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Baumol's Climate Disease

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Key words: Structural change, Climate capital, Integrated assessment model, Social cost of carbon, Baumol's cost disease

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Abstract

We investigate optimal carbon abatement in a dynamic general equilibrium climate-economy model with endogenous structural change. By differentiating the production of investment from consumption, we show that social cost of carbon can be conceived as a reduction in physical capital. In addition, we distinguish two final sectors in terms of productivity growth and climate vulnerability. We theoretically show that heterogeneous climate vulnerability results in a climate-induced version of Baumol's cost disease. Further, if climate-vulnerable sectors have high (low) productivity growth, climate impact can either ameliorate (aggravate) the Baumol's cost disease, call for less (more) stringent climate policy. We conclude that carbon abatement should not only factor in unpriced climate capital, but also be tailored to Baumol's cost and climate diseases.

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6 1. Introduction

7 Economic growth may be hampered by a stagnant services sector (Bau-
8 mol, 1967) and by climate change (Nordhaus and Yang, 1996). This pa-
9 per shows that climate change would have a similar effect as Baumol’s cost
10 disease. Optimal greenhouse gas emission reduction should take this into
11 account.

12 The paper can be summarized with three arguments. First, climate prox-
13 ied by temperature rise is an *essential capital ‘bad’* used in economic pro-
14 duction¹. Climate is an *essential* input to economic production. Growing
15 crops requires decent climate conditions including appropriate temperature,
16 humidity, sunshine, etc. White-collar workers in high-tech companies de-
17 mand air-conditioning. A higher temperature is typically found to exert an
18 adverse impact on economic production (Tol, 2018). In this sense, climate is
19 a *‘bad’* capital. Climate is a *stock*. Climate change is driven by the historical
20 accumulation of emissions. Thus, climate embodies similar inter-temporal
21 properties as physical or human capital (Lucas Jr, 1988).

22 Because climate is underpriced, carbon dioxide is overinvested. When
23 climate is recognized as capital bad, emission of carbon dioxide is naturally
24 a disinvestment. In addition, climate is a public good, as climate capital
25 is both *nonrival* and *nonexcludable*. On one hand, like ideas, climate cap-
26 ital is *nonrival*. Once the cost of attaining a lower level of climate capital,
27 *e.g.* temperature, has been incurred, the climate capital can be leveraged
28 repeatedly at no additional costs. One agent’s use of temperature does not
29 affect another agent’s use. Furthermore, climate capital is *nonexcludable*,
30 unlike (patented, trademarked or copyrighted) ideas. Nobody is capable of
31 appropriating the property of climate, whether they are individuals, firms,
32 or countries. No agent can stop another agent from using temperature. This
33 implies that there are endless incentives to invest carbon dioxide emissions in
34 the atmosphere. In plain language, because emitting carbon dioxide is free,

¹There are few precedents for considering climate as capital (Arrow et al., 2004, 2012; Barrage, 2020). See also Weitzman (2016) who viewed environmental quality as a stock of capital. Likewise, one may hence interpret climate capital as the desirability of the climate conditions, which can be represented by a function of temperature. Then, climate capital is a capital good. However, in line with the current literature commonly using temperature in the production function (e.g. Nordhaus, 2017; Golosov et al., 2014; Barrage, 2020), we use temperature here to proxy climate capital directly. This manner may be counterintuitive at first sight, but can provide modelling convenience.

35 profit-maximizing firms do not care whether carbon emissions are contribut-
36 ing to climate change.

37 The second argument is that heterogeneous climate vulnerability between
38 sectors reflects the potential to produce with climate capital, causing the cli-
39 mate version of Baumol’s cost disease—*Baumol’s climate disease* in short.
40 Although climate capital is uniformly acquired, the ability to produce varies
41 between sectors at any level of climate capital. For some sectors, climate
42 capital is by its very nature a core requisite, implying a higher climate vul-
43 nerability. Other economic activities are not fastidious about climate condi-
44 tions. As climate change progresses due to overinvested carbon, the climate
45 vulnerability gap can be expected to widen between these sectors. This divi-
46 sion echoes Baumol (1967) that conceptually differentiated progressive with
47 non-progressive sectors due to their technological structure. If products in
48 sectors are not substitutes, more and more productive factors would flow from
49 progressive to stagnant sectors. Eventually, the overall productivity growth
50 declines as the non-progressive sectors are expanding, notoriously known as
51 Baumol’s cost disease². Likewise, if a sector is progressively damaged by
52 climate change, productive factors are increasingly absorbed into it, render-
53 ing the overall economy more vulnerable to climate change. In effect, higher
54 climate vulnerability is analogous to slower productivity growth, giving rise
55 to Baumol’s climate disease.

56 The third argument is that evaluating climate impact should factor in
57 technology-driven structural change. Baumol’s climate disease recognizes
58 the role of heterogeneous climate vulnerability, but its net effect depends
59 on both technological structure and climate vulnerability. More specifically,
60 climate vulnerability in each sector can be either aggravated or compensated
61 by technological change. If a sector with high climate vulnerability is blessed
62 with high technological growth, climate impact can be less worrisome because
63 the technological structure makes this sector more resilient. On the contrary,
64 if a sector with high climate vulnerability is further depressed by gloomy
65 technological prospects, the relative price of production in this sector will
66 grow even higher. Consequently, Baumol’s cost disease bites harder. In this
67 case, reducing carbon emissions can generate dual benefits including both

²Nordhaus (2008) provides empirical evidence for Baumol’s cost disease. Some recent studies explore Baumol’s cost disease in dynamic growth models, and confirm that the rising price of services relative to goods will slow aggregate productivity growth (Ngai and Pissarides, 2007; Herrendorf et al., 2021).

68 avoided climate damages and moderated cost disease.

69 Although the economics literature on climate impact is burgeoning (e.g.
70 Bakkensen and Barrage, 2018; Carleton et al., 2022; Waldinger, 2022; Cruz
71 and Rossi-Hansberg, 2023; Acemoglu and Rafey, 2023; Tol, 2022, etc.), the
72 conception of climate as capital, to our knowledge, has not been formalized in
73 climate-economy models. The paper makes some progress in this regard. We
74 start with standard properties that naturally come along with identifying cli-
75 mate as a capital. For example, climate capital delivers negative returns, and
76 the marginal return to climate capital is non-decreasing at a higher temper-
77 ature. Besides, nonrival climate capital features decreasing returns to scale.
78 Because climate capital is also nonexcludable, the nonrivalry contributes to
79 the negative climate externality, in contrast to the positive externality in
80 the knowledge capital. Nobel Prize Committee (2018) points out that exter-
81 nalities bridge the contributions of Romer and Nordhaus. Along its route,
82 we emphasize that nonrivalry and nonexcludability of climate capital are the
83 fundamental cause of climate change, and that integrated assessment mod-
84 els should assume non-constant-return-to-scale technology for climate capi-
85 tal in production functions. Moreover, the paper interprets climate damage
86 functions as the ability to produce with climate capital, which can differ in
87 sectors.

88 To shed light on optimal carbon abatement under structural change, this
89 paper then establishes a dynamic general equilibrium climate-economy model
90 with endogenous structural change. The climate-economy linkage stands on
91 the shoulders of Golosov et al. (2014), Nordhaus (2017) and Barrage (2020).
92 Economic production requires energy as essential input, which will generate
93 carbon emissions. Unabated carbon emissions will enter the atmosphere and
94 affect climate capital that is indispensable for economic activities. On the
95 one hand, our model differentiates *two* final production sectors, both of which
96 use physical capital, labor, energy, knowledge and climate as input. In addi-
97 tion, both sectors adopt non-constant-return-to-scale technology when using
98 knowledge and climate for production. Thus, technological growth and cli-
99 mate vulnerability combine to shape the relative price between two sectors.
100 On the other hand, production in two sectors are required for both con-
101 sumption and investment (*two* final expenditures). Therefore, the model is
102 characterized by a *two-by-two* structure. Following Herrendorf et al. (2021),
103 García-Santana et al. (2021) and Buera et al. (2020), we induce structural

104 transformation in both consumption and investment via the price effect³. For
105 both expenditures, the substitution elasticity is less than unity between two
106 final products (Herrendorf et al., 2013, 2021; García-Santana et al., 2021).
107 Hence, the comparative scarcity between two products determines their rel-
108 ative price, leading up to structural change. The results of the model are
109 generalized as follows.

110 First, we provide a novel representation of the social cost of carbon based
111 on investment. By differentiating the production of investment and consump-
112 tion, we find that the trade-off between abatement costs and avoided climate
113 damage is based on investment rather than consumption. This result theo-
114 retically supports that climate is a capital bad. Thus, the real cost of carbon
115 can be conceived as a drag on physical capital. Existing studies usually de-
116 fine the social cost of carbon as the consumption loss due to an additional
117 tonne of CO₂ (Nordhaus, 2014; Golosov et al., 2014; Barrage, 2020). In one-
118 sector growth model, economic production is utilized for either consumption
119 or investment without differences. Thus, investment-equivalent social cost of
120 carbon is identical to consumption-equivalent social cost of carbon therein.
121 Social cost of carbon denominated in terms of consumption has straightfor-
122 ward welfare implications because consumption is a direct measure of welfare,
123 unlike investment. By comparison, Arrow et al. (2012) adopts social cost of
124 carbon to approximate the change in environmental capital, implying a cost
125 in investment. In their language, the social cost of carbon denominated by
126 investment reflects the cost in wealth instead of directly in income, and hence
127 also has welfare implications owing to its close relevance to sustainability. It
128 should be noted that the choice of numeraire only influences the numerical
129 value of social cost of carbon, whereas optimal allocation is immune to ei-
130 ther choice. Investment-equivalent social cost of carbon is associated with
131 consumption-equivalent social cost of carbon by the relative price of invest-
132 ment to consumption.

133 Second, we theoretically demonstrate how climate change can influence
134 Baumol’s cost disease. For one thing, we assume the Cobb-Douglas func-
135 tions in two sectors with the same factor intensity. For another, we allow
136 for different technological growth and climate vulnerability in both sectors.
137 Absent different technological growths, the relative price in the more climate-

³The income effect is the other important force in incurring structural change (Buera and Kaboski, 2009; Boppart, 2014; Comin et al., 2021; Alder et al., 2022).

138 vulnerable sector will increase as climate change proceeds, because produc-
139 tion in this sector is comparatively scarcer than that of less climate-vulnerable
140 sector, exacerbating the climate impact via Baumol’s climate disease. Ac-
141 counting for heterogeneous technological growth, the relative price between
142 two sectors is pinned down by the relative technological growth combined
143 with relative climate vulnerability. Suppose that the impact of technological
144 growth dominates that of climate vulnerability. The relative price between
145 two sectors will increase further when the more susceptible sector is also ex-
146 experiencing slower technological growth. That is, climate change exacerbates
147 the Baumol’s cost disease. By comparison, when the more susceptible sector
148 has high productivity growth, the relative price will still go up, but to an
149 extent less than absent climate impact. In other words, although climate
150 change takes a toll in both sectors, it ameliorates the Baumol’s cost disease.

151 Third, we quantify the model. For expositional convenience, we divide
152 the economy into goods and services. Dividing the economy into goods and
153 services is not uncommon in the structural change literature (e.g. Moro,
154 2015; Leon-Ledesma and Moro, 2020; Herrendorf et al., 2021), motivated
155 by the observed slower technological growth in services. In addition, we
156 find some preliminary empirical evidence that services are less susceptible to
157 climate change than goods. In line with the literature, we assume that the
158 productivity growth in the goods sector is three times that in the services
159 sector. Absent climate damage, the capital stock in 2100 is set identical to
160 that in the DICE model for comparability. We adopt the damage function
161 from DICE, assuming that the relative damage level in the goods sector is
162 two times higher than in services. Using the data from World Bank, we pin
163 down the factor shares used in each sector in the initial period.

164 Fourth, our numerical results validate that Baumol’s cost disease is an
165 important consideration for carbon abatement policy. When two sectors are
166 only different in climate vulnerability, capital stock is reduced by 12.34%
167 in 2100 and 19.37% in 2150, compared to a decrease of 11.25% and 17.47%
168 under homogeneous climate vulnerability. Thus, Baumol’s climate disease
169 aggravates aggregate climate impact. As a consequence, a more stringent
170 climate policy is required to achieve the optimal allocation, which achieves
171 the net-zero carbon emission in 2095, earlier than in 2100 for homogeneous
172 climate vulnerability. When also accounting for differentiated productivity
173 growth in the baseline model, there is little difference for capital stock be-
174 tween heterogeneous or homogeneous climate vulnerability. Moreover, as
175 consumption responds to climate with lags, consumption is even improved

176 under heterogeneous climate vulnerability in the considered periods. This is
177 because the expanding services sector is less vulnerable to climate change, or
178 alternatively, the goods sector that is more vulnerable enjoys a higher pro-
179 ductivity growth, showing higher resilience to climate change. A less strict
180 abatement policy is required for optimal allocation, putting off 10 years for
181 achieving net-zero emissions. Furthermore, we consider a counterfactual sce-
182 nario where the services sector is assumed to be more climate-vulnerable.
183 Quantitative results come to that the climate damage on capital stock will
184 be aggravated by a further loss of 9.20 percentage points if climate change
185 increases the relative price of services, *i.e.* the more severe Baumol's cost
186 disease. Accordingly, net-zero emissions are required to be achieved twenty
187 years earlier.

188 In addition, we quantify two definitions of the social cost of carbon. In
189 the presence of optimal abatement, the social cost of carbon at 2100 stands
190 for an investment loss of \$254 per tone of CO₂, and a consumption loss of
191 \$182 per tone of CO₂. Compared to investment, consumption is composed
192 of a higher ratio of services. As the relative price of services is climbing
193 over time, so will the price of consumption relative to investment. Given a
194 numeraire with a higher price, consumption-equivalent social cost of carbon
195 is lower than investment-equivalent one. Moreover, we find that a lower
196 social time preference rate will generate a larger gap between the values of
197 two definitions.

198 Although we only simulate goods and services in the model, our results
199 imply that climate policy should be tailored to Baumol's joint cost-and-
200 climate disease. The more sectors are there in the economy with low produc-
201 tivity growth and high climate vulnerability, *i.e.* the more acute the Baumol's
202 joint cost-and-climate disease, the stronger incentives to reduce the carbon
203 emissions. Otherwise, the long-run economy growth would be plagued by
204 both climate change and exacerbated Baumol's cost disease. In addition, the
205 social planner need increase adaptation investment into any sector with both
206 high climate vulnerability and low productivity growth. Thus, our paper
207 has policy implications for both abatement and adaptation under structural
208 change.

209 This paper relates to the current literature in the following ways. First,
210 existing literature typically denominates the social cost of carbon in terms
211 of consumption (Nordhaus, 2014; Golosov et al., 2014), we propose an al-
212 ternative definition in term of investment. In so doing, we show that social
213 cost of carbon is a drag on productive capital rather than directly on con-

214 sumption. We also demonstrate two definitions of social cost of carbon can
215 be bridged by the relative price of investment to consumption. Second, the
216 paper is relevant to studies on climate damages. Casey et al. (2021) as-
217 sume that the climate system evolves exogenously, and analyzes the climate
218 damages on consumption and investment with the focus on heterogeneous
219 damages between sectors. Our study is consistent with theirs in finding that
220 heterogeneous climate vulnerability will exacerbate aggregate damage level,
221 which could be explained by the less than unity substitution elasticity be-
222 tween each product in producing investment and consumption. This paper,
223 however, differs from theirs in that we focus on the background of structural
224 change. Baumol’s cost and climate diseases are critical factors in determin-
225 ing the realized impact of climate change. Third, the paper falls within the
226 broad category of structural change economics (Herrendorf et al., 2014), and
227 we add that climate vulnerability is also complementary to incurring the
228 price effect.

229 The remainder of the paper is organized as follows. Section 2 formalize
230 climate as a capital. Section 3 establishes a climate-economy model and
231 theoretically analyzes the incentives to disinvest into climate capital. Section
232 4 introduces the calibration process. Section 5 discusses the quantitative
233 results. Some sensitivity analyses and extensions are included in Section 6,
234 and Section 7 concludes the paper.

235 **2. Climate capital in production function**

236 This section discusses several fundamental properties associated with cli-
237 mate capital, which have not been formalized previously. Where necessary,
238 we compare climate capital with other common factors in production. In
239 so doing, we are able to interpret the cause of climate change from the per-
240 spective of investment. In addition, we note the link between climate capital
241 and climate damage function that is commonly used in climate economics
242 literature.

243 Temperature change T_t is considered as an appropriate proxy for climate
244 capital, consistent with extant studies (Barrage and Nordhaus, 2023; Golosov
245 et al., 2014; Cruz and Rossi-Hansberg, 2023). In addition to climate capital,
246 economic production at period t also requires physical capital K_t , labor L_t ,
247 ideas A_t , and energy E_t .

$$Y_t = F(A_t, T_t, K_t, L_t, E_t) \quad (1)$$

248 where F represents some technology to utilize these factors in production.
249 The last argument energy E_t can be either fossil fuels that will emit carbon
250 dioxide or renewable energy with no carbon emissions.

251 *2.1. Negative and increasing returns*

252 Unlike other factors, climate represented by global mean temperature
253 change is a bad capital. More input of other factors (*i.e.* physical capi-
254 tal, human capital, energy and ideas) generate more revenues, whereas an
255 increase in temperature causes economic losses:

$$\frac{\partial F}{\partial T_t} < 0 \tag{2}$$

256 Moreover, as the temperature increases further, the marginal returns to cli-
257 mate capital is increasing:

$$\frac{\partial^2 F}{\partial^2 T_t} > 0 \tag{3}$$

258 Increasing returns to climate capital captures both the beliefs (Barrage and
259 Nordhaus, 2023; Weitzman, 2010; Pindyck, 2021) and some empirical evi-
260 dence (Burke et al., 2015; Newell et al., 2021) that climate impact is exacer-
261 bated at a higher temperature.

262 *2.2. Decreasing returns to scale*

263 In nature, climate capital is a *public good*, because it is both nonrival and
264 nonexcludable. Consequently, climate capital is overinvested, giving rise to
265 global warming.

266 Climate capital is nonrival. An individual's use of climate capital does not
267 preclude others from using climate capital. Once climate capital is produced
268 (represented by global temperature change), all firms use it for economic pro-
269 duction without paying for additional costs. When global mean temperature
270 rises, an enduring heat wave may ensue in an African village, devastating the
271 harvests of all peasants. One peasant's adversity cannot lower the possibility
272 or extent of another peasant in the same village. In Singapore, a coastal
273 high-tech company is simultaneously plagued by the sea-level rise that floods
274 the working office due to the same climate capital, *i.e.* global mean temper-
275 ature change. While the sea level is rising in Singapore, miserable peasants
276 find no reasons to believe that flooding makes global temperature increase
277 or decrease, nor will the company think the heat wave in Africa will cool

278 down the global suddenly. Climate capital, once produced, can be enjoyed
 279 by everyone and hence is not scare. However, good climate capital is scare in
 280 that, for example, there is some unknown level of global temperature change
 281 leading up to maximum global economic production, *ceteris paribus*.

282 Nonrivalry of climate capital implies that production is characterized by
 283 decreasing returns to scale. The standard replication argument is valid for
 284 physical capital, human capital and energy, but not for ideas and climate
 285 capital. Romer (1986, 1990) has illuminated that ideas are nonrival and
 286 consequently that economic production features increasing returns to scale.
 287 Because climate is a bad capital, climate capital is characterized by decreas-
 288 ing returns to scale. In other words, for any $\lambda > 1$, we have:

$$\begin{aligned}
 F(A_t, T_t, \lambda K_t, \lambda L_t, \lambda E_t) &= \lambda F(A_t, T_t, K_t, L_t, E_t) \\
 F(\lambda A_t, T_t, \lambda K_t, \lambda L_t, \lambda E_t) &> \lambda F(A_t, T_t, K_t, L_t, E_t) \\
 F(A_t, \lambda T_t, \lambda K_t, \lambda L_t, \lambda E_t) &< \lambda F(A_t, T_t, K_t, L_t, E_t)
 \end{aligned}
 \tag{4}$$

289 Climate capital is also nonexcludable, leading up to overinvested carbon.
 290 Compared to knowledge capital that can be partially excludable in the pres-
 291 ence of patents, the property of climate capital cannot be appropriated in
 292 reality. Suppose that a firm reduces one unit of carbon investment into cli-
 293 mate capital and shoulders the associated abatement costs. Because climate
 294 capital is not excludable, all firms in the economy can benefit from this one
 295 unit of reduced carbon that lowers the level of climate capital. Thus, the
 296 abatement costs for reduced carbon cannot be compensated for by private
 297 revenues. In the market, when the social price of carbon is not defined, no
 298 firm is motivated to disinvest carbon into climate capital.

299 *2.3. Climate capital and damage function*

300 Although climate capital proxied by global mean temperature is uniform
 301 to everybody, the ability to produce with climate capital can be quite dif-
 302 ferent. In other words, climate impact is heterogeneous. This can be ex-
 303 plained by geographic endowments, adaptation technology, industry struc-
 304 ture, etc. In existing literature (e.g.: Barrage and Nordhaus, 2023; Golosov
 305 et al., 2014; Barrage, 2020; Cruz and Rossi-Hansberg, 2023), the damage
 306 function pioneered by (Nordhaus, 1992) is commonly leveraged to reflect the
 307 productivity of climate capital. Admittedly, the damage function is among
 308 the most uncertain parts in climate-economy models in terms of both forms
 309 and parameters (Pindyck, 2021). The paper makes no efforts to determine

310 any well-suited damage function. Instead, as we will see below, the analysis
311 only requires that climate damage functions should be sector-specific so as
312 to reflect the differentiated productivity of climate capital between sectors.

313 **3. Model and theory**

314 This section establishes a dynamic climate-economy model with endoge-
315 nous structural change. The climate-economy structure is borrowed from
316 Nordhaus (2017), Golosov et al. (2014) and Barrage (2020). The economic
317 module is augmented with a two-by-two structure. On the one hand, we al-
318 low for two final production sectors with heterogeneous productivity growth
319 rate and climate vulnerability, both of which can affect the relative price of
320 products in two sectors⁴. On the other hand, following Greenwood et al.
321 (1997), Herrendorf et al. (2014) and Foerster et al. (2022), we differentiate
322 two final expenditures of economic production—consumption and investment
323 in terms of their compositions of final products. Thus, structural change can
324 take place within both consumption and investment when the price in one
325 sector changes relative to the other. We start from the competitive market
326 and show its equivalence to social planner problem by introducing a carbon
327 tax.

328 Given the established model, we first theoretically show how to achieve
329 the optimal allocation in the presence of climate externality. This result con-
330 stitutes the fundamental incentive for addressing climate change—unpriced
331 climate capital and overinvested carbon. Then, we show the relative price
332 between two products, which can be perceived as the acuteness of the Bau-
333 mol’s cost disease. Reducing carbon changes the relative price, and hence
334 becomes another important consideration in optimal carbon abatement de-
335 cision.

336 *3.1. Households*

337 The economy accommodates an infinitely-lived, representative household
338 whose lifetime utility is determined by:

$$U_0 \equiv \sum_{t=0}^{\infty} \beta^t U(C_t) \quad (5)$$

⁴Our model can be easily extended to a multi-sector case.

339 where β denotes the social time of preference and C_t market consumption
 340 at period t . In fact, the household's utility can also be affected directly
 341 by climate change. For example, it can influence amenities, biodiversity
 342 or health conditions that households value⁵. Since the paper focuses on
 343 economic dynamics, we abstract from these possibilities.

344 The consumption bundle is composed of two different products:

$$C_t = F_C(C_{1t}, C_{2t}) \quad (6)$$

345 where C_{it} stands for consumption of product $i \in \{1, 2\}$ respectively. F_C
 346 captures the household's preference for each product, and can be regarded
 347 as a costless technology aggregating both consumption.

348 The representative household should satisfy its budget constraint in each
 349 period:

$$p_{1t}C_{1t} + p_{2t}C_{2t} + K_{t+1} \leq w_t L_t + (1 + r_t - \delta)K_t + \Pi_t + Tran_t \quad (7)$$

350 where K_{t+1} is the capital holdings at time $t+1$, w_t the wage rate, L_t the labor
 351 supply, r_t the rental rate of capital, δ the capital depreciation rate, Π_t the
 352 dividends from the energy sector, $Tran_t$ the lump-sum transfer of carbon tax
 353 levied by the government. We set investment as the numeraire, normalizing
 354 its price to one in each period, and define p_{it} as the price of product i .

355 Thus, the household's first-order condition requires that saving decisions
 356 and allocations of goods and services in consumption must satisfy:

$$\frac{U_{C_{1t}}/p_{1t}}{U_{C_{1,t+1}}/p_{1,t+1}} = \frac{U_{C_{2t}}/p_{2t}}{U_{C_{2,t+1}}/p_{2,t+1}} = \beta(1 + r_t - \delta) \quad (8)$$

357 where U_{cit} represents the partial derivative of instantaneous utility function
 358 with respect to consumption i at time t . This equation demonstrates that,
 359 between two subsequent periods, the representative household will equate
 360 the price-adjusted marginal rates of substitution in each consumption to the
 361 return rate on saving.

⁵This consideration can be represented by either introducing a climate variable such as temperature rise into the utility function (Barrage, 2020) or considering the climate impact on non-market goods (Tol, 1994; Sterner and Persson, 2008; Drupp and Hänsel, 2021).

362 *3.2. Two final production sectors*

363 There are two final sectors whose production functions follow from Eq.(1).
 364 Further, each sector $i \in \{1, 2\}$ adopts a constant-returns-to-scale technology
 365 \tilde{F} to combine physical capital, labor and energy, and satisfies the Inada con-
 366 ditions. By comparison, both climate capital and knowledge capital feature
 367 non-constant returns to scale, represented by \hat{F} . Thus, we have:

$$\begin{aligned} Y_{1t} &= F_1(A_{1t}, T_t, K_{1t}, L_{1t}, E_{1t}) \\ &= \hat{F}_1(A_{1t}, T_t) \tilde{F}_1(K_{1t}, L_{1t}, E_{1t}) \end{aligned} \quad (9)$$

$$\begin{aligned} Y_{2t} &= F_2(A_{2t}, T_t, K_{2t}, L_{2t}, E_{2t}) \\ &= \hat{F}_2(A_{2t}, T_t) \tilde{F}_2(K_{2t}, L_{2t}, E_{2t}) \end{aligned} \quad (10)$$

368 Note that climate capital is uniformly utilized in both sectors, whereas other
 369 factors and production technologies can be sector-specific.

370 In a competitive market, profit-maximizing firms in both sectors should
 371 equate their marginal products to their prices:

$$\begin{aligned} p_{1t}F_{1Lt} &= p_{2t}F_{2Lt} = w_t \\ p_{1t}F_{1Kt} &= p_{2t}F_{2Kt} = r_t \\ p_{1t}F_{1Et} &= p_{2t}F_{2Et} = p_{Et} \end{aligned} \quad (11)$$

372 where F_{ijt} represents the partial derivative of sector i production function
 373 with respect to rival input $j \in \{K, L, E\}$, and p_{Et} denotes the energy price.

374 In addition, production in both sectors can be utilized for either con-
 375 sumption or investment such that:

$$\begin{aligned} Y_{1t} &= C_{1t} + I_{1t} \\ Y_{2t} &= C_{2t} + I_{2t} \end{aligned} \quad (12)$$

376 where I_{it} is the output from sector i used for investment.

377 Total nominal final output can thus be defined as:

$$Y_t = p_{1t}Y_{1t} + p_{2t}Y_{2t} \quad (13)$$

378 *3.3. Investment production sector*

379 In the economy, there is also an intermediate investment sector that
 380 adopts a constant-to-scale technology and combines the production from two
 381 final sectors to produce final investment:

$$I_t = F_I(A_{It}, I_{1t}, I_{2t}) \quad (14)$$

382 where A_{I_t} denotes an exogenous investment-specific technical change to pro-
 383 duce aggregate investment. We do not allow for a direct climate impact on
 384 investment production in Eq.(14). However, temperature change indirectly
 385 influences investment because as it reduces final products supplied to produce
 386 investment⁶.

387 3.4. Energy sector

388 Using both capital K_{Et} and labor L_{Et} , the intermediate energy sector pro-
 389 duces with a constant-return-to-scale technology. Hence, energy production
 390 is given by:

$$E_t = A_{Et} \tilde{F}_E(K_{Et}, L_{Et}) \quad (15)$$

391 Energy production is allocated to two final sectors as input. Following Bar-
 392 rage (2020), we assume that carbon-based energy can be unlimitedly supplied
 393 and therefore incurs zero Hotelling rents. Climate capital is in reality also
 394 used for energy production, but we make simplifications here considering that
 395 the energy sector accounts for a relatively small proportion in the economy.

396 Energy firms can choose to produce a fraction μ_t of energy with some
 397 zero-emission technologies at an additional abatement investment $\Theta_t(\mu_t E_t)$.
 398 For each unit of emission, firms are obliged to pay the carbon tax. Thus, the
 399 profits of energy producers are:

$$\Pi_t = p_{Et} E_t - [(1 - \mu_t) E_t] \tau_{Et} - w_t L_{Et} - r_t K_{Et} - \Theta_t(\mu_t E_t) \quad (16)$$

400 where τ_{Et} denotes the carbon tax on uncontrolled carbon emissions from two
 401 final sectors $\{E_i^{unc}\}_{i=0}^t = \{(1 - \mu_t)(E_{1i} + E_{2i})\}_{i=0}^t$. We only consider an aggre-
 402 gate carbon control rate μ_t , and we discuss the implications of differentiated
 403 control rates in Section 6.

⁶Allowing for the climate impact on investment explicitly will exacerbate the climate impact on growth rate. Fankhauser and Tol (2005) and Dietz and Stern (2015) show that such growth effect can be embodied in the climate impact on capital depreciation explicitly, analogous to modelling a climate impact on investment production. A climate impact on economic growth will acutely exacerbate economic losses compared to its frontier, whereas the level effect is more modest (Pindyck, 2021; Cai et al., 2023). However, there still exist some intellectual gaps between modelling practices and empirical evidence to support the growth effect of climate change (Dell et al., 2012; Burke et al., 2015; Newell et al., 2021). Further, Herrendorf et al. (2021) and García-Santana et al. (2021) find the exogenous investment-specific technical change plays a very limited role in driving long-run growth. Given all these, we only implicitly account for the climate impact on investment.

404 Again, in the competitive market, energy producers equate the marginal
 405 products of each input to their corresponding prices:

$$\begin{aligned} (p_{Et} - \tau_{Et})F_{Elt} &= w_t \\ (p_{Et} - \tau_{Et})F_{Ekt} &= r_t \end{aligned} \quad (17)$$

406 Moreover, the formulation in Eq.(16) implies that profit-maximizing en-
 407 ergy producers are incentivised to equate the marginal benefit of avoided tax
 408 payment per unit of uncontrolled carbon emissions to marginal abatement
 409 costs:

$$\tau_{Et} = \Theta'_t(\mu_t E_t) \quad (18)$$

410 In each period, the productive factors are freely mobile across sectors:

$$\begin{aligned} L_t &= L_{1t} + L_{2t} + L_{Et} \\ K_t &= K_{1t} + K_{2t} + K_{Et} \\ E_t &= E_{1t} + E_{2t} \end{aligned} \quad (19)$$

411 where aggregate labor force L_t is exogenously given at each period.

412 3.5. Carbon cycle and climate

413 We follow the convention of climate economics literature in viewing tem-
 414 perature as a sufficient proxy for climate change. Specifically, atmospheric
 415 temperature change T_t at period t is determined by the historical path of
 416 carbon emissions after control $\{E_i^{unc}\}_{i=0}^t = \{(1 - \mu_i)(E_{1i} + E_{2i})\}_{i=0}^t$, initial
 417 climate conditions \mathbf{M}_0 including atmospheric carbon concentrations, deep
 418 ocean temperatures, etc., and exogenous shifters $\{\boldsymbol{\eta}_i\}_{i=0}^t$ such as land-based
 419 emissions:

$$T_t = \Phi(\mathbf{M}_0, E_0^{unc}, E_1^{unc}, \dots, E_t^{unc}, \boldsymbol{\eta}_0, \dots, \boldsymbol{\eta}_t) \quad (20)$$

420 where $\frac{\partial T_{t+j}}{\partial E_t^{unc}}$ holds for $\forall t, j \geq 0$. The very nature that climate change, proxied
 421 by T_t , hinges on the *stock* of carbon emissions in the atmosphere hints that
 422 climate is a capital. Note that temperature is not exclusively dictated by
 423 current-period carbon emission, which is a *flow* variable.

424 3.6. Competitive equilibrium

425 Now we can present the standard definition of competitive equilibrium in
426 the economy, augmented with the climate system.

427 **Definition 1.** A competitive equilibrium consists of a sequence of exogenously-
428 given productivity $\{A_{1t}, A_{2t}, A_{It}, A_{Et}\}_{t=0}^{\infty}$, a series of allocations $\{C_{1t}, C_{2t}, I_{1t},$
429 $I_{2t}, L_{1t}, L_{2t}, L_{Et}, K_{1,t+1}, K_{2,t+1}, K_{E,t+1}, E_{1t}, E_{2t}, \mu_t, T_t\}_{t=0}^{\infty}$, a set of prices $\{r_t,$
430 $w_t, p_{1t}, p_{2t}, p_{Et}, \}_{t=0}^{\infty}$ and a series of policies $\{\tau_{Et}\}_{t=0}^{\infty}$ such that in each period,
431 given prices and policies:

- 432 (i) the household solves the utility-maximizing problem subject to the budget
433 constraint,
434 (ii) firms in two final production sectors and two intermediate sectors (energy
435 and investment) maximize profits,
436 (iii) temperature changes in line with the carbon cycle constraint, and
437 (iv) markets clear.

438 By virtue of the above definition, we now demonstrate what a first-best
439 carbon tax is needed to decentralize the optimal allocation in the competitive
440 equilibrium:

441 **Proposition 1.** The allocations $\{C_{1t}, C_{2t}, I_{1t}, I_{2t}, L_{1t}, L_{2t}, L_{Et}, K_{1,t+1}, K_{2,t+1},$
442 $K_{E,t+1}, E_{1t}, E_{2t}, \mu_t, T_t\}_{t=0}^{\infty}$, along with initial capital stock K_0 , initial carbon
443 concentrations \mathbf{M}_0 , and climate shifters $\{\boldsymbol{\eta}_i\}_{i=0}^t$ in a competitive equilibrium
444 satisfy:

$$F_1(A_{1t}, T_t, L_{1t}, K_{1t}, E_{1t}) \geq C_{1t} + I_{1t} \quad (21)$$

$$F_2(A_{2t}, T_t, L_{2t}, K_{2t}, E_{2t}) \geq C_{2t} + I_{2t} \quad (22)$$

$$F_C(C_{1t}, C_{2t}) \geq C_t \quad (23)$$

$$F_I(A_{It}, I_{1t}, I_{2t}) + (1 - \delta)K_t \geq K_{t+1} + \Theta_t(\mu_t E_t) \quad (24)$$

$$E_t \leq A_{Et} F_E(K_{Et}, L_{Et}) \quad (25)$$

$$T_t \geq \Phi(\mathbf{M}_0, (1 - \mu_0)(E_{10} + E_{20}), \dots, (1 - \mu_t)(E_{1t} + E_{2t}), \boldsymbol{\eta}_0, \dots, \boldsymbol{\eta}_t) \quad (26)$$

$$L_t \geq L_{1t} + L_{2t} + L_{Et} \quad (27)$$

$$K_t \geq K_{1t} + K_{2t} + K_{Et} \quad (28)$$

$$E_t \geq E_{1t} + E_{2t} \quad (29)$$

445 Therefore, given an allocation that maximizes the household's net present
446 utility Eq.(5) and simultaneously satisfies constraints Eq.(21)-Eq.(29), letting

447 λ_{It} the Lagrange multiplier on the capital accumulation constraint Eq.(24),
 448 one can formulate a carbon tax equal to:

$$\begin{aligned}
 \tau_{Et} &= \underbrace{\Theta'_t}_{\text{Marginal abatement cost}} \\
 &= \underbrace{F_{I1t}F_{1Et} - \frac{F_{I1t}F_{1lt}}{F_{Elt}}}_{\text{Marginal product of energy}} = \underbrace{F_{I2t}F_{2Et} - \frac{F_{I2t}F_{2lt}}{F_{Elt}}}_{\text{Marginal benefit of carbon abatement}} \\
 &= (-1) \sum_{j=0}^{\infty} \beta^j \left(\underbrace{\frac{U_{C,t+j}}{\lambda_{It}} \frac{\partial C_{t+j}}{\partial C_{1,t+j}} \frac{\partial Y_{1,t+j}}{\partial T_{t+j}} \frac{\partial T_{t+j}}{\partial E_t^{unc}}}_{\text{Impacts on sector 1}} + \underbrace{\frac{U_{C,t+j}}{\lambda_{It}} \frac{\partial C_{t+j}}{\partial C_{2,t+j}} \frac{\partial Y_{2,t+j}}{\partial T_{t+j}} \frac{\partial T_{t+j}}{\partial E_t^{unc}}}_{\text{Impacts on sector 2}} \right) \quad (30)
 \end{aligned}$$

449 such that the competitive market can achieve the optimal allocation as in the
 450 social planner problem, and the discounting of output damages in period t is
 451 governed by:

$$\frac{\lambda_{It}}{\beta \lambda_{I,t+1}} = F_{Ig,t+1} F_{gk,t+1} + (1 - \delta) = F_{Is,t+1} F_{sk,t+1} + (1 - \delta) \quad (31)$$

452 Proof: See Appendix A. Eq.(30) describes the classic wisdom (Baumol,
 453 1972; Golosov et al., 2014) to address climate (environmental) externality.
 454 The optimal allocation requires **equating** marginal product of carbon-based
 455 energy **to** marginal abatement costs, **and also to** current-value marginal
 456 benefit of carbon abatement, namely climate impact due to an additional tone
 457 of carbon emission times minus one. To decentralize such optimal allocation,
 458 the global planner needs to levy a Pigouvian tax equal to Θ'_t .

459 However, the theoretical finding deviates from previous studies primar-
 460 ily in establishing investment, rather than consumption, as the core metric
 461 in the trade-off. Marginal abatement cost is by construction denominated
 462 by investment as previously introduced. The marginal product of energy is
 463 represented by how much final investment per unit of energy can produce
 464 net of the opportunity cost in energy production. The marginal impact of
 465 carbon emission is also denominated in terms of investment. Under optimal
 466 allocation, Pigouvian tax is numerically equal to the social cost of carbon.

467 Social cost of carbon is conventionally defined as the shadow price of car-
 468 bon measured by the utility of per unit of consumption (Nordhaus, 2014;
 469 Golosov et al., 2014; Barrage, 2020)⁷. Thus, the common definition reflects
 470 the amount of consumption one would like to sacrifice today in order to
 471 reduce an additional unit of welfare-reducing emissions.

472 Motivated by this result, we provide an alternative definition for social
 473 cost of carbon, *i.e.* investment loss due to an additional tone of carbon emis-
 474 sion. Recall in Section 2 that climate is a capital and carbon is an investment.
 475 If economic production is not utilized for the investment in abatement tech-
 476 nology, it can be leveraged to accumulate physical capital. However, if no
 477 abatement technology is adopted, carbon will be overinvested. Eventually,
 478 the global mean temperature rises, generating an impact equivalent to a loss
 479 in physical capital. The pigouvian tax in Eq.(30) seeks an optimal invest-
 480 ment bundle that guarantees the equalized marginal product of each kind
 481 of investment. Therefore, the real cost of carbon is on investment rather
 482 than consumption, and climate change is due to disinvestment instead of
 483 malconsumption.

484 In fact, two definitions of social cost of carbon deviate only when invest-
 485 ment and consumption are produced in different ways. Denoting the marginal
 486 value of investment λ_{I_t} and that of consumption λ_{C_t} , one can establish the
 487 following identity:

$$\frac{\lambda_{I_t}}{\lambda_{C_t}} = \frac{F_{C1t}}{F_{I1t}} = \frac{F_{C2t}}{F_{I2t}} \quad (32)$$

488 The marginal value of investment relative to that of consumption is gov-
 489 erned by how each final product is transformed into between consumption
 490 and investment. In one-sector climate-economy models without any other
 491 distortions like Nordhaus (2014) and Golosov et al. (2014), a unit of final pro-
 492 duction can be either consumed or invested without any differences. Thus,
 493 both F_{C1t}/F_{I1t} and F_{C2t}/F_{I2t} are cancelled out, and two definitions of social
 494 cost of carbon are numerically identical.

495 Although social cost of carbon as a price is different, optimal allocation
 496 is fixed regardless of any numeraire. In addition, both definitions have their

⁷Consumption-equivalent social cost of carbon can be generalized as $SCC_{CE} = \frac{\partial U}{\partial E_t} / \frac{\partial U}{\partial C_t}$, while investment-equivalent social cost of carbon is formulated as $SCC_{IE} = \frac{\partial U}{\partial E_t} / \frac{\partial U}{\partial I_t}$.

497 strengths and weaknesses. Consumption-equivalent social cost of carbon does
 498 not reflect the very nature that climate change is a drag on investment, but
 499 has convenient welfare implications because it demonstrates the consumption
 500 loss due to an additional tone of carbon emission. In comparison, investment-
 501 equivalent social cost of carbon cannot provide direct welfare interpretations.
 502 After all, people care consumption rather than investment⁸.

503 3.7. Drivers of structural change

504 We induce structural change within both consumption and investment
 505 through the price effect⁹. The price effect reflects that the value-added share
 506 of a certain product can also increase when its relative price goes up. We
 507 assume two final production sectors are only different in technological growth
 508 rate and climate vulnerability. Following Herrendorf et al. (2014), the pro-
 509 duction functions in both sectors adopt the Cobb-Douglas form with identical
 510 factor intensity¹⁰:

$$\begin{aligned}
 Y_{1t} &= \hat{F}_1(A_{1t}, T_t) K_{1t}^\alpha L_{1t}^{1-\alpha-\nu} E_{1t}^\nu \\
 Y_{2t} &= \hat{F}_2(A_{2t}, T_t) K_{2t}^\alpha L_{2t}^{1-\alpha-\nu} E_{2t}^\nu
 \end{aligned}
 \tag{33}$$

511 where how climate capital interacts with knowledge capital in the production
 512 functions remains undefined without loss of generality.

513 In addition, both consumption and investment functions are assumed to

⁸Having said that, investment-equivalent social cost of carbon can be utilized to calculate genuine saving (or comprehensive wealth) for measuring sustainable development (Arrow et al., 2004, 2012).

⁹Existing studies generalize two broad forces behind structural change—the income effect and the price effect. The income effect captures that as income increases, so will the value-added share of products with a higher income elasticity.

¹⁰The price effect can also occur when sectors differ in capital intensity or the substitution elasticity between reproducible factors (Acemoglu and Guerrieri, 2008; Alvarez-Cuadrado et al., 2017). We abstract from these two possibilities for two reasons. First, Herrendorf et al. (2015) showed that sectors with different productivity growths alone can fit well the post-war structural change in the United States. Second, the Baumol’s cost disease, which is the focus of this paper, is concerned with the technological structure behind each sector.

514 be the CES form:

$$C_t = \left(\omega_c^{\frac{1}{\epsilon_c}} C_{1t}^{\frac{\epsilon_c-1}{\epsilon_c}} + (1 - \omega_c)^{\frac{1}{\epsilon_c}} C_{2t}^{\frac{\epsilon_c-1}{\epsilon_c}} \right)^{\frac{\epsilon_c}{\epsilon_c-1}} \quad (34)$$

$$I_t = A_{It} \left(\omega_I^{\frac{1}{\epsilon_I}} I_{1t}^{\frac{\epsilon_I-1}{\epsilon_I}} + (1 - \omega_I)^{\frac{1}{\epsilon_I}} I_{2t}^{\frac{\epsilon_I-1}{\epsilon_I}} \right)^{\frac{\epsilon_I}{\epsilon_I-1}} \quad (35)$$

515 where ω_c and ω_I are the weights of product 1 in consumption and invest-
 516 ment. ϵ_c and ϵ_I are the substitution elasticities between two products in
 517 producing final consumption and investment, both of which are less than
 518 unit. Note that consumption and investment can be different in terms of
 519 weight of each product, substitution elasticity, and investment-specific tech-
 520 nological progress.

521 **Proposition 2.** *Given the production function in Eq.(33), absent carbon tax,*
 522 *it is straightforward to show that the relative price between two products in*
 523 *competitive market is pinned down by:*

$$\frac{p_{2t}}{p_{1t}} = \frac{\hat{F}_1(A_{1t}, T_t)}{\hat{F}_2(A_{2t}, T_t)} \quad (36)$$

524 *such that given the consumption and investment production functions as*
 525 *Eq.(34) and Eq.(35), the share of product i will increase in tandem with its*
 526 *relative price. Thus, structural change takes place via the price effect. More-*
 527 *over, two definitions of social cost of carbon are linked by the transformation*
 528 *ratio:*

$$\frac{SCC_{CE}}{SCC_{IE}} = \underbrace{\frac{A_{It}}{ISTC}}_1 \times \frac{\left[\omega_c \hat{F}_1(A_{1t}, T_t)^{\epsilon_c-1} + (1 - \omega_c) \hat{F}_2(A_{2t}, T_t)^{\epsilon_c-1} \right]^{\frac{1}{\epsilon_c-1}}}{\underbrace{\left[\omega_I \hat{F}_1(A_{1t}, T_t)^{\epsilon_I-1} + (1 - \omega_I) \hat{F}_2(A_{2t}, T_t)^{\epsilon_I-1} \right]^{\frac{1}{\epsilon_I-1}}}_{SC \text{ interacted with climate}}} \quad (37)$$

529 Proof: See Appendix A. Proposition 2 presents two relative prices that
 530 are related to the Baumol's cost disease and social cost of carbon, respec-
 531 tively.

532 **The first** is the relative price between two final products in Eq.(36),
 533 jointly determined by technological productivity growth and climate vulner-
 534 ability. We consider the relative price under three different cases, and discuss

535 their relevance to the Baumol’s cost disease. Note that the substitution elas-
 536 ticity between two final products are less than unit in both Eq.(34) and
 537 Eq.(35).

538 **Case 1: Only technological productivity affects the relative price.**
 539 In structural change literature, climate vulnerability is normally not included.
 540 Thus, following the common assumption that technology enters the produc-
 541 tion function in multiplicative form, Eq.(36) boils down to:

$$\frac{p_{2t}}{p_{1t}} = \frac{A_{1t}}{A_{2t}} \quad (38)$$

542 Assume that sector 1 has a robust productivity growth, while sector 2 is
 543 stagnant in growth (like services). Thus, the relative price of product 2 to
 544 product 1 will increase over time. As products in both sectors are necessary in
 545 producing consumption and investment, more and more productive resources
 546 will flow into the non-progressive sector because of its increasing relative
 547 price, and the share of this sector is expanding in the economy. In the long
 548 run, the aggregate productivity growth slows down due to an growing sector
 549 with slow productivity growth. Thus, *the Baumol’s cost disease* occurs, as
 550 studied in Ngai and Pissarides (2007) and Herrendorf et al. (2021).

551 **Case 2: Only climate vulnerability affects the relative price.** Cli-
 552 mate vulnerability between two sectors, determined by climate capital, can
 553 also influence the relative price, leading up to *the Baumol’s climate disease*.
 554 Assume that two final sectors have fixed knowledge capital so that technolog-
 555 ical productivity is constant in both sectors. Thus, Eq.(36) can be rewritten
 556 to:

$$\frac{p_{2t}}{p_{1t}} = \frac{\hat{F}_1(T_t)}{\hat{F}_2(T_t)} \quad (39)$$

557 where $\hat{F}_i(T_t)$ reflects the ability of sector i to produce to uniform climate
 558 capital T_t . As explained in Section 2, it can be perceived as the climate
 559 damage function, and governs heterogeneous climate vulnerability. Thus,
 560 a higher level of climate capital T_t implies a high damage level, and hence
 561 a lower level of $\hat{F}_i(T_t)$. As climate capital is nonrival and nonexcludable,
 562 climate capital is overestimated and a higher level of global mean temperature
 563 is attained. Assume that economic production in sector 2 is more reliant on
 564 climate capital. Thus, given a higher temperature uniform to both sectors,
 565 $\hat{F}_2(T_t)$ is increasingly lower than $\hat{F}_1(T_t)$. Thus, the relative price of product

566 2 is climbing gradually. Again, because both products are necessary and
567 cannot be well substituted, the expenditure on product 2 will increase in
568 accordance. Thus, given an expanding sector in the economy more vulnerable
569 to climate change, the aggregate economy will become increasingly vulnerable
570 to climate change. In effect, a sector that is more vulnerable to climate change
571 is technically a sector with slower productivity growth.

572 Existing climate-economy models (Barrage and Nordhaus, 2023; Golosov
573 et al., 2014; Barrage, 2020, e.g.:.) usually treat the economy as a single final
574 sector, and study the incentives to address climate change. In this paper, we
575 show that because climate capital is nonrival, nonexcludable and unpriced, it
576 leads to overinvested carbon. This is the first incentive for carbon abatement
577 in Proposition 1. We add here that the Baumol’s climate disease is another
578 important incentive to cope with climate change seriously after accounting for
579 heterogeneous climate vulnerability. Long-run economic growth is hampered
580 by climate change due to unpriced climate capital, and this adverse impact
581 can be potentially aggravated by the Baumol’s climate disease.

582 **Case 3: Both affect the relative price.** In reality, technological
583 productivity and climate vulnerability jointly determine the relative price
584 as in Eq.(36). Suppose that sector 2 has lower productivity growth and
585 higher climate vulnerability, its relative price will be higher than both Case
586 1 and Case 2. Put differently, *the joint effect of Baumol’s cost and climate*
587 *diseases* is even more acute. Thus, failure to pricing climate capital can drag
588 down aggregate economic growth severely, and there is a stronger incentive to
589 disinvest carbon. Suppose that sector 2 has high productivity growth and also
590 high climate vulnerability. Under the plausible assumption that the impact
591 of productivity growth outweighs climate vulnerability, the relative price of
592 product 2 to product 1 may also increase, but to an extent less than absent
593 climate change. Baumol’s cost and climate diseases are ameliorated. Thus,
594 the urgency to address climate change is reduced. This reasoning may be
595 surprising at first sight, but can be valid. A sector with higher productivity
596 growth implies a higher resilience to climate change. Although the sector
597 may be more vulnerable to climate change, it can soon recover from climate
598 damage by rapidly accumulating knowledge capital.

599 **The second price** bridges two definitions of social cost of carbon, and
600 in fact reflects the relative price of investment to consumption. As shown
601 by Eq.(37), the ratios depends on investment-specific technical change A_{It} ,
602 how climate capital interacts with knowledge capital in each final sector
603 $F_i(A_{it}, T_t)$, the weight of product 1 in producing investment and consumption

604 ω_I and ω_c , and the substitution elasticity between two products in invest-
605 ment and consumption ϵ_I and ϵ_c . In climate-economy models with one final
606 production sector, because the productions of investment and consumption
607 are not specified, all items are cancelled out¹¹. The consumption-equivalent
608 social cost of carbon is the same as the investment-equivalent one. Our
609 specifications of investment and consumption production are admittedly not
610 comprehensive. But they serve as good examples for illustrating that only
611 under very strict condition would one expect two definitions of social cost of
612 carbon are numerically identical. The real cost of carbon is on investment,
613 and but can be denominated in terms of consumption after transformation.

614 4. Calibration

615 4.1. Sector division

616 We divide the whole economy into goods and services, motivated by two
617 reasons. It is important to note that sector division in this paper is for
618 heuristic purpose, rather than for approximating the real world perfectly.

619 **Reason 1:** On the climate-to-economy side, the services sector appears
620 to be less vulnerable to weather shocks than the goods sector. Following
621 Burke et al. (2015) but focusing on sectoral impact, we investigate

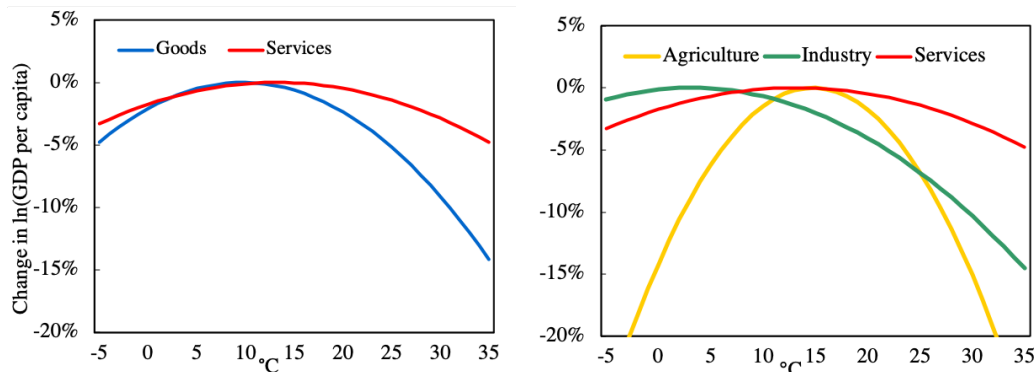
$$\Delta Y_{it}^j = h(T_{ij}) + g(P_{ij}) + \mu_i + \zeta_t + \theta_i t + \theta_{i2} t^2 + \epsilon_{it} \quad (40)$$

622 where ΔY_{it}^j is the output growth rate of sector j (either goods or services)
623 in country i at year t , T annual average temperature, P precipitation, μ_i
624 country-specific constant terms, ζ_t year fixed effects and $\theta_i t + \theta_{i2} t^2$ flexible
625 country-specific time trends.

626 Figure 1 shows when the global annual average temperature rises above
627 around 13 degrees Celsius, the impact on the goods sector will soon be larger
628 than on the services, and the gap is widened at a higher temperature (Panel
629 a). Even when subtracting the agriculture sector, that is among the most
630 vulnerable to temperature, weather shocks take a heavier toll on the left
631 industry production than services (Panel b). Moreover, the adverse impact
632 on industry can start at a temperature much lower than services. These
633 results are consistent with Casey et al. (2021) and Rudik et al. (2021) that

¹¹Section 6 examines a simplified case where there are two final sectors producing investment and consumption, respectively.

634 labor productivity can suffer a heavier loss under heat stress in outdoor
 635 activities which are more concentrated in the goods sector.



(a) Impact on goods and services

(b) Impact on three sectors

Notes: The figure shows how sectoral GDP growth can be affected by temperature shocks using the data from Burke et al. (2015).

Figure 1: Sectoral damages

636 **Reason 2:** The sluggish services sector may drive down aggregate pro-
 637 ductivity growth.

638 The services sector affects aggregate productivity growth. One-sector
 639 climate-economy models do not explicitly include this prospect. Evolving
 640 growth path in each sector combines to determine aggregate growth path (Fo-
 641 erster et al., 2022), and hence an expanding sector with a lower-than-average
 642 growth rate is capable of slowing down aggregate growth, which is roughly the
 643 core of Baumol’s cost disease (Baumol, 1967; Nordhaus, 2008). In the past
 644 decades, a strand of literature has been actively engaged in leveraging the
 645 growth models to analyze the implications of rising services on long-run eco-
 646 nomic growth (e.g.: Duarte and Restuccia, 2010; Ngai and Pissarides, 2007;
 647 Leon-Ledesma and Moro, 2020; Duernecker et al., 2023). However, the rise
 648 of services receives surprisingly deficient attention in the climate economics
 649 literature.

650 Given such division, we calibrate the model.

651 *4.2. Households*

652 The representative household maximize the population-weighted lifetime
653 utility:

$$\sum_{t=0}^{\infty} \beta^t N_t U(c_{1t}, c_{2t}) \quad (41)$$

654 where N_t is aggregate population projections following the DICE model
655 (Nordhaus, 2017). c_{1t} represents consumption of goods, and c_{2t} consump-
656 tion of services.

657 We use the literature to calibrate the consumption production function
658 Eq.(34) (see Table 1). The gap in substitution elasticity between earlier and
659 recent literature can be reconciled by two different accounting approaches
660 matching the data, final expenditure and value added (Herrendorf et al.,
661 2013). We take a benchmark value of 0.2 for parameter ϵ_C governing the
662 substitution elasticity between goods and services in consumption. In ad-
663 dition, the services expenditure share in consumption is 0.8. Overall, our
664 chosen values are consistent with existing studies that observe the comple-
665 mentary relationship between goods and services in consumption as well as
666 a relatively larger proportion of services.

Table 1: Parameters of the utility function

Source	Calibrated to	$1 - \omega_c$	ϵ_c
Buera and Kaboski (2009)	USA	NA	0.5
Duarte and Restuccia (2010)	USA	0.96	0.4
Herrendorf et al. (2013)	USA	0.81	0.002
Moro (2015)	USA	0.95	0.4
Alder et al. (2022)	AUS, CAN, GBR & USA	0.60-0.77	0.00-0.17

667 *4.3. Production sectors*

668 We assume the Cobb-Douglas production technology for both final produc-
669 tion sectors, with capital, labor and energy as inputs. Thus, the produc-
670 tion functions are given as:

$$\begin{aligned} \tilde{F}_1(L_{1t}, K_{1t}, E_{1t}) &= K_{1t}^\alpha L_{1t}^{1-\alpha-\beta} E_{1t}^\beta \\ \tilde{F}_2(L_{2t}, K_{2t}, E_{2t}) &= K_{2t}^\alpha L_{2t}^{1-\alpha-\beta} E_{2t}^\beta \end{aligned} \quad (42)$$

671 The identical factor intensity in two sectors are assumed to simplify the
672 model. If capital share differs in each sector, this would generate another
673 force for structural change via the price effect, as discussed above¹². Thus,
674 following Nordhaus (2017) and Golosov et al. (2014), we adopt a capital share
675 of $\alpha = 0.3$ and an energy share of $\beta = 0.03$ for both sectors.

676 For the sectoral productivity growth and climate vulnerability, we assume:

$$\begin{aligned}\hat{F}_1(A_{1t}, T_t) &= A_{1t}(1 - D_1(T_t)) \\ \hat{F}_2(A_{2t}, T_t) &= A_{2t}(1 - D_2(T_t))\end{aligned}\tag{43}$$

677 where $D_i(T_t)$ represents the fraction of output loss due to temperature change
678 T_t in sector i at time t . We follow both the DICE model (Nordhaus, 1992,
679 2017) and Golosov et al. (2014) where climate damage enters the production
680 function in multiplicative form. The departure from previous works is that
681 we allow for differentiated impact of temperature rise on producing goods
682 and services. To pin down the technological growth in each sector, we first
683 abstract from climate damages. Then, we determine the relative ratio of the
684 goods sector to the services from existing studies (see Table 2), and, taking
685 this ratio as given, mimic the capital stock in the DICE model at 2100. This
686 strategy guarantees the closest comparability to DICE at an identical wealth
687 level. Let γ_i denote the technological growth in sector i . Taking a benchmark
688 value of 3 for γ_1/γ_2 , we have $\gamma_1 = 10.86\%$ and $\gamma_2 = 3.62\%$.

Table 2: Parameters of sectoral productivity growth

Source	Calibrated to	γ_1/γ_2	γ_a/γ_2	γ_m/γ_2
Leon-Ledesma and Moro (2020)	USA	5.43	NA	NA
Comin et al. (2021)	USA	NA	2.64	1.20
Buera et al. (2020)	USA	NA	4.17	1.75

Notes: γ_i denotes the technological growth in sector i , with 1 for goods, 2 for services, a for agriculture and m for manufacturing.

689 Now we move on to investment production function Eq.(35). Recent
690 studies delving into the structural change within investment arrive at con-
691 sistent findings that exogenous investment-specific technical change has a

¹²One could argue that energy share is higher in the goods sector as it is more energy-intensive. Given our main intention is to understand the interactions between climate change and structural change dynamics, we assume energy intensity is also equivalent in both sectors.

692 minor or even negligible effect in long-run growth (Herrendorf et al., 2021;
693 García-Santana et al., 2021; Buera et al., 2020). Herrendorf et al. (2021)
694 finds that the productivity growth in goods can be three times larger than
695 investment-specific technical change. Therefore, in addition to assuming no
696 climate impact, we further assume for simplicity it remains constant, namely,
697 $\gamma_{I,2015} = 0\%$. The investment-specific technology level in the initial period
698 (in 2015) is normalized to one. Moreover, we adopt $\omega_I = 0.57$ and $\epsilon_I = 0.5$,
699 both of which are consistent with existing studies (Table 3).

Table 3: Parameters of the final investment production function

Source	Calibrated to	ω_I	ϵ_I
Herrendorf et al. (2021)	USA	0.65	0.00
García-Santana et al. (2021)	Countries in PWT & WIOD	0.58	0.51
Buera et al. (2020)	USA	0.52	0.01

700 For the energy sector, we also assume a Cobb-Douglas production func-
701 tion:

$$E_t = A_{Et} K_{Et}^{\alpha_E} L_{Et}^{1-\alpha_E} \quad (44)$$

702 where the labor share is 0.403 adopted from Barrage (2020). In addition, the
703 energy sector is assigned to the same labor-augmented productivity growth
704 as the goods sector.

705 For value added shares of goods and services in initial period, we refer to
706 the World Development Indicators. Goods account for 33.57% of aggregate
707 value added, and services is 66.43%. We further combine with first order
708 conditions to determine the factor share in each sector in the initial period.

709 4.4. Carbon cycle and climate models

710 The current paper borrows the carbon cycle and climate model from the
711 DICE model (Nordhaus, 2017), which generates a warming of 3.1°C for a
712 doubling of carbon concentrations in equilibrium and a transient climate
713 sensitivity of 1.7°C.

714 First, the equations of the carbon cycle include three reservoirs (the atmo-
715 sphere M_t^{At} , the upper oceans and the biosphere M_t^{Up} , and the deep oceans

716 M_t^{Lo}):

$$\begin{pmatrix} M_t^{At} \\ M_t^{Up} \\ M_t^{Lo} \end{pmatrix} = \begin{pmatrix} \phi_{11} & \phi_{21} & 0 \\ \phi_{12} & \phi_{22} & \phi_{32} \\ 0 & \phi_{23} & \phi_{33} \end{pmatrix} \begin{pmatrix} M_{t-1}^{At} \\ M_{t-1}^{Up} \\ M_{t-1}^{Lo} \end{pmatrix} + \begin{pmatrix} E_t^M + E_t^{Land} \\ 0 \\ 0 \end{pmatrix} \quad (45)$$

717 where ϕ_{ij} measures the carbon flow between reservoirs and E_t^{Land} represents
718 exogenous land carbon emissions.

719 Second, the increased carbon concentrations in the atmosphere elevate
720 radiative forcing:

$$\chi_t = \kappa [\ln (M_t^{At} / M_{1750}^{At}) / \ln(2)] + \chi_t^{Ex} \quad (46)$$

721 where χ_t^{Ex} is the exogenous forcing from other greenhouse gases.

722 Last, higher radiative forcing raises the atmospheric temperature T_t and,
723 indirectly, the deep ocean temperature T_t^{Lo} :

$$\begin{pmatrix} T_t \\ T_t^{Lo} \end{pmatrix} = \begin{pmatrix} 1 - \zeta_1 \zeta_2 - \zeta_1 \zeta_3 & \zeta_1 \zeta_3 \\ 1 - \zeta_4 & \zeta_4 \end{pmatrix} \begin{pmatrix} T_{t-1} \\ T_{t-1}^{Lo} \end{pmatrix} + \begin{pmatrix} \zeta_1 \chi_t \\ 0 \end{pmatrix} \quad (47)$$

724 where $\{\zeta_i\}_{i=1}^4$ are parameters governing heat exchange between the atmo-
725 sphere and the ocean.

726 4.5. Sectoral climate damages

727 In the DICE model, the damage function is calibrated to match a damage
728 of 2.1% damage of income at 3°C. We adopt the damage function as in DICE-
729 2016, and suppose that the curvature of the damage function is identical in
730 both sectors. Furthermore, our calibration matches that the relative climate
731 damage in the goods sector is three times that of services and also that at a
732 temperature rise of 3°C, the combined damage from two sectors amount to
733 that of DICE. The damage function in the IAMs has always been one of the
734 most uncertain components, and this concern also applies here. However,
735 although the damage function is highly uncertain, our analysis only requires
736 that sector is different in the productivity of climate capital. Therefore, the
737 benchmark model adopts a damage function for output in each sector as
738 follows:

$$1 - D_1(T_t) = \frac{1}{1 + 0.004352 * T_t^2} \quad (48)$$

$$1 - D_2(T_t) = \frac{1}{1 + 0.001414 * T_t^2} \quad (49)$$

739 *4.6. Abatement costs*

740 In the DICE model, the abatement cost function is directly governed
 741 by the control rate, whereas the abatement costs in this study are related
 742 to the unit of abated carbon emission. Thus, following Barrage (2020), we
 743 recalibrate the abatement cost function through a logistic approximation to
 744 the abatement cost curve implied by Nordhaus (2017):

$$\Theta_t(\mu_t E_t) = \frac{\bar{a} P_t^{backstop}}{1 + a_t \exp(b_{0t} - b_{1t}(\mu_t E_t)^{b_2})} \cdot (\mu_t E_t) \quad (50)$$

745 where $P_t^{backstop}$ is the price for backstop technology.

746 Finally, we have $\bar{a} = 0.7464$, $a_t = 0.6561 + 0.8881t$, $b_{0t} = 7.864 - 1.4858t$,
 747 $b_{1t} = 1.6791 - 0.3157t$ and $b_2 = 0.4207$. It should be noted that the abatement
 748 costs is denominated by investment product whereas the abatement costs in
 749 DICE adopt the final output as numeraire. We perform sensitivity tests for
 750 abatement costs, and find that the key insights in this study are not affected.

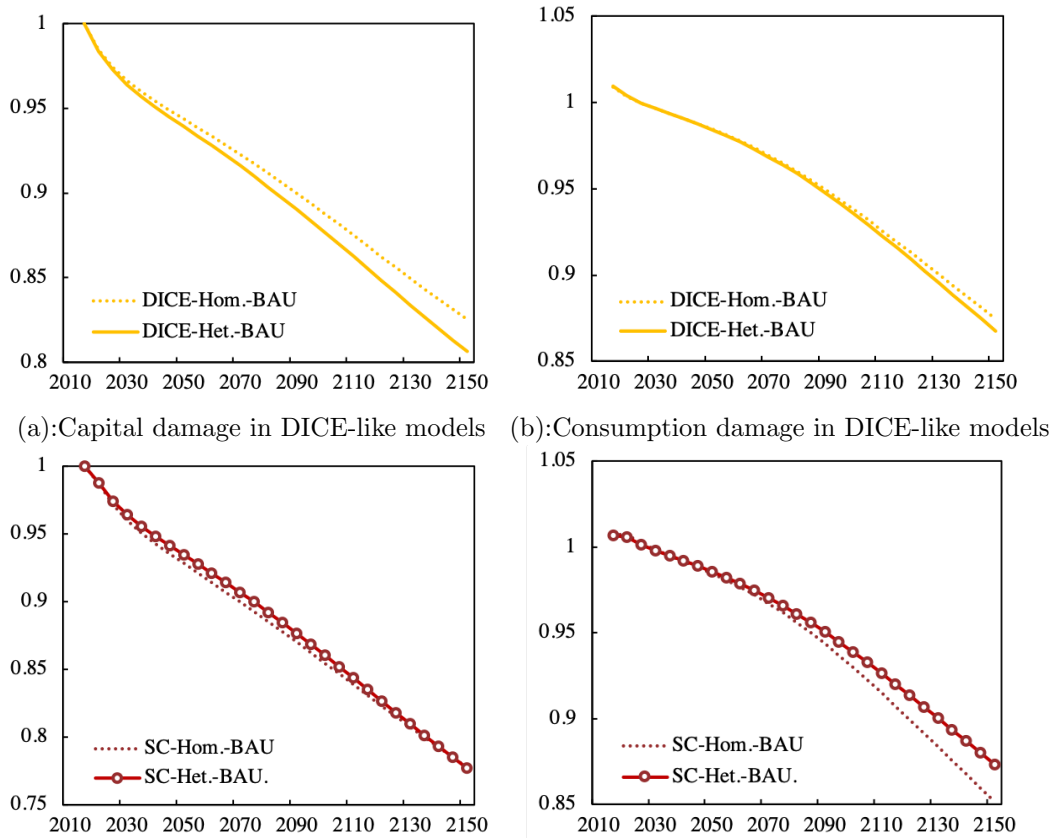
751 Further details on calibration are provided in Appendix B.

752 **5. Quantitative results**

753 In this section, we present the numerical results of the constructed climate-
 754 economy model. Two standard scenarios are considered throughout, a business-
 755 as-usual (BAU) scenario where the climate externality is completely ignored
 756 so that no abatement policy is adopted, and an optimal scenario where a
 757 carbon tax is adopted equating marginal abatement cost to marginal climate
 758 damage. We also consider, where necessary and for ease of exposition, an
 759 additional scenario with no climate (pure economic growth model) to demon-
 760 strate the economic frontier. We first present the damage level to explore
 761 whether the Baumol’s climate disease is consistent with the theoretical results
 762 in Section 3. Then, we quantify the social cost of carbon with two different
 763 definitions, namely, investment-equivalent and consumption-equivalent, and
 764 explain their implications.

765 *5.1. Climate damage and abatement incentive*

766 Figure 2 displays the relative level of capital stock and consumption in
 767 the BAU scenario compared to their economic frontier without climate dam-
 768 age. DICE-like models denotes that two sectors have identical productivity



(a):Capital damage in DICE-like models (b):Consumption damage in DICE-like models
(c):Capital damage under structural change (d):Consumption damage under structural change
Notes: Panels (a)-(d) compare the results under both homogeneous(Hom.) and heterogeneous(Het.) climate vulnerability. The vertical axis describes the relative level of each economic variable in the business-as-usual scenarios compared to the their frontiers under no climate externality in each period. DICE means two identical sectors, SC means structural change.

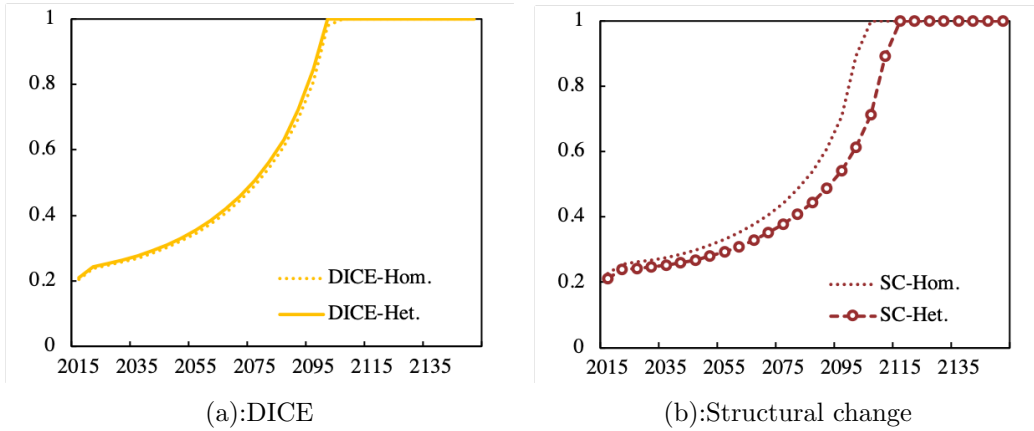
Figure 2: Capital and consumption damage

769 growth, while 'under structural change' means that the productivity growth
770 rate in goods is three times that in services.

771 When two sectors have the same productivity growth, only the Baumol's
772 climate disease is operating, as the Case 2 in Section 3. Panels (a) and (b)
773 show that climate damage is indeed higher under heterogeneous climate vul-
774 nerability, validating the impact of the Baumol's climate disease. When no
775 abatement policy is adopted, capital stock is 5.62% (6.07%) lower in 2050,
776 11.25% (12.34%) lower in 2100, and 17.47% (19.37%) lower in 2150 than its
777 frontier under homogeneous (heterogeneous) damage (Panel a). Aggregate
778 consumption under heterogeneous damage is also in general lower than ho-
779 mogeneous one (Panel b), but the gap is narrower than capital damage. For
780 DICE-like models, the consumption level is 0.03 percentage points higher in
781 2050 when sectors are equally vulnerable, and this difference increases to 0.71
782 percentage points in 2150.

783 If we assume the goods sector has a productivity growth two times faster
784 than services, a different pattern is obtained. Under heterogeneous climate
785 vulnerability, both capital and consumption damages are lower before the
786 end of this century, compared to under homogeneous climate vulnerability.
787 As investment consists of an increasing proportion of services, relative capital
788 damage curve under heterogeneous damage overlaps with or is even slightly
789 above that under homogeneous damage in initial periods (Panel c). Put
790 differently, the trend that services is gaining its importance in investment
791 makes economic growth more resilient. By comparison, aggregate consump-
792 tion is elevated in the displayed period (Panel d), due to higher dependence
793 on services in consumption than investment, and also to that capital damage
794 is not aggravated under heterogeneous climate vulnerability in the displayed
795 periods.

796 Figure 3 on optimal abatement rate confirms that the incentives to reduce
797 investment into climate capital is influenced by the Baumol's cost and climate
798 diseases. When only the Baumol's climate disease is operating, the abate-
799 ment curve is higher under heterogeneous climate vulnerability, although the
800 its gap with under homogeneous climate vulnerability is not obvious (Panel
801 a). But the time to achieve net zero emissions is advanced by five years.
802 In comparison, if accounting for rising services, the abatement policy is less
803 strict under heterogeneous climate vulnerability, as reflected in the lower
804 circle-dash line (Panel b). It is suggested that the social planner should put
805 off the time to achieve net zero emissions by 10 years. The reason is that
806 although the goods sector is more vulnerable to climate change, its productiv-



Notes: Panels (a)-(b) show the optimal abatement rate under both homogeneous(Hom.) and heterogeneous(Het.) climate vulnerability.

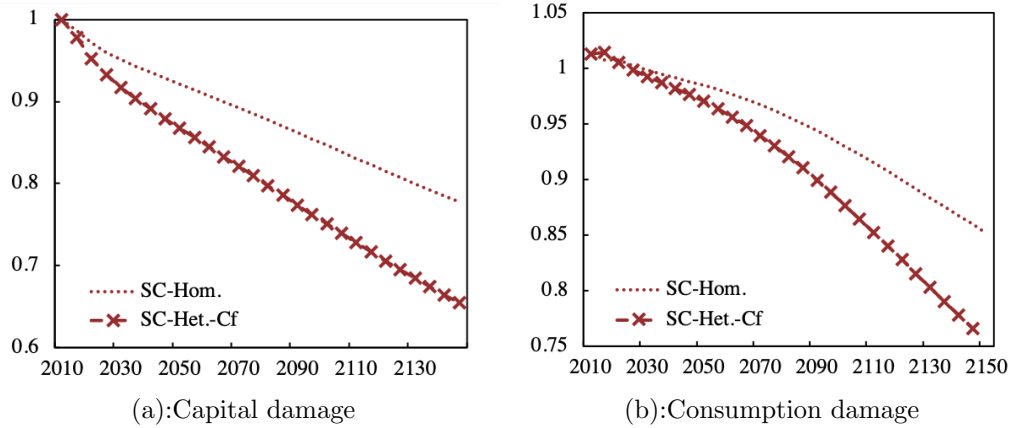
Figure 3: Optimal abatement rate

807 ity growth rate is also higher than services. Thus, climate change ameliorates
 808 the impact of the Baumol’s cost disease.

809 *5.2. Counterfactual experiments*

810 Previous numerical exercises are based on the observations that the goods
 811 sector is more climate-vulnerable than the services sector, whereas we analyze
 812 in Case 3 that the climate impact can be either amplified or ameliorated by
 813 the relative price. Because this paper cannot exhaust all sector divisions,
 814 it considers a counterfactual case assuming that the climate impact on the
 815 services sector is three times that on goods. In this case, the relative price
 816 between two sectors will be further increased.

817 Figure 4 displays that both capital and consumption are considerably
 818 reduced when heterogeneous climate vulnerability aggravates the Baumol’s
 819 cost disease. Climate change will decrease capital stock by 14.55% in 2100 if
 820 its impact is uniform to each sector. By comparison, the capital loss will ad-
 821 ditionally increase by 9.20 percentage points to 23.75% under heterogeneous
 822 climate vulnerability. The impact on capital stock brings about a further
 823 drop of 4.14 percentage points in consumption by the end of this century. As
 824 a result, the optimal strategy to cope with climate change is to achieve net-
 825 zero emissions in 2085, twenty years ahead of the time under homogeneous
 826 vulnerability.



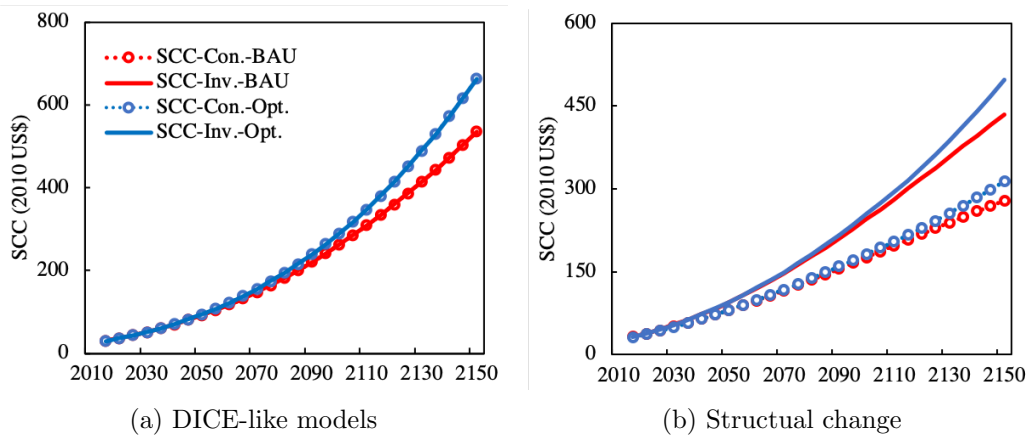
Notes: Panels (a)-(b) compare the results under both homogeneous(Hom.) and heterogeneous(Het.) climate vulnerability. The vertical axis describes the relative level of each economic variable in the business-as-usual scenarios compared to the their frontiers under no climate externality in each period. The services sector is assumed to be, counterfactually, more climate-vulnerable than the goods sector.

Figure 4: Counterfactual capital and consumption damages

827 *5.3. Social cost of carbon: consumption equivalent v.s. investment equivalent*

828 In Section 4, we theoretically show that the actual trade-off between
 829 abatement cost and climate damage resides in how the final investment is
 830 affected, and propose investment-equivalent social cost of carbon in addition
 831 to consumption-equivalent one. In this part, we quantify the social cost of
 832 carbon under both definitions (Figure 5). For better illustration, we compare
 833 DICE-like models with models under structural change.

834 Two definitions of social cost of carbon generate identical numerical val-
 835 ues in the DICE-like models (Panel a). In a symmetric world, a unit of
 836 final production can be used to produce the same amount of investment or
 837 consumption, and therefore one can arbitrarily choose either definition. In
 838 contrast, under structural change (Panel b), there is an obvious divergence.
 839 In 2100, the social cost of carbon in the optimal scenario comes to a invest-
 840 ment loss of \$254/tCO₂, or equivalently a consumption loss of \$182/CO₂.
 841 In 2150, this gap further expands, with investment-equivalent social cost
 842 of carbon climbing to \$497/tCO₂, 59% higher than consumption-equivalent
 843 one. Because two final production sectors differ in productivity growth rate,
 844 climate vulnerability and also their compositions in consumption and invest-
 845 ment, one unit of final production can no longer be converted to an equalized



Notes: Two definitions of social cost of carbon are presented—consumption equivalent social cost of carbon (SCC-Con.) and investment equivalent one (SCC-Inv.). BAU denotes the business-as-usual scenario (no abatement), and Opt. denotes the optimal scenario.

Figure 5: Social cost of carbon

846 amount between investment and consumption. More concretely, since the
 847 production of consumption is assumed to be more heavily reliant on services,
 848 which has a lower productivity growth, its price relative to investment will
 849 rise, eventually leading to a lower value of social cost of carbon denominated
 850 by consumption.

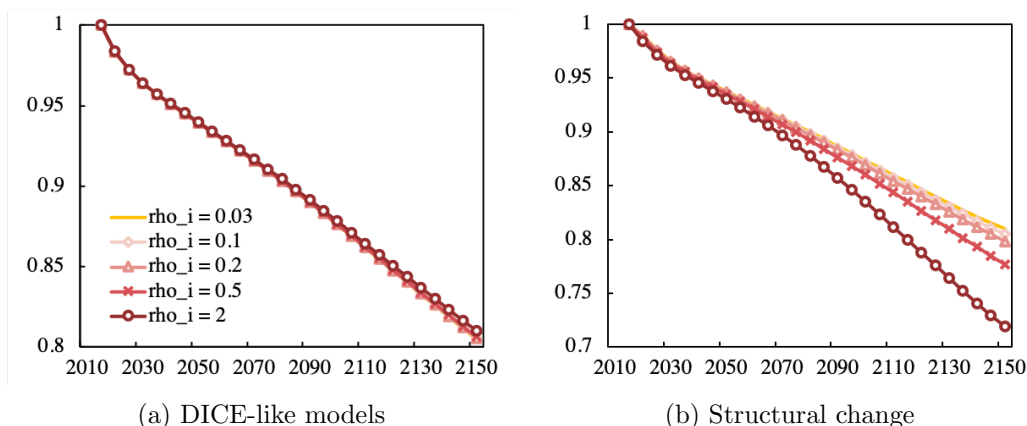
851 6. Sensitivity and extensions

852 In this section, we first test the sensitivity of our results by changing the
 853 values of some key parameters. Then, we extend with two alternative models.

854 6.1. Sensitivity analyses

855 First, the substitution elasticity between two sectors can affect the net
 856 impact of the Baumol’s cost disease. We focus on the elasticity in investment
 857 production. In general, extant studies are consistent that the substitution
 858 elasticity between goods and services is low. In our baseline model, we choose
 859 a value of 0.5. Some studies argue that this value could be even lower and
 860 close to zero. Thus, we test the robustness of our results by choosing a
 861 value of 0.03, 0.1 and 0.5. Also, we perform the model with a value of
 862 2 as a comparison, where two products can easily substitute each other in
 863 formulating the final investment. Results are displayed in Figure 6. Changing

864 the substitution elasticity can work through altering both the price effect and
 865 the potential to transit to a less vulnerable sector consisting of more services.

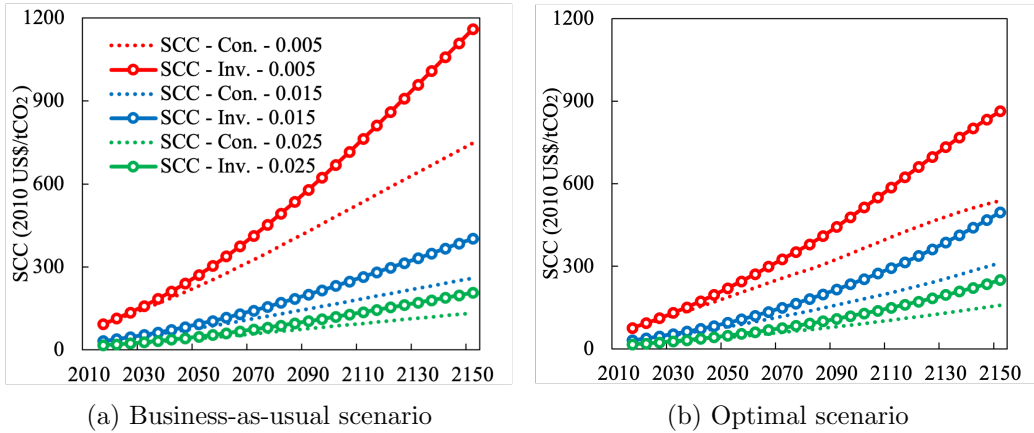


Notes: The vertical axis shows the relative level of capital stock under heterogeneous damage to its economic frontier (without climate damage). ρ_i is the substitution elasticity between goods and services in producing final investment.

Figure 6: Capital damage under different substitution elasticities

866 When sectors are only different in climate vulnerability, a lower-than-unit
 867 substitution elasticity yields a lower level of capital stock, although changes
 868 are negligible (Panel a). Notably, when goods and services are assumed to be
 869 substitutes (ρ_i as 2), we observe that relative climate damages are slightly
 870 alleviated in the DICE-like models. Once accounting for the rising services
 871 in structural change model, we find that a lower elasticity is associated with
 872 a lower relative damage. Because a lower elasticity can generate a more severe
 873 Baumol’s cost disease, the climate impact is further alleviated by the
 874 Baumol’s cost disease. Moreover, when two products are considered as sub-
 875 stitutes, the relative damage level is considerably aggravated. This should
 876 not be surprising because when two products can well substitute each other,
 877 the Baumol’s cost disease is no longer operating and hence the economy is
 878 more prosperous absent climate impact. Higher production brings about
 879 more carbon emissions and consequently further increases global mean tem-
 880 perature, giving rise to higher damage levels.

881 Second, the social time preference rate is a key factor in driving the re-
 882 sults of the social cost of carbon and debates around it abound (Barrage,
 883 2018). We are specifically interested in whether such choices will also matter
 884 to the gap between two definitions of social cost of carbon. We address this



Notes: Two definitions of social cost of carbon are presented in the figure, which are consumption equivalent social cost of carbon (SCC-Con.) and investment equivalent one (SCC-Inv.). Results are reported choosing different values of social time preference (0.005, 0.015 or 0.025).

Figure 7: Social cost of carbon and the discount rate

885 problem by altering the benchmark value of the social time preference from
 886 0.015 (which is used by the DICE model) to a percentage point higher and
 887 lower. Figure 15 shows that when a lower social time preference is chosen,
 888 the implied social cost of carbon under both scenarios will climb dramati-
 889 cally. Moreover, the gap is amplified between the consumption equivalent
 890 social cost of carbon and the investment equivalent one. For example, the
 891 gap in 2100 between two definitions is enlarged from $\$34/\text{tCO}_t$ (0.025) to
 892 $\$52/\text{tCO}_t$ (0.015) and further to $\$187/\text{tCO}_t$ (0.005) under the business-as-
 893 usual scenario. A similar picture is observed in the optimal scenario.

894 *6.2. Alternative models*

895 We present two alternative models and discuss their implications. All
 896 proofs are included in the appendix.

897 **Case 1: Consumption and investment.** The model can be simplified
 898 to a two-sector version that produces consumption and investment respec-
 899 tively. The two-sector growth model resembles in structure that in Green-
 900 wood et al. (1997) and Foerster et al. (2022), and enables us to demonstrate
 901 that the deviation between the consumption-equivalent and investment-equivalent
 902 social costs of carbon originates from the detailed consideration of the dis-
 903 tinct procedures for producing consumption and investment. It can be shown

904 that the optimal carbon tax in this case is pinned down by:

$$\begin{aligned}
\Theta' &= F_{IEt} - \frac{F_{Ilt}}{F_{Elt}} \\
&= (-1) \sum_{j=0}^{\infty} \beta^j \left(\underbrace{\frac{\lambda_{C,t+j}}{\lambda_{It}} \frac{\partial Y_{C,t+j}}{\partial T_{t+j}}}_{\text{Impact on consumption}} + \underbrace{\frac{\lambda_{I,t+j}}{\lambda_{It}} \frac{\partial Y_{I,t+j}}{\partial T_{t+j}}}_{\text{Impact on investment}} \right) \frac{\partial T_{t+j}}{\partial E_t^{unc}} \quad (51)
\end{aligned}$$

905 This identity also establishes the shadow price of investment as denomi-
906 nation, but the climate damage aggregates both consumption damage and
907 investment damage. In the baseline model, energy input should be utilized
908 to produce two final products first, and then two products are combined to
909 produce the aggregate investment. By comparison, the benefits of one ad-
910 ditional tone of carbon emission is now represented by how much aggregate
911 investment it can straightly produce. To sum up, the trade-off still centers
912 on investment instead of consumption.

913 **Case 2: Differential abatement costs between sectors.** In the
914 model, we do not allow for the more realistic case that each production
915 sector can be characterized by different abatement costs (Gillingham and
916 Stock, 2018). This can be easily included in the model by introducing two
917 individual abatement cost functions. In so doing, one can establish that the
918 marginal abatement cost in each sector should be equalized and also equal
919 to marginal climate damages:

$$\Theta'_{gt} = \Theta'_{st} = MD \quad (52)$$

920 where Θ_{it} denotes the abatement cost function in sector i and MD the
921 marginal climate damages aggregating both sectors. It is of practical in-
922 terest to include differentiated abatement functions in each sector¹³.

923 7. Discussion and Conclusion

924 This paper establishes a dynamic general equilibrium model with en-
925 dogenous structural change. Using the model, we investigate optimal carbon
926 abatement under structural change.

¹³Vogt-Schilb et al. (2018) further shows that after accounting for the value of abatement capital in the future, optimal marginal abatement cost can differ in each sector. We do not include this concern in the current paper, but it can be an interesting extension.

927 Three reasons stand out for reducing carbon investment in the atmo-
928 sphere. First, climate is an essential capital used in economic production,
929 but it is unpriced, nonrival, and nonexcludable. Thus, climate capital is
930 disinvested by carbon emissions, and too much carbon emissions imply a
931 deteriorating productive base, which can be conceived as reduction in phys-
932 ical capital. For modelling practice, climate capital proxied by global mean
933 temperature is characterized by decreasing returns to scale. Second, the
934 heterogeneous productivity of climate capital amplifies the productivity dif-
935 ference between sectors, leading to Baumol's climate disease. Third, Bau-
936 mol's climate disease can either alleviate or exacerbate Baumol's cost disease,
937 depending on the combination of productivity growth and climate vulnerabil-
938 ity. Whenever there is a sector with higher climate vulnerability and lower
939 productivity growth, higher abatement is required. The first reason is well-
940 established (Nordhaus, 1992). The second and third are new and can call for
941 more stringent greenhouse gas emission reduction.

942 The model used is stylized for maximum transparency and insight. This
943 implies that key factors that may well affect optimal climate policy are omit-
944 ted from the analysis. The model has one region only. This not only reduces
945 the public bad nature of carbon dioxide emissions, it also excludes any ef-
946 fects of international trade and investment. The model has only two sectors.
947 This makes the model less suitable as a representation of less developed
948 countries. Structural economic change is one of the drivers of the Environ-
949 mental Kuznets Curve. The upward phase of the EKC is hard to capture
950 without agriculture. Agriculture is, of course, also the sector most exposed
951 to the impacts of climate change. Furthermore, the model abstracts from
952 distortions of the capital market and prior tax distortions. Such distortions
953 surely interact with climate policy and may well with Baumol's cost and cli-
954 mate diseases. Finally, technological progress is assumed to be exogenous.
955 The innovation public good interacts with the climate public bad. And, as
956 technological progress is at the heart of Baumol's cost disease, endogenizing
957 technological progress may well affect the results presented here. All these
958 are deferred to future research.

959 Until those complications are studied in detail, we conclude that climate
960 change causes a phenomenon that is similar to Baumol's cost diseases. Bau-
961 mol's climate disease, and its interaction with Baumol's cost diseases when
962 two diseases are complementary, increase the negative impacts of climate
963 change and so justifies more stringent climate policy.

964 **Acknowledgement**

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 972 expressed are our own and do not reflect the views of the supporting agencies
 973 or authors' affiliations.

974 **Appendix A. Proofs**

975 The first step is to show how capital accumulation equation Eq.(24) is ob-
 976 tained. We start with the representative household's problem and associated
 977 first order conditions. We assume throughout the solution to the household's
 978 problem is interior.

979 The representative household seeks to maximize lifetime utility according
 980 to:

$$U_0 \equiv \sum_{t=0}^{\infty} \beta^t U(C_t) \tag{A.1}$$

981 The household faces the following two constraints Eq.(6) and Eq.(7).

982 Eq.(6) describes how each kind of product is tranformed into final ag-
 983 gregate consumption, and Equation Eq.(7) is the budget constraint faced by
 984 the household. Letting ζ_t and γ_t be the Lagrange multiplier on Eq.(6) and
 985 Eq.(7) at time t respectively, the first order conditions are given by:

986 $[C_t]:$

$$\beta^t U_{C_t} = \zeta_t \tag{A.2}$$

987 $[C_{1t}]:$

$$\zeta_t F_{C_{1t}} = \gamma_t p_{1t} \tag{A.3}$$

988 $[C_{2t}]:$

$$\zeta_t F_{C_{2t}} = \gamma_t p_{2t} \tag{A.4}$$

989 $[K_{t+1}]$:

$$\gamma_{t+1}(1 + r_{t+1} - \delta) = \gamma_t \quad (\text{A.5})$$

990 For the producers of goods and services, their problems to maximize
991 profits are:

$$\max_{K_{it}, L_{it}, E_{it}} p_{it}Y_{it} - r_t K_{it} - w_t L_{it} - p_{et}E_{it}, \quad \text{where } i \in \{1, 2\} \quad (\text{A.6})$$

992 Thus, the first order conditions to each input factor satisfy:

$$\begin{aligned} p_{1t}F_{1lt} &= p_{2t}F_{2lt} = w_t & (\text{A.7}) \\ p_{1t}F_{1kt} &= p_{2t}F_{2kt} = r_t \\ p_{1t}F_{1Et} &= p_{2t}F_{2Et} = p_{Et} \end{aligned}$$

993 The investment producer solves:

$$\max_{I_{1t}, I_{2t}} p_{It}F_I(A_{It}, I_{1t}, I_{2t}) - p_{1t}I_{1t} - p_{2t}I_{2t} \quad (\text{A.8})$$

994 where the price of final investment product in each period is normalized to
995 one. The corresponding first order conditions are:

$$\begin{aligned} F_{I1t} &= p_{1t} & (\text{A.9}) \\ F_{I2t} &= p_{2t} \end{aligned}$$

996 For the energy sector, the representative firm solves:

$$\max_{K_{Et}, L_{Et}, \mu} \Pi_t = p_{Et}A_{Et}F_E(K_{Et}, L_{Et}) - [(1 - \mu_t)E_t]\tau_{Et} - w_t L_{Et} - r_t K_{Et} - \Theta_t(\mu_t E_t) \quad (\text{A.10})$$

997 The associated first-order conditions are:

$$\begin{aligned} (p_{Et} - \tau_{Et})F_{Elt} &= w_t & (\text{A.11}) \\ (p_{Et} - \tau_{Et})F_{Ekt} &= r_t \\ \tau_{Et} &= \Theta'_t(\mu_t E_t) \end{aligned}$$

998 Assume that the government only levies carbon tax and makes a lump-
999 sum transfer to the household:

$$Tran_t = [(1 - \mu_t)E_t]\tau_{Et} \quad (\text{A.12})$$

1000 Adding up the household's budget constraint (7), the definition of energy
 1001 profits (A.10), and the government transfer (A.12), we have:

$$p_{gt}C_{gt} + p_{st}C_{st} + K_{t+1} \leq w_t(L_t - L_{Et}) + (1 - \delta)K_t + p_{Et}E_t + r_t(K_t - K_{Et}) - \Theta_t(\mu_t E_t) \quad (\text{A.13})$$

1002 Substituting into the market clearing conditions as per capital, labor and
 1003 energy Eq.(19) gives:

$$p_{gt}C_{gt} + p_{st}C_{st} + K_{t+1} \leq w_t(L_{gt} + L_{st}) + (1 - \delta)K_t + p_{Et}(E_{gt} + E_{st}) + r_t(K_{gt} + K_{st}) - \Theta_t(\mu_t E_t) \quad (\text{A.14})$$

1004 Invoking the factor prices based on first order conditions (A.7) yields:

$$p_{gt}C_{gt} + p_{st}C_{st} + K_{t+1} \leq p_{gt}F_{glt}L_{gt} + p_{st}F_{slt}L_{st} + (1 - \delta)K_t + p_{gt}F_{gEt}E_{gt} + p_{st}F_{sEt}E_{st} + p_{gt}F_{gkt}K_{gt} + p_{st}F_{skt}K_{st} - \Theta_t(\mu_t E_t) \quad (\text{A.15})$$

1005 Substituting the Euler's theorem based on the assumption of constant returns
 1006 to scale in two final production sectors gives:

$$p_{gt}C_{gt} + p_{st}C_{st} + K_{t+1} \leq p_{gt}Y_{gt} + p_{st}Y_{st} + (1 - \delta)K_t + \Theta_t(\mu_t E_t) \quad (\text{A.16})$$

1007 Recalling the utilization rule of final production (12), the above equation can
 1008 be rewritten to:

$$K_{t+1} \leq p_{gt}I_{gt} + p_{st}I_{st} + (1 - \delta)K_t + \Theta_t(\mu_t E_t) \quad (\text{A.17})$$

1009 Revoking the Euler's theorem based on the assumption of constant returns
 1010 to scale in the investment production sector:

$$K_{t+1} \leq I_t + (1 - \delta)K_t + \Theta_t(\mu_t E_t) \quad (\text{A.18})$$

1011 This gives the capital accumulation constraint as in (24). The carbon cy-
 1012 cle constraint, the consumption aggregation constraint, the investment pro-
 1013 ducer's budget constraint and the energy producer's budget constraint all
 1014 hold by definition in competitive equilibrium.

1015

Thus, the social planner problem can be established as:

$$\begin{aligned}
& \max \sum_{t=0}^{\infty} \beta^t U(C_t) \\
& + \sum_{t=0}^{\infty} \beta^t \lambda_{1t} [F_1(A_{1t}, T_t, L_{1t}, K_{1t}, E_{1t}) - C_{1t} - I_{1t}] \\
& + \sum_{t=0}^{\infty} \beta^t \lambda_{2t} [F_2(A_{2t}, T_t, L_{2t}, K_{2t}, E_{2t}) - C_{2t} - I_{2t}] \\
& + \sum_{t=0}^{\infty} \beta^t \lambda_{Ct} [F_C(C_{1t}, C_{2t}) - C_t] \\
& + \sum_{t=0}^{\infty} \beta^t \lambda_{It} [F_I(A_{It}, I_{1t}, I_{2t}) + (1 - \delta)K_t - K_{t+1} - \Theta_t(\mu_t E_t)] \\
& + \sum_{t=0}^{\infty} \beta^t \xi_t \{T_t - \Phi[\mathbf{M}_0, (1 - \mu_0)(E_{10} + E_{20}), \dots, (1 - \mu_t)(E_{1t} + E_{2t}), \boldsymbol{\eta}_0, \dots, \boldsymbol{\eta}_t]\} \\
& + \sum_{t=0}^{\infty} \beta^t \chi_{lt} [L_t - L_{1t} - L_{2t} - L_{Et}] \\
& + \sum_{t=0}^{\infty} \beta^t \chi_{kt} [K_t - K_{1t} - K_{2t} - K_{Et}] \\
& + \sum_{t=0}^{\infty} \beta^t \chi_{Et} [A_{Et} F_E(K_{Et}, L_{Et}) - E_{1t} - E_{2t}]
\end{aligned} \tag{A.19}$$

1016

The F.O.C w.r.t. C_{1t} is:

$$\lambda_{Ct} \frac{\partial C_t}{\partial C_{1t}} = \lambda_{1t}$$

1017

The F.O.C w.r.t. C_{2t} is:

$$\lambda_{Ct} \frac{\partial C_t}{\partial C_{2t}} = \lambda_{2t}$$

1018

The F.O.C w.r.t. C_t is:

$$U_{Ct} = \lambda_{Ct}$$

1019 The F.O.C w.r.t. K_{t+1} is:

$$\beta\lambda_{I,t+1}(1 - \delta) + \beta\chi_{k,t+1} = \lambda_{It}$$

1020 The F.O.C w.r.t. K_{1t} is:

$$\lambda_{1t}F_{1kt} = \chi_{kt}$$

1021 The F.O.C w.r.t. K_{2t} is:

$$\lambda_{2t}F_{2kt} = \chi_{kt}$$

1022 The F.O.C w.r.t. K_{Et} is:

$$\chi_{Et}F_{Ekt} = \chi_{kt}$$

1023 The F.O.C w.r.t. I_{1t} is:

$$\lambda_{It}F_{I1t} = \lambda_{1t}$$

1024 The F.O.C w.r.t. I_{2t} is:

$$\lambda_{It}F_{I2t} = \lambda_{2t}$$

1025 The F.O.C w.r.t. L_{1t} is:

$$\lambda_{1t}F_{1lt} = \chi_{lt}$$

1026 The F.O.C w.r.t. L_{2t} is:

$$\lambda_{2t}F_{2lt} = \chi_{lt}$$

1027 The F.O.C w.r.t. L_{Et} is:

$$\chi_{Et}F_{Elt} = \chi_{lt}$$

1028 The F.O.C w.r.t. E_{1t} is:

$$\lambda_{1t}F_{1Et} - \lambda_{It}\mu_t\Theta' - \chi_{Et} = \sum_{j=0}^{\infty} \beta^j \xi_{t+j}(1 - \mu_t) \frac{\partial T_{t+j}}{\partial E_t^{unc}}$$

1029 The F.O.C w.r.t. E_{2t} is:

$$\lambda_{2t}F_{2Et} - \lambda_{1t}\mu_t\Theta' - \chi_{Et} = \sum_{j=0}^{\infty} \beta^j \xi_{t+j}(1 - \mu_t) \frac{\partial T_{t+j}}{\partial E_t^{unc}}$$

1030 The F.O.C w.r.t. T_t is:

$$\lambda_{1t} \frac{\partial Y_{1t}}{\partial T_t} + \lambda_{2t} \frac{\partial Y_{2t}}{\partial T_t} + \xi_t = 0$$

1031 The F.O.C w.r.t. μ_t is:

$$\lambda_{1t}\Theta' = \sum_{j=0}^{\infty} \beta^j \xi_{t+j} \frac{\partial T_{t+j}}{\partial E_t^{unc}}$$

1032 Rearranging above equations yields:

$$\begin{aligned} \Theta' &= F_{I1t}F_{1Et} - \frac{F_{I1t}F_{1lt}}{F_{Elt}} = F_{I2t}F_{2Et} - \frac{F_{I2t}F_{2lt}}{F_{Elt}} \\ &= (-1) \sum_{j=0}^{\infty} \beta^j \left\{ \frac{\lambda_{1,t+j}}{\lambda_{1t}} \frac{\partial Y_{1,t+j}}{\partial T_{t+j}} + \frac{\lambda_{2,t+j}}{\lambda_{1t}} \frac{\partial Y_{2,t+j}}{\partial T_{t+j}} \right\} \\ &= (-1) \sum_{j=0}^{\infty} \beta^j \left(\underbrace{\frac{U_{C,t+j}}{\lambda_{1t}} \frac{\partial C_{t+j}}{\partial C_{1,t+j}} \frac{\partial Y_{1,t+j}}{\partial T_{t+j}} \frac{\partial T_{t+j}}{\partial E_t^{unc}}}_{\text{Impacts on sector 1}} + \underbrace{\frac{U_{C,t+j}}{\lambda_{1t}} \frac{\partial C_{t+j}}{\partial C_{2,t+j}} \frac{\partial Y_{2,t+j}}{\partial T_{t+j}} \frac{\partial T_{t+j}}{\partial E_t^{unc}}}_{\text{Impacts on sector 2}} \right) \end{aligned} \quad (\text{A.20})$$

1033 where the government's discounting of output damages in period t is governed
1034 by:

$$\frac{\lambda_{1t}}{\beta\lambda_{1,t+1}} = F_{I1,t+1}F_{1k,t+1} + (1 - \delta) = F_{I2,t+1}F_{s2,t+1} + (1 - \delta) \quad (\text{A.21})$$

1035 *Q.E.D.*

1036 **Proof of Proposition 2**

1037 There are two final sectors in the economy. Each sector will employ rival
1038 factors including physical capital labor, and energy for production. Produc-
1039 tion in both sectors requires nonrival factors including knowledge capital and
1040 climate capital. Thus, the production functions are given by:

$$\begin{aligned} Y_{1t} &= \hat{F}_1(A_{1t}, T_t) K_{1t}^\alpha L_{1t}^{1-\alpha-\nu} E_{1t}^\nu \\ Y_{2t} &= \hat{F}_2(A_{2t}, T_t) K_{2t}^\alpha L_{2t}^{1-\alpha-\nu} E_{2t}^\nu \end{aligned} \quad (\text{A.22})$$

1041 In addition, there is an intermediate energy production using capital and
 1042 labor:

$$E_t = A_{Et} K_{Et}^{\alpha_E} L_{Et}^{1-\alpha_E} \quad (\text{A.23})$$

1043 Note that we assume the energy sector is immune to climate change.

1044 Then, market clearing conditions will be given by:

$$\begin{aligned} L_t &= L_{1t} + L_{2t} + L_{et} \\ K_t &= K_{1t} + K_{2t} + K_{et} \\ E_t &= E_{1t} + E_{2t} \end{aligned} \quad (\text{A.24})$$

1045 Firms in two final sectors shall decide their production plans to maximize
 1046 profits:

$$\max_{K_{it}, L_{it}, E_{it}} p_{it} Y_{it} - r_t K_{it} - w_t L_{it} - p_{Et} E_{it} \quad (\text{A.25})$$

1047 If the government implements no carbon tax, firms in energy sector will
 1048 decide their production plans according to:

$$\max_{K_{Et}, L_{Et}} p_{Et} E_t - r_t K_{Et} - w_t L_{Et} \quad (\text{A.26})$$

1049 Thus, one can obtain the identity across sectors using the interest rate:

$$\begin{aligned} r_t &= \alpha p_{1t} \hat{F}_1(A_{1t}, T_t) \left(\frac{K_{1t}}{L_{1t}} \right)^{\alpha-1} \left(\frac{E_{1t}}{L_{1t}} \right)^\nu \\ &= \alpha p_{2t} \hat{F}_2(A_{2t}, T_t) \left(\frac{K_{2t}}{L_{2t}} \right)^{\alpha-1} \left(\frac{E_{2t}}{L_{2t}} \right)^\nu \\ &= \alpha_E p_{Et} A_{Et} \left(\frac{K_{Et}}{L_{Et}} \right)^{\alpha_E-1} \end{aligned} \quad (\text{A.27})$$

1050 In a similar vein, the identity using the wage will be:

$$\begin{aligned} w_t &= (1 - \alpha - \nu) p_{1t} \hat{F}_1(A_{1t}, T_t) \left(\frac{K_{1t}}{L_{1t}} \right)^\alpha \left(\frac{E_{1t}}{L_{1t}} \right)^\nu \\ &= (1 - \alpha - \nu) p_{2t} \hat{F}_2(A_{2t}, T_t) \left(\frac{K_{2t}}{L_{2t}} \right)^\alpha \left(\frac{E_{2t}}{L_{2t}} \right)^\nu \\ &= (1 - \alpha_E) p_{Et} A_{Et} \left(\frac{K_{Et}}{L_{Et}} \right)^{-\alpha_E} \end{aligned} \quad (\text{A.28})$$

1051 Finally, the identity using the energy price is given by:

$$\begin{aligned}
p_{Et} &= \nu p_{1t} \hat{F}_1(A_{1t}, T_t) \left(\frac{K_{1t}}{L_{1t}} \right)^\alpha \left(\frac{E_{1t}}{L_{1t}} \right)^{\nu-1} \\
&= \nu p_{2t} \hat{F}_2(A_{2t}, T_t) \left(\frac{K_{2t}}{L_{2t}} \right)^\alpha \left(\frac{E_{2t}}{L_{2t}} \right)^{\nu-1}
\end{aligned} \tag{A.29}$$

1052 Combining the above three identities, the capital-labor ratios between
1053 three sectors should satisfy:

$$\frac{K_{1t}}{L_{1t}} = \frac{K_{2t}}{L_{2t}} = \frac{K_{Et}}{L_{Et}} \tag{A.30}$$

1054 Likewise, the energy-labor ratios between two final sectors should satisfy:

$$\frac{E_{1t}}{L_{1t}} = \frac{E_{2t}}{L_{2t}} \tag{A.31}$$

1055 Substituting Eq.(A.30)-Eq.(A.31) into Eq.(A.27) to Eq.(A.29), one can
1056 obtain the relative price of services to goods is given by:

$$\frac{p_{2t}}{p_{1t}} = \frac{\hat{F}_1(A_{1t}, T_t)}{\hat{F}_2(A_{2t}, T_t)} \tag{A.32}$$

1057 Given the production productions of consumption and investment Eq.(34)
1058 and Eq.(35), it is straightforward to show that the cost minimization problem
1059 for producing both yields:

$$\frac{p_{1t} C_{1t}}{p_{2t} C_{2t}} = \frac{\omega_c}{1 - \omega_c} \left(\frac{p_{1t}}{p_{2t}} \right)^{1-\epsilon_c} \tag{A.33}$$

$$\frac{p_{1t} I_{1t}}{p_{2t} I_{2t}} = \frac{\omega_I}{1 - \omega_I} \left(\frac{p_{1t}}{p_{2t}} \right)^{1-\epsilon_I} \tag{A.34}$$

1060 Substituting Eq.(A.32) into above gives:

$$\frac{C_{1t}}{C_{2t}} = \frac{\omega_c}{1 - \omega_c} \left(\frac{\hat{F}_1(A_{1t}, T_t)}{\hat{F}_2(A_{2t}, T_t)} \right)^{\epsilon_c} \tag{A.35}$$

$$\frac{I_{1t}}{I_{2t}} = \frac{\omega_I}{1 - \omega_I} \left(\frac{\hat{F}_1(A_{1t}, T_t)}{\hat{F}_2(A_{2t}, T_t)} \right)^{\epsilon_I} \tag{A.36}$$

1061 The consumption production function Eq.(34) can be rewritten in two
 1062 different ways:

$$C_t = \left(\omega_c^{\frac{1}{\epsilon_c}} + (1 - \omega_c)^{\frac{1}{\epsilon_c}} \left(\frac{C_{2t}}{C_{1t}} \right)^{\frac{\epsilon_c - 1}{\epsilon_c}} \right)^{\epsilon_c} C_{1t} \quad (\text{A.37})$$

$$C_t = \left(\omega_c^{\frac{1}{\epsilon_c}} \left(\frac{C_{1t}}{C_{2t}} \right)^{\frac{\epsilon_c - 1}{\epsilon_c}} + (1 - \omega_c)^{\frac{1}{\epsilon_c}} \right)^{\frac{\epsilon_c}{\epsilon_c - 1}} C_{2t} \quad (\text{A.38})$$

1063 Combining Eq.(A.35) and above two equations, we obtain:

$$C_t = \left(\omega_c^{\frac{1}{\epsilon_c}} + \frac{(1 - \omega_c)}{\omega_c^{\frac{\epsilon_c - 1}{\epsilon_c}}} \left(\frac{\hat{F}_2(A_{2t}, T_t)}{\hat{F}_1(A_{1t}, T_t)} \right)^{\frac{\epsilon_c - 1}{\epsilon_c}} \right)^{\frac{\epsilon_c}{\epsilon_c - 1}} C_{1t} \quad (\text{A.39})$$

$$C_t = \left(\frac{\omega_c}{(1 - \omega_c)^{\frac{\epsilon_c - 1}{\epsilon_c}}} \left(\frac{\hat{F}_1(A_{1t}, T_t)}{\hat{F}_2(A_{2t}, T_t)} \right)^{\frac{\epsilon_c - 1}{\epsilon_c}} + (1 - \omega_c)^{\frac{1}{\epsilon_c}} \right)^{\frac{\epsilon_c}{\epsilon_c - 1}} C_{2t} \quad (\text{A.40})$$

1064 Rearranging both equations and adding together, we have:

$$C_t = \left(\omega_c \hat{F}_1(A_{1t}, T_t)^{\epsilon_c - 1} + (1 - \omega_c) \hat{F}_2(A_{2t}, T_t)^{\epsilon_c - 1} \right)^{\frac{1}{\epsilon_c - 1}} \left(\frac{C_{1t}}{\hat{F}_1(A_{1t}, T_t)} + \frac{C_{2t}}{\hat{F}_2(A_{2t}, T_t)} \right) \quad (\text{A.41})$$

1065 In a similiar vein, for investment we have:

$$I_t = A_{It} \left(\omega_I \hat{F}_1(A_{1t}, T_t)^{\epsilon_I - 1} + (1 - \omega_I) \hat{F}_2(A_{2t}, T_t)^{\epsilon_I - 1} \right)^{\frac{1}{\epsilon_I - 1}} \left(\frac{I_{1t}}{\hat{F}_1(A_{1t}, T_t)} + \frac{I_{2t}}{\hat{F}_2(A_{2t}, T_t)} \right) \quad (\text{A.42})$$

1066 Thus, the transformation ratio between two definitions of social cost of
 1067 carbon is given by:

$$\begin{aligned} \frac{SCC_{CE}}{SCC_{IE}} &= \frac{\lambda_I}{\lambda_c} \\ &= \frac{F_{C1t}}{F_{I1t}} = \frac{F_{C2t}}{F_{I2t}} \\ &= \frac{\left[\omega_c \hat{F}_1(A_{1t}, T_t)^{\epsilon_c - 1} + (1 - \omega_c) \hat{F}_2(A_{2t}, T_t)^{\epsilon_c - 1} \right]^{\frac{1}{\epsilon_c - 1}}}{A_{It} \left[\omega_I \hat{F}_1(A_{1t}, T_t)^{\epsilon_I - 1} + (1 - \omega_I) \hat{F}_2(A_{2t}, T_t)^{\epsilon_I - 1} \right]^{\frac{1}{\epsilon_I - 1}}} \end{aligned} \quad (\text{A.43})$$

1069 **Appendix B. Calibration details**

Table B.4: Parameters in climate module common to all models

Parameters	Value	Sources & notes
Carbon cycle equations: $\begin{pmatrix} M_t^{At} \\ M_t^{Up} \\ M_t^{Lo} \end{pmatrix} = \begin{pmatrix} \phi_{11} & \phi_{21} & 0 \\ \phi_{12} & \phi_{22} & \phi_{32} \\ 0 & \phi_{23} & \phi_{33} \end{pmatrix} \begin{pmatrix} M_{t-1}^{At} \\ M_{t-1}^{Up} \\ M_{t-1}^{Lo} \end{pmatrix} + \begin{pmatrix} E_t^M + E_t^{Land} \\ 0 \\ 0 \end{pmatrix}$		
M_{2015}^{At}	851	Nordhaus (2017), GtC
M_{2015}^{Up}	460	Nordhaus (2017), GtC
M_{2015}^{Lo}	1740	Nordhaus (2017), GtC
E_{2015}^{Land}	2.6	GtCO2/year
E_t^{Land}	$E_{2015}^{Land}(0.885)^t$	Nordhaus (2017), per five years
$\phi - 11$	0.88	Nordhaus (2017)
ϕ_{21}	0.196	Nordhaus (2017)
ϕ_{12}	0.12	Nordhaus (2017)
ϕ_{22}	0.797	Nordhaus (2017)
ϕ_{23}	0.007	Nordhaus (2017)
ϕ_{32}	0.001	Nordhaus (2017)
ϕ_{33}	0.999	Nordhaus (2017)
Radiative forcings: $\chi_t = \kappa [\ln (M_t^{At} / M_{1750}^{At}) / \ln(2)] + \chi_t^{Ex}$		
κ	3.6813	
M_{1750}^{At}	588	Nordhaus (2017), GtC
χ_{2015}^{Ex}	0.5	Nordhaus (2017), Watt/m2
χ_{2100}^{Ex}	1	Nordhaus (2017), Watt/m2
Temperature: $\begin{pmatrix} T_t \\ T_t^{Lo} \end{pmatrix} = \begin{pmatrix} 1 - \zeta_1\zeta_2 - \zeta_1\zeta_3 & \zeta_1\zeta_3 \\ 1 - \zeta_4 & \zeta_4 \end{pmatrix} \begin{pmatrix} T_{t-1} \\ T_{t-1}^{Lo} \end{pmatrix} + \begin{pmatrix} \zeta_1\chi_t \\ 0 \end{pmatrix}$		
T_0	0.85	Nordhaus (2017), degree
T_0^{Lo}	0.0068	Nordhaus (2017), degree
ζ_1		Nordhaus (2017)
ζ_2		Nordhaus (2017)
ζ_3		Nordhaus (2017)
ζ_4		Nordhaus (2017)

Table B.5: Economic frontiers in the DICE-like model

Parameters	Value	Sources & notes
Preference: $U = \left[\left(\omega_c^{\frac{1}{\epsilon_c}} C_{1t}^{\frac{\epsilon_c-1}{\epsilon_c}} + (1 - \omega_c)^{\frac{1}{\epsilon_c}} C_{2t}^{\frac{\epsilon_c-1}{\epsilon_c}} \right)^{\frac{\epsilon_c}{\epsilon_c-1}} \right]^{1-\sigma} / (1 - \sigma)$		
σ	1.45	Nordhaus (2017)
β	0.985	Nordhaus (2017)
ω_c	0.5	Consumption expenditures are implicitly assumed to be equalized in the DICE model
ϵ_c	0.2	Table 1
Final production sectors: $Y_{it} = A_{it} K_{it}^\alpha L_{it}^{1-\alpha-\nu} E_{it}^\nu$, $i \in \{1, 2\}$		
α	0.3	Nordhaus (2017)
ν	0.03	Golosov et al. (2014)
Y_{2015}	105.1774	Nordhaus (2017), trillion 2010 US\$; $Y_t = p_{1t} Y_{1t} + p_{2t} Y_{2t}$ (note: $p_{1t} = p_{2t} = 1$)
$Y_{1,2015}$	35.3032	According to World Bank, the goods sector accounts for 33.47% in 2015, trillion 2010 US\$
$Y_{2,2015}$	69.8742	
K_{2015}	223	Nordhaus (2017), trillion 2010 US\$,
L_{2015}	7403	Nordhaus (2017), million, calibrated to Nordhaus (2017)
E_{2015}	35.85	Nordhaus (2017), GtCO2/year, carbon-based energy
$K_{1,2015}$	70.634	Net of factors used in energy sector, factor shares in two final sectors are equal to value added shares
$K_{2,2015}$	139.8029	
$L_{1,2015}$	2240.8038	
$L_{2,2015}$	4820.9785	
$E_{1,2015}$	23.8168	Energy shares in two final sectors are equal to value added shares
$E_{2,2015}$	12.0332	
$A_{1,2015}$	5.024	$= Y_{1,2015} / (K_{1,2015}^\alpha L_{1,2015}^{1-\alpha-\nu} E_{1,2015}^\nu)$
$A_{2,2015}$	5.024	$= Y_{2,2015} / (K_{2,2015}^\alpha L_{2,2015}^{1-\alpha-\nu} E_{2,2015}^\nu)$
$\gamma_{1,2015}$	0.076	Nordhaus (2017)
$\gamma_{2,2015}$	0.076	Nordhaus (2017)
Energy sector: $E_t = A_{Et} K_{Et}^{\alpha_E} L_{Et}^{1-\alpha_E}$		
$K_{E,2015}$	12.5631	Initial shares are pinned down according to equalized interest rate and wage between sectors
$L_{E,2015}$	131.2177	
α_E	0.597	Barrage (2020)
$A_{E,2015}$	17.9382	$= E_{2015} / (K_{E,2015}^{\alpha_E} L_{E,2015}^{1-\alpha_E})$
$\gamma_{E,2015}$	$(1 + \gamma_{1,2015})^{\frac{\alpha_E}{1-\alpha-\nu}} - 1$	Assume that energy sector shares the same labor-augmenting technical change as final sector
Investment production: $I_t = A_{It} \left(\omega_I^{\frac{1}{\epsilon_I}} I_{1t}^{\frac{\epsilon_I-1}{\epsilon_I}} + (1 - \omega_I)^{\frac{1}{\epsilon_I}} I_{2t}^{\frac{\epsilon_I-1}{\epsilon_I}} \right)^{\frac{\epsilon_I}{\epsilon_I-1}}$		
ω_c	0.5	Investment expenditures are implicitly assumed to be equalized in the DICE model
ϵ_c	0.5	Table 1
$A_{I,2015}$	1	Normalized
$\gamma_{I,2015}$	0	Assume no investment-specific technical change

Table B.6: Parameters in abatement cost function common to all models

Parameters	Value	Sources & notes
Abatement cost function: $\Theta_t(\mu_t E_t) = \frac{\bar{a} P_t^{backstop}}{1 + a_t \exp(b_{0t} - b_{1t}(\mu_t E_t)^{b_2})} \cdot (\mu_t E_t)$		
\bar{a}	0.7464	
a_t	$0.0236 + 0.8881t$	
b_{0t}	$7.8640 - 1.4858t$	Minimizing the gap with DICE
b_{1t}	$1.6791 - 0.3157t$	
b_2	0.4207	
$P_t^{backstop}$	$550 \times (1 - 0.025)^{t-1}$	Nordhaus (2017), per five year for a period, 2010US\$/tCO2

Table B.7: Homogeneous climate vulnerability in DICE-like models

Parameters	Value	Sources & notes
Damage function: $1 - D_i(T_t) = 1/(1 + \theta_i * T_t^2)$, $i \in \{1, 2\}$		
θ_1	0.00236	DICE implicitly assumes homogeneous climate vulnerability
θ_2	0.00236	between sectors

Table B.8: Economic modules with heterogeneous climate vulnerability in DICE-like models

Parameters	Value	Sources & notes
Final production sector: $Y_{it} = (1 - D_i(T_t)) A_{it} K_{it}^\alpha L_{it}^{1-\alpha-\nu} E_{it}^\nu$, $i \in \{1, 2\}$		
$Y_{1,2015}/((1 - D_1)$	35.3032	Table B.5
$Y_{2,2015}/((1 - D_2)$	69.8742	Table B.5
$K_{1,2015}$	70.5347	
$K_{2,2015}$	139.9023	
$L_{1,2015}$	2237.3701	In line with value added shares, adjusted by climate damages
$L_{2,2015}$	4834.4122	
$E_{1,2015}$	23.8337	
$E_{2,2015}$	12.0163	
$A_{1,2015}$	5.0311	$= Y_{1,2015}/((1 - D_1(T_{2015})) K_{1,2015}^\alpha L_{1,2015}^{1-\alpha-\nu} E_{1,2015}^\nu)$
$A_{2,2015}$	5.0205	$= Y_{2,2015}/((1 - D_1(T_{2015})) K_{2,2015}^\alpha L_{2,2015}^{1-\alpha-\nu} E_{2,2015}^\nu)$
Damage function: $1 - D_i(T_t) = 1/(1 + \theta_i * T_t^2)$, $i \in \{1, 2\}$		
θ_1	0.001414	Aggregate damage amounts to that of DICE, and the impact
θ_2	0.004352	on goods is three times that on services

Table B.9: Economic frontiers under structural change

Parameters	Value	Sources & notes
Preference: $U = \left[\left(\omega_c^{\frac{1}{\epsilon_c}} C_{1t}^{\frac{\epsilon_c-1}{\epsilon_c}} + (1 - \omega_c)^{\frac{1}{\epsilon_c}} C_{2t}^{\frac{\epsilon_c-1}{\epsilon_c}} \right)^{\frac{\epsilon_c}{\epsilon_c-1}} \right]^{1-\sigma}$		$/(1 - \sigma)$
σ	1.45	Nordhaus (2017)
β	0.985	Nordhaus (2017)
ω_c	0.75	Table 1
ϵ_c	0.2	Table 1
Final production sector: $Y_{it} = A_{it} K_{it}^{\alpha} L_{it}^{1-\alpha-\nu} E_{it}^{\nu}$, $i \in \{1, 2\}$		
α	0.3	Nordhaus (2017)
ν	0.03	Golosov et al. (2014)
Y_{2015}	105.1774	Nordhaus (2017), trillion 2010US\$; $Y_{2015} = p_{1,2015} Y_{1,2015} + p_{2,2015} Y_{2,2015}$, nominal production in the initial period is selected as the numéraire
$p_{1,2015} Y_{1,2015}$	35.3032	Based on value added shares in total nominal output
$p_{2,2015} Y_{2,2015}$	69.8742	
K_{2015}	223	Nordhaus (2017), trillion 2010US\$
L_{2015}	7403	Nordhaus (2017), million, calibrated to Nordhaus (2017)
E_{2015}	35.85	Nordhaus (2017), GtCO2/year, carbon-based energy
$K_{1,2015}$	70.634	Net of factors used in energy sector, factor shares in two final sectors are equal to value added shares
$K_{2,2015}$	139.8029	
$L_{1,2015}$	2240.8038	
$L_{2,2015}$	4820.9785	
$E_{1,2015}$	23.8168	Energy shares in two final sectors are equal to value added shares
$E_{2,2015}$	12.0332	
$p_{1,2015} A_{1,2015}$	5.024	$= p_{1,2015} Y_{1,2015} / (K_{1,2015}^{\alpha} L_{1,2015}^{1-\alpha-\nu} E_{1,2015}^{\nu})$
$p_{2,2015} A_{2,2015}$	5.024	$= p_{2,2015} Y_{2,2015} / (K_{2,2015}^{\alpha} L_{2,2015}^{1-\alpha-\nu} E_{2,2015}^{\nu})$
$\gamma_{1,2015}$	0.1086	Matching Table B.5 to obtain the same capital stock level in 2100
$\gamma_{2,2015}$	0.0362	
Energy sector: $E_t = A_{Et} K_{Et}^{\alpha_E} L_{Et}^{1-\alpha_E}$		
$K_{E,2015}$	12.5631	Initial shares are pinned down according to equalized interest rate and wage between sectors
$L_{E,2015}$	131.2177	
α_E	0.597	Barrage (2020)
$A_{E,2015}$	17.9382	$= E_{2015} / (K_{E,2015}^{\alpha_E} L_{E,2015}^{1-\alpha_E})$
$\gamma_{E,2015}$	$(1 + \gamma_{1,2015})^{\frac{\alpha_E}{1-\alpha-\nu}} - 1$	Assume that energy sector shares the same labor-augmenting technical change as final sector
Investment production: $I_t = A_{It} \left(\omega_I^{\frac{1}{\epsilon_I}} I_{1t}^{\frac{\epsilon_I-1}{\epsilon_I}} + (1 - \omega_I)^{\frac{1}{\epsilon_I}} I_{2t}^{\frac{\epsilon_I-1}{\epsilon_I}} \right)^{\frac{\epsilon_I}{\epsilon_I-1}}$		
ω_c	0.43	Table 3
ϵ_c	0.5	Table 3
$A_{I,2015}$	1	Normalized
$\gamma_{I,2015}$	0	Assume no investment-specific technical change

Table B.10: Homogeneous and heterogeneous climate vulnerability under structural change

Parameters	Value	Sources & notes
Parameters are the same as Table B.7 and Table B.8		

Table B.11: Parameters in counterfactual scenarios under structural change

Parameters	Value	Sources & notes
Final production sector: $Y_{it} = (1 - D_i(T_t))A_{it}K_{it}^\alpha L_{it}^{1-\alpha-\nu} E_{it}^\nu$, $i \in \{1, 2\}$		
$Y_{1,2015}/((1 - D_1))$	35.3032	Table B.5
$Y_{2,2015}/((1 - D_2))$	69.8742	Table B.5
$K_{1,2015}$	70.7335	
$K_{2,2015}$	139.7035	
$L_{1,2015}$	2444.2399	In line with value added shares, adjusted by climate damages
$L_{2,2015}$	4827.5424	
$E_{1,2015}$	23.8337	
$E_{2,2015}$	12.0501	
$p_{1,2015}A_{1,2015}$	5.0167	$= p_{1,2015}Y_{1,2015}/((1 - D_1(T_{2015}))K_{1,2015}^\alpha L_{1,2015}^{1-\alpha-\nu} E_{1,2015}^\nu)$
$p_{2,2015}A_{2,2015}$	5.0276	$= p_{2,2015}Y_{2,2015}/((1 - D_1(T_{2015}))K_{2,2015}^\alpha L_{2,2015}^{1-\alpha-\nu} E_{2,2015}^\nu)$
Damage function: $1 - D_i(T_t) = 1/(1 + \theta_i * T_t^2)$, $i \in \{1, 2\}$		
θ_1	0.004352	Aggregate damage amounts to that of DICE, and the impact on goods is three times that on services
θ_2	0.001414	

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