating can be significantly reduced with a smaller impact on gate time than by just performing multiple smaller loops [13]. Here, we experimentally demonstrate this effect, using a pair of trapped <sup>171</sup>Yb<sup>+</sup> ions. We then build upon this result to show that these same paths also dramatically increase the resilience of the gate to errors caused by symmetric detuning errors. We demonstrate how this resilience becomes particularly significant in the case of the mode used for the gate not being cooled close to the ground state.

By off-resonantly driving the red and blue motional sidebands of a pair of ions coupled to a common motional mode, the MS Hamiltonian

$$H_{\rm MS} = \frac{\hbar\delta}{4} \hat{S}_x (\hat{a}^{\dagger} e^{i\delta t} + \hat{a} e^{-i\delta t}) \tag{1}$$

can be realized, where  $\hat{S}_x = \hat{\sigma}_{x1} + \hat{\sigma}_{x2}$  is the sum of the  $\hat{\sigma}_x$  matrices for the two ions,  $\hat{a}^{\dagger}$  and  $\hat{a}$  are the motional mode raising and lowering operators, respectively, and  $\delta$  is the magnitude of the detuning from the red and blue sidebands. When the driving fields are applied for a time  $\tau = 2\pi/\delta$ , the pair of ions undergo the unitary transformation

$$U_{\rm MS} = \exp\left(i\frac{\pi}{4}\hat{\sigma}_{x1}\hat{\sigma}_{x2}\right),\tag{2}$$

which can produce a maximally entangled state from an initial product state.

In practice, there are a number of mechanisms by which the fidelity of the MS gate will be reduced from 1. Here we consider two sources of infidelity: a dephasing of the gate caused by heating of the motional mode during the gate process, and an incorrect phase pickup and residual entanglement of the qubits with the motional mode caused by a symmetric detuning frequency error. This symmetric detuning occurs as a result of the magnitude of the gate detuning  $\delta$  being set incorrectly by the same amount for both ions,  $\Delta$ —for instance, due to a drift in trap frequency.

If the total infidelity is small, the fidelity of the gate can be expressed as a sum of independent infidelities  $F = 1 - (E_{\rm h} + E_{\Delta} + E_{\rm oth})$ , where  $E_{\rm h}$  is the infidelity due to heating,  $E_{\Delta}$  is the infidelity due to symmetric detuning error, and  $E_{\rm oth}$  is the sum of any other infidelities, which we henceforth do not consider. Since the infidelities are small, we will consider the infidelities only to the leading order in either heating rate or detuning error. The errors due to nonzero heating rate and symmetric detuning error are then

$$E_{\rm h} = \frac{\pi \dot{\bar{n}}}{\delta}, \qquad E_{\Delta} = \left(\frac{3}{4} + \bar{n}\right) \pi^2 \left(\frac{\Delta}{\delta}\right)^2, \qquad (3)$$

respectively, where  $\bar{n}$  is the heating rate and  $\Delta$  is the error in gate detuning (see Supplemental Material [16]. Note that the error due to incorrect detuning is also dependent on the mean excitation of the motional mode at the start of the gate  $\bar{n}$  (we assume the phonon distribution to be thermal)—if the ion is "hotter" (larger  $\bar{n}$ ) at the start of the gate operation, it becomes much more sensitive to parameter errors.

Haddadfarshi *et al.* introduced a method to reduce the effect of heating and dephasing of the motional mode on the gate fidelity [13]. They considered a multitone generalization of the MS gate (MTMS), where instead of driving each ion sideband with a single field, MTMS gates use N fields or tones to drive each sideband at detunings  $\delta_j = j\delta$  with  $\{j = 1, ..., N\}$  as shown in Fig. 1(a), and each tone's strength is given by coefficients  $c_j$ , that can be chosen to be real. The Hamiltonian thus becomes

$$H_{\rm MS} = \hbar \delta \hat{S}_x \sum_{j=1}^N c_j (\hat{a}^{\dagger} e^{ij\delta t} + \hat{a} e^{-ij\delta t}). \tag{4}$$

The condition to produce a maximally entangling unitary constrains the values of the coefficients  $c_j$  to be  $\sum_{j=1}^{N} (c_j^2/j) = \frac{1}{16}$ , which corresponds to a standard single-tone MS gate having a coefficient  $c_1 = \frac{1}{4}$ .

The effect of any MS-type Hamiltonian is to excite the motion of different spin components, causing them to selectively acquire a phase, before (ideally) returning them to their initial motional state. This excitation can be considered as a time-varying displacement in a rotating



FIG. 1. (a) Energy level diagram showing multitone gate fields detuned from the correct gate detuning  $\delta$  by  $\Delta_r$  and  $\Delta_b$  for the red and blue sidebands, respectively. MTMS gates provide protection against errors of the form  $\Delta_r = \Delta_b = \Delta$ . (b) Phase space trajectories for one- (red), two- (blue), and three-tone (green) gates. Unlike the single-tone case, the average displacement  $\langle \alpha(t) \rangle = 0$  for two or more tones. In addition, as the number of tones increases,  $\langle |\alpha(t)|^2 \rangle$  becomes smaller. The effect of this reduction in squared displacement is to reduce the adverse effect of heating on gate fidelity. (c) For a single-tone gate, a symmetric detuning error ( $\delta/\Delta = 0.05$ ) results in both incomplete loops in phase space, causing error due to the residual entanglement between the spin and motional states of the qubit, and incorrect phase accumulation. For the two- and three-tone gates, the loops come much closer to completion (visually indistinguishable from closed loops), effectively eliminating residual qubit-motion entanglement as a contribution to the infidelity, and although not visually obvious, the phase picked up also becomes closer to the ideal. Both of these effects lead to a reduction in sensitivity to symmetric detuning errors.

phase space, and the effect of heating depends quadratically on the magnitude of this displacement during the gate. Haddadfarshi *et al.* found that the best reduction in the effect of heating of the mode over the course of the gate is found when the average phase space displacement is zero, and the average squared phase-space displacement is minimized over the course of the gate. This corresponds to parameters where  $\sum_{j=1}^{N} (c_j/j) = 0$ , and  $\sum_{j=1}^{N} (|c_j|^2/j^2)$ is minimized (see the Supplemental Material [16] for more detail). The effect of using the MTMS gate on the phase-space trajectories can be seen in Fig. 1(b).

For MTMS gates, the heating rate defining the infidelity is modified by a factor given by (see Supplemental Material [16])

$$\dot{\bar{n}}_{\rm MT} = 8 \left( \sum_{j=1}^{N} \frac{c_j^2}{j^2} + \left( \sum_{j=1}^{N} \frac{c_j}{j} \right)^2 \right) \dot{\bar{n}}.$$
 (5)

The minimization conditions mean that this can be understood as a smaller effective heating rate. For  $N = \{1, 2, 3\}$ , then  $\dot{\bar{n}}_{MT} = \{1, 1/3, 1/5.19\} \times \dot{\bar{n}}$ , respectively.

We show here that MTMS gates also protect against errors due to an incorrect symmetric detuning. In this case, the MTMS Hamiltonian is modified to become

$$H_{\rm MS} = \hbar \delta \hat{S}_x \sum_{j=1}^N c_j (\hat{a}^{\dagger} e^{i(j\delta + \Delta)t} + \hat{a} e^{-i(j\delta + \Delta)t}).$$
(6)

By expanding the fidelity of the gate in powers of the fractional symmetric detuning error,  $\Delta/\delta$ , we obtain the same set of constraints on the coefficients,  $c_j$ , as was obtained when minimizing the effect of motional decoherence, so the gate is protected against both sources of infidelity (see Supplemental Material [16]).

The infidelity of the optimized MTMS gates due to symmetric detuning error, to leading order in  $\Delta/\delta$ , is given by

$$E_{\Delta}^{MT} \simeq 16\pi^2 \left(\frac{\Delta}{\delta}\right)^2 \left(\sum_{j=1}^N \frac{c_j^2}{j^2}\right)^2 \tag{7}$$

$$=\frac{1}{36}\pi^2 \left(\frac{\Delta}{\delta}\right)^2 \simeq 0.028\pi^2 \left(\frac{\Delta}{\delta}\right)^2 \quad (N=2) \tag{8}$$

$$= \frac{39 - 12\sqrt{3}}{1936} \pi^2 \left(\frac{\Delta}{\delta}\right)^2 \simeq 0.0094 \pi^2 \left(\frac{\Delta}{\delta}\right)^2 (N=3). \quad (9)$$

The sensitivity to  $\Delta$  is significantly reduced for two- and three-tone gates compared with the standard MS gate [Eq. (3)]. The infidelity is also independent of the initial distribution of motional states, unlike Eq. (3). This is because the effect of residual qubit-motional entanglement on the fidelity is zero to this order of  $\Delta/\delta$ , the infidelity being completely due to the incorrect phase being acquired during the gate. This may be of particular interest when gates are combined with shuttling operations which induce heating [3,5]. Figure 1(c) shows gates with symmetric detuning error  $\delta/\Delta = 0.05$ . The single-tone gate produces an obviously incomplete loop. For the MTMS gates, while the detuning produces a rotation of the phase-space paths, the two paths appear indistinguishable from closed loopsthe two-tone gate comes almost 70 times closer to completion than the single-tone, and the three-tone gate comes almost 360 times closer.

We demonstrate this technique experimentally using a pair of  $^{171}$ Yb<sup>+</sup> ions [20]. The hyperfine ground state is driven using microwave and radio-frequency radiation, and a magnetic field gradient of 23.6(3) T/m is generated

using permanent magnets to enable the requisite coupling between the internal spin and collective motional modes [21,22]. The ions are decoupled from magnetic field noise using a dressed state system [23–25]. For each ion a pair of microwave fields couples  $|^{2}S_{1/2}, F = 0\rangle \equiv |0\rangle$ with  $|^{2}S_{1/2}, F = 1, m_{F} = -1\rangle \equiv |-1\rangle$  and  $|^{2}S_{1/2}, F = 1, m_{F} = +1\rangle \equiv |+1\rangle$  which, in the interaction picture, gives three well-protected states, including  $(|+1\rangle - |-1\rangle)/\sqrt{2} \equiv |D\rangle$ . The pair of states  $|D\rangle$  and  $|^{2}S_{1/2}, F = 1, m_{F} = 0\rangle \equiv |0'\rangle$  form a well protected qubit with transition frequencies 11.0 MHz and 13.9 MHz for each ion, respectively, and a coherence time of 500 ms.

A maximally entangled Bell state is created and analyzed for standard single-tone (N = 1) and two-tone (N = 2) MS gates, since moving from one to two tones should show the largest improvement in gate robustness. The single-tone MS gate procedure is detailed in more detail in Ref. [26]. The gate was performed on the stretch mode of the ions, with frequency  $\nu/2\pi = 461$  kHz, which gives an effective Lamb-Dicke parameter of  $\eta = 0.004$ . Single- and two-tone gates with the same gate time  $\tau$  and detuning  $\delta$  were compared. The single-tone gate uses a pair of gate fields per ion, each of carrier Rabi frequency  $\Omega_0/2\pi = 36$  kHz, and since  $\delta = 2\eta \Omega_0$ , the detuning is  $\delta/2\pi = 292$  Hz, and the gate time is  $\tau = 2\pi/\delta = 3.42$  ms. The two-tone gate uses two pairs of gate fields per ion, with the Rabi frequencies of the two tones in each pair being  $\Omega_1 = -0.576\Omega_0$  at  $\delta$  and  $\Omega_2 = 1.152\Omega_0$  at  $2\delta$ , corresponding to  $c_1 = -0.144$  and  $c_2 = 0.288$ . The beating between the two tones produces a time-varying Rabi frequency, and thus a time-varying Stark shift that we compensate for by changing the gate field detunings during the gate operation—see the Supplemental Material [16] for more information. Before performing the gate operation, the stretch mode was sideband cooled to an initial temperature of  $\bar{n} \approx 0.1$  [27].

The fidelity of Bell-state production is found by measuring selected elements of the density matrix, specifically the total population in the states  $|0'0'\rangle$  and  $|DD\rangle$ , and the coherence between these two states [26]. A maximum likelihood method was used to determine these two values, as well as the errors in their measurement (see Supplemental Material [16]).

To demonstrate the effectiveness of the MTMS technique for protection against heating, the heating rate was artificially increased. Noise with a flat amplitude spectrum over a bandwidth of 20 kHz, centered around the secular frequency  $\nu$ , was capacitively coupled onto an end-cap dc trap electrode, and the heating rate was controlled by changing the amplitude of this noise. Heating rates with no added noise, and for two different amplitudes of artificial noise, were measured by introducing a varying time delay after sideband cooling and measuring the temperature of the ion using sideband spectroscopy. Figure 2 shows the gate fidelity as a function of these three heating rates for both single- and two-tone gates. The



FIG. 2. Infidelities due to heating are reduced by moving from a single- to a two-tone MS gate, shown in red and blue, respectively. Both gates are of duration  $\tau = 3.4$  ms. Solid lines are the results of a numerical simulation, and three experimental points are shown for each type of gate where the heating rate has been increased artificially through noise injection. Fidelities are normalized to the fidelity at the single-tone fidelity measured at the lowest heating rate [0.94(2)] to account for other errors [29]. The two-tone gate requires a higher peak Rabi frequency for a given gate duration. Numerical simulation of a faster single-tone gate with this higher Rabi frequency is shown in a dashed black line, showing the two-tone gate is still superior.

solid lines are the results of a numerical simulation of the master equation with appropriate Lindblad operators to model heating, the results of which show good agreement with the theoretical values for fidelity given by Eq. S.7 of the Supplemental Material [16]. The dashed line is the result of a numerical simulation for a faster single-tone gate at a higher power, as defined by the peak Rabi frequency used for the two-tone gate, and demonstrates that two-tone gates still exhibit lower error due to heating. No increase in fidelity is observed for the two-tone gate at no induced heating compared to the single-tone gate due to the small contribution to overall infidelity from heating, smaller than the measurement uncertainty. The measured infidelity at no induced heating is thought to be largely a result of dephasing and depolarizing, and parameter mis-set primarily of the form  $\Delta_b \neq \Delta_r$ , where  $\Delta_r$  and  $\Delta_b$  are the detuning errors on each sideband [see Fig. 1(a)]. Methods to protect against this error exist [28], and combining these with MTMS techniques may offer a solution.

In order to demonstrate robustness to symmetric detuning errors, a symmetric detuning error of up to  $\pm 0.2\delta$  was added to the nominal zero error detuning [30]. Results are shown in Fig. 3, where again solid lines show the result of numerical simulation. A clear consistency between simulation and experimental results can be seen, demonstrating strong protection against both heating and detuning errors obtained by using a two-tone rather than the standard single-tone MS gate.

Since the symmetric detuning error for multitone gates no longer exhibits any dependence on the initial mean



FIG. 3. The effect of symmetric detuning error is significantly reduced by moving to two tones, shown here for a gate duration of  $\tau = 3.4$  ms. The experimental fidelities for nonzero nominal detuning errors are calculated with respect to the Bell state defined by zero nominal detuning, to account for any phase shift induced by the error. Solid lines are from numerical simulations, but with an offset applied to detuning error to account for any error in determining the trap frequency. Experimentally determined fidelities are normalized to the single-tone fidelity with zero nominal detuning error [0.96(2)] to account for other infidelities. The symmetric detuning offset was fitted using the single-tone theory curve to account for the uncertainty in the initial setting of experimental parameters.

excitation of the motional mode of the ions to first order in  $\Delta/\delta$ , this also opens up the possibility of performing gates at higher  $\bar{n}$ , which can, e.g., be reached by Doppler cooling. A multitone gate of fidelity 0.85(1) has been demonstrated at an initial thermal state with  $\bar{n} = 53(4)$ , compared to a single-tone fidelity of 0.50(5), as shown in Fig. 4. The dominant infidelity of the MTMS gate is expected to be due to detuning errors of the form  $\Delta_r \neq \Delta_b$ , which remain sensitive to  $\bar{n}$ .

We have shown that for a given gate time, the use of a two-tone MS gate instead of a standard single-tone MS gate substantially reduces the effect of motional heating, as well as significantly lowering the sensitivity to symmetric detuning errors. This comes at a cost in terms of resources—the peak power required to drive the gate is 3 times higher, while the average power is  $\frac{5}{3}$  times higher. However, provided heating is a significant source of error, MTMS gates should prove a powerful tool, particularly for large-scale systems required for quantum computing with comparatively low ion heights and potentially noisier and less stable environments [31,32].

In addition, we note that MTMS gates also provide protection against fluctuations in the trap frequency caused by Kerr coupling of the stretch mode to the radial mode [33,34], which is only Doppler cooled, thus alleviating one of the main restrictions on using the stretch mode for two qubit gates. Finally, the use of MTMS gates also acts to reduce off-resonant excitation of the carrier caused by the gate fields compared to a single-tone gate, despite the



FIG. 4. Parity curves at an initial motional mode of  $\bar{n} = 53(4)$  for a single- (red) and two-tone (blue) gate after ions have been only Doppler cooled. A significant improvement in contrast is seen for the two-tone gate, since the dependence of gate infidelity on  $\bar{n}$  to first order in  $\Delta$  is eliminated by the use of multiple tones.

higher peak power. This is due to the lower initial Rabi frequency and the sinusoidal variation in Rabi frequency acting as a natural pulse shaping to reduce this excitation, opening up the potential for performing faster gates.

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*Note added.*—Recently, we have become aware of related work where similar methods were used to make laser-based entangling gates more robust [35].

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- [29] The gate infidelity is primarily due to dephasing and depolarization of the qubits, and parameter mis-sets of the form  $\Delta_r \neq \Delta_b$  caused by difficult-to-characterize Stark shifts. We did not fully compensate errors due to Stark shifts, which are the largest contribution to the infidelity, in order to accelerate acquisition of data, since this work is focused on the mitigation of symmetric detuning and heating-induced errors, rather than realizing a gate of high fidelity.
- [30] Due to ac Stark shift caused by the gate fields causing a symmetric detuning offset, and the difficulty of accurately measuring the carrier Rabi frequency  $\Omega_0$  directly, we have to experimentally determine the correct value of the detuning  $\delta$  for a given gate time  $\tau$ .
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